synthetic datasets

```
Warning: package 'bartMachine' was built under R version 4.3.3

Warning: package 'randomForest' was built under R version 4.3.3

Warning: package 'missForest' was built under R version 4.3.3

Warning: package 'dbarts' was built under R version 4.3.3

Warning: package 'BART' was built under R version 4.3.3

Warning: package 'bench' was built under R version 4.3.3
```

create dataset

```
linear_dgp_fun <- function(n_train, n_test, p, beta, noise_sd) {
    n <- n_train + n_test
    X <- matrix(rnorm(n * p), nrow = n, ncol = p)
    y <- X %*% beta + rnorm(n, sd = noise_sd)
    data_list <- list(
        X_train = X[1:n_train, , drop = FALSE],
        y_train = y[1:n_train],
        X_test = X[(n_train + 1):n, , drop = FALSE],
        y_test = y[(n_train + 1):n]
    )
    return(data_list)
}
linear_dgp <- create_dgp(
    .dgp_fun = linear_dgp_fun, .name = "Linear DGP",
    # additional named parameters to pass to .dgp_fun()
    n_train = 350, n_test = 120, p = 4, beta = c(1,2,1.5,3), noise_sd = 1
)</pre>
```

build BART model

```
BART_fun <- function(X_train, y_train, X_test, y_test, num_trees,alpha,beta) {
  train_X <- data.frame(X_train)</pre>
  test_X <- data.frame(X_test)</pre>
  t <- bench::mark(fit <- wbart(x.train = train_X,
                                          y.train = y_train,
                                          x.test = test X,
                                          ntree = num_trees,
                                           base = alpha,
                                          power = beta))
  time <- mean(t$time[[1]])</pre>
  predictions <- colMeans(fit$yhat.test)</pre>
  mse_score <- mean((y_test - predictions)^2)</pre>
 return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
}
dbarts_fun <- function(X_train, y_train, X_test, y_test, num_trees,alpha,beta){</pre>
  train_X <- data.frame(X_train)</pre>
  test_X <- data.frame(X_test)</pre>
  t <- bench::mark(bart_model <- bart(x.train = train_X,</pre>
                                          y.train = y_train,
                                          x.test = test_X,
                                          ntree = num_trees,
                                          base = alpha,
                                          power = beta))
  time <- mean(t$time[[1]])</pre>
  predictions <- colMeans(bart_model$yhat.test)</pre>
  mse_score <- mean((y_test - predictions)^2)</pre>
  return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
bartMachine_fun <- function(X_train, y_train, X_test,y_test,num_trees,alpha,beta){</pre>
  train_X <- data.frame(X_train)</pre>
  test_X <- data.frame(X_test)</pre>
  bart_model <- bartMachine(</pre>
          X = train_X,
          y = y_train,
          num_trees = num_trees,
          beta = beta,
```

```
alpha = alpha
                              )
                              # The value of calculating the time required for modeling
       time <- bart_model$time_to_build</pre>
       predictions <- predict(bart_model,test_X,type = "prob")</pre>
       mse_score <- mean((y_test - predictions)^2)</pre>
       return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
}
SoftBart_fun<- function(X_train, y_train, X_test,y_test,num_trees,alpha,beta){
       train_X <- data.frame(X_train)</pre>
       test_X <- data.frame(X_test)</pre>
       t <- bench::mark({bart_model <- softbart(X = train_X, Y = y_train, X_test = test_X, hyperatest = test_X, hyperates
                              #print(t)
       time <- mean(t$time[[1]])</pre>
       predictions <- bart_model$y_hat_test_mean</pre>
       mse_score <- mean((y_test - predictions)^2)</pre>
       return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
```

create evaluation

```
posterior_mse <- function(fit_results,truth_col,estimate_col){
    y_test = fit_results$truth_col
    pred = fit_results$estimate_col
    return(mean((y_test - pred)^2))
}

pred_err <- create_evaluator(
    .eval_fun = posterior_mse, .name = 'Posterior MSE',
    # additional named parameters to pass to .eval_fun()
    truth_col = "y_test", estimate_col = "predictions"
)

BART <- create_method(
    .method_fun = BART_fun, .name = "BART",
    # additional named parameters to pass to .method_fun()</pre>
```

```
num_trees=50,alpha=0.95,beta=2
)
dbarts <- create method(.method fun = dbarts fun,.name = "dbarts",</pre>
                       num_trees=50,alpha=0.95,beta=2)
bartMachine <- create_method(.method_fun = bartMachine_fun,.name = "bartMachine",</pre>
                       num_trees=50,alpha=0.95,beta=2)
SoftBart <- create_method(.method_fun = SoftBart_fun,.name = "SoftBart",</pre>
                       num_trees=50,alpha=0.95,beta=2)
# Create experiment
experiment <- create_experiment(name = "Test Experiment") %>%
  add_dgp(linear_dgp) %>%
  add_method(dbarts) %>%
  add_method(BART) %>%
  add_method(bartMachine) %>%
  add_method(SoftBart) %>%
  add_evaluator(pred_err)
results <- run_experiment(experiment, n_reps = 4, save = TRUE)
Fitting Test Experiment...
Warning: Some expressions had a GC in every iteration; so filtering is
disabled.
Saving fit results...
Fit results saved | time taken: 0.029452 seconds
4 reps completed (totals: 4/4) | time taken: 2.388415 minutes
Evaluating Test Experiment...
Warning: Unknown or uninitialised column: `truth_col`.
Warning: Unknown or uninitialised column: `estimate_col`.
Evaluation completed | time taken: 0.000029 minutes
Saving eval results...
Eval results saved | time taken: 0.037716 seconds
_____
No visualizers to visualize. Skipping visualization.
_____
```

results\$fit results

```
# A tibble: 16 x 7
         .dgp_name
                     .method_name time
                                                   mse y_test
                                                                    predictions
   .rep
   <chr> <chr>
                                  t>
                                                  <dbl> <list>
                                                                    st>
                     <chr>
                                  <bench_tm [1]> 1.50 <dbl [120]> <dbl [120]>
 1 1
         Linear DGP BART
                                  <bench_tm [1]> 1.48 <dbl [120]> <dbl [120]>
 2 1
         Linear DGP SoftBart
 3 1
         Linear DGP bartMachine <drtn [1]>
                                                  1.72 <dbl [120] > <dbl [120] >
 4 1
         Linear DGP dbarts
                                  <bench tm [1]> 1.37 <dbl [120]> <dbl [120]>
                                  <bench tm [1]> 1.25 <dbl [120]> <dbl [120]>
 5 2
         Linear DGP BART
 6 2
         Linear DGP SoftBart
                                  <bench tm [1]> 1.20 <dbl [120]> <dbl [120]>
 7 2
         Linear DGP bartMachine <drtn [1]>
                                                  1.49 <dbl [120] > <dbl [120] >
 8 2
         Linear DGP dbarts
                                  <bench_tm [1]> 1.23 <dbl [120]> <dbl [120]>
 9 3
         Linear DGP BART
                                  <bench tm [1]> 1.41 <dbl [120]> <dbl [120]>
10 3
         Linear DGP SoftBart
                                  <bench tm [1]> 1.21 <dbl [120]> <dbl [120]>
         Linear DGP bartMachine <drtn [1]>
                                                  1.45 <dbl [120] > <dbl [120] >
11 3
12 3
         Linear DGP dbarts
                                  <bench_tm [1]> 1.44 <dbl [120]> <dbl [120]>
13 4
         Linear DGP BART
                                  <bench_tm [1]> 1.51 <dbl [120]> <dbl [120]>
14 4
         Linear DGP SoftBart
                                  <bench_tm [1]> 1.12 <dbl [120]> <dbl [120]>
                                                  1.37 <dbl [120] > <dbl [120] >
15 4
         Linear DGP bartMachine <drtn [1]>
16 4
         Linear DGP dbarts
                                  <bench_tm [1]> 1.42 <dbl [120]> <dbl [120]>
BART_fun <- function(X_train, y_train, X_test, y_test, num_trees,alpha,beta) {
  train_X <- data.frame(X_train)</pre>
  test_X <- data.frame(X_test)</pre>
  t <- system.time(fit <- wbart(x.train = train_X,
                                        y.train = y_train,
                                        x.test = test X,
                                        ntree = num_trees,
                                        base = alpha,
                                        power = beta))
  time <- as.numeric(t["elapsed"])</pre>
  predictions <- colMeans(fit$yhat.test)</pre>
  mse_score <- mean((y_test - predictions)^2)</pre>
  return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
}
```

```
dbarts fun <- function(X train, y train, X test, y test, num trees, alpha, beta) {
  train_X <- data.frame(X_train)</pre>
  test X <- data.frame(X test)</pre>
  t <- system.time(bart_model <- bart(x.train = train_X,
                                          y.train = y train,
                                          x.test = test_X,
                                          ntree = num_trees,
                                          base = alpha,
                                          power = beta))
  time <- as.numeric(t["elapsed"])</pre>
  predictions <- colMeans(bart_model$yhat.test)</pre>
  mse_score <- mean((y_test - predictions)^2)</pre>
 return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
}
bartMachine_fun <- function(X_train, y_train, X_test,y_test,num_trees,alpha,beta){</pre>
  train_X <- data.frame(X_train)</pre>
  test_X <- data.frame(X_test)</pre>
  bart_model <- bartMachine(</pre>
          X = train_X,
          y = y_train,
          num trees = num trees,
          beta = beta,
          alpha = alpha
        # The value of calculating the time required for modeling
  time <- bart_model$time_to_build</pre>
  predictions <- predict(bart_model,test_X,type = "prob")</pre>
  mse_score <- mean((y_test - predictions)^2)</pre>
  return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
}
SoftBart_fun<- function(X_train, y_train, X_test,y_test,num_trees,alpha,beta){</pre>
  train_X <- data.frame(X_train)</pre>
  test X <- data.frame(X test)</pre>
  t <- system.time({bart_model <- softbart(X = train_X, Y = y_train, X_test = test_X, hypers
        #print(t)
  time <- as.numeric(t["elapsed"])</pre>
  predictions <- bart_model$y_hat_test_mean</pre>
```

```
mse_score <- mean((y_test - predictions)^2)</pre>
  return(list(time = time, mse=mse_score,y_test=y_test,predictions=predictions))
BART <- create method(
  .method_fun = BART_fun, .name = "BART",
  # additional named parameters to pass to .method_fun()
 num_trees=50,alpha=0.95,beta=2
dbarts <- create method(.method_fun = dbarts_fun,.name = "dbarts",
                        num_trees=50,alpha=0.95,beta=2)
bartMachine <- create_method(.method_fun = bartMachine_fun,.name = "bartMachine",</pre>
                        num_trees=50,alpha=0.95,beta=2)
SoftBart <- create_method(.method_fun = SoftBart_fun,.name = "SoftBart",</pre>
                        num_trees=50,alpha=0.95,beta=2)
# Create experiment
experiment <- create_experiment(name = "Test Experiment") %>%
  add dgp(linear dgp) %>%
 add_method(dbarts) %>%
  add method(BART) %>%
  add_method(bartMachine) %>%
  add_method(SoftBart) %>%
  add_evaluator(pred_err)
results <- run experiment(experiment, n_reps = 4, save = TRUE)
Fitting Test Experiment...
Saving fit results...
Fit results saved | time taken: 0.026530 seconds
4 reps completed (totals: 4/4) | time taken: 1.186117 minutes
Evaluating Test Experiment...
Warning: Unknown or uninitialised column: `truth_col`.
Warning: Unknown or uninitialised column: `estimate_col`.
```

```
if(as.numeric(results$fit_results$.rep)[4*1-3] == 1&&2 == 2){
  print(1)
}
```

[1] 1

```
gain_summary <- function(repeat_time, results_table){</pre>
  result <- data.frame()
 time_BART <- c()</pre>
 mse_BART <- c()</pre>
 time_dbarts <- c()</pre>
  mse_dbarts <- c()</pre>
  time_BM <- c()</pre>
  mse_BM <- c()
  time_SB <- c()
  mse_SB <- c()</pre>
  for (i in 1:repeat_time) {
    if(results_table\$.method_name[4*i-3] == "BART" &&
       as.numeric(results_table$.rep)[4*i-3]==i){
      time_BART[i] <- results_table$time[[4*i-3]]</pre>
      mse_BART[i] <- results_table$mse[4*i-3]</pre>
    if(results_table$.method_name[4*i-2] == "SoftBart"&&
       as.numeric(results_table$.rep)[4*i-2]==i){
      time_SB[i] <- results_table$time[[4*i-2]]</pre>
      mse_SB[i] <- results_table$mse[4*i-2]</pre>
    }
    if(results_table$.method_name[4*i-1] == "bartMachine"&&
       as.numeric(results_table\$.rep)[4*i-1]==i){
```

```
time_BM[i] <- results_table$time[[4*i-1]]</pre>
    mse BM[i] <- results table$mse[4*i-1]</pre>
  if(results_table$.method_name[4*i] == "dbarts"&&
     as.numeric(results table\$.rep)[4*i]==i){
    time_dbarts[i] <- results_table$time[[4*i]]</pre>
    mse_dbarts[i] <- results_table$mse[4*i]</pre>
  }
}
row_BART <- data.frame(MSE mean = mean(mse_BART), MSE se = sd(mse_BART),
                        running_time_mean = mean(time_BART),
                        running_time_sd = sd(time_BART),
                        package_name = "BART")
row_SB <- data.frame(MSE_mean = mean(mse_SB), MSE_se = sd(mse_SB),
                         running_time_mean = mean(time_SB),
                        running_time_sd = sd(time_SB),
                         package_name = "SoftBart")
row BM <- data.frame(MSE mean = mean(mse BM), MSE se = sd(mse BM),
                        running_time_mean = mean(time_BM),
                        running_time_sd = sd(time_BM),
                        package_name = "bartMachine")
row_dbarts <- data.frame(MSE_mean = mean(mse_dbarts), MSE_se = sd(mse_dbarts),</pre>
                        running time mean = mean(time dbarts),
                        running_time_sd = sd(time_dbarts),
                        package_name = "dbarts")
result <- rbind(result,row_BART)</pre>
result <- rbind(result,row_SB)</pre>
result <- rbind(result,row_BM)</pre>
result <- rbind(result,row_dbarts)</pre>
return(result)
```

```
summary <- gain_summary(repeat_time = 4,results_table = results$fit_results)
summary</pre>
```

```
MSE_mean
             MSE_se running_time_mean running_time_sd package_name
1 1.493237 0.1441812
                             0.6325000
                                            0.01707825
                                                                BART
                                                            SoftBart
2 1.245414 0.1216852
                            14.9450000
                                            0.32377976
                                            0.01711178 bartMachine
3 1.406950 0.2328272
                             0.4786825
4 1.482073 0.1401047
                             0.1550000
                                            0.01290994
                                                              dbarts
```

```
result <- data.frame()
time BART <- c()
mse BART <- c()
time_dbarts <- c()</pre>
mse dbarts <- c()
time_BM \leftarrow c()
mse_BM <- c()
time SB <- c()
mse_SB \leftarrow c()
for (i in 1:4) {
  if(results$fit_results$.method_name[4*i-3] == "BART" &&
    as.numeric(results$fit_results$.rep)[4*i-3]==i){
    time_BART[i] <- results$fit_results$time[[4*i-3]]</pre>
    mse_BART[i] <- results$fit_results$mse[4*i-3]</pre>
  if(results$fit results$.method name[4*i-2]=="SoftBart"&&
     as.numeric(results$fit results$.rep)[4*i-2]==i){
    time_SB[i] <- results$fit_results$time[[4*i-2]]</pre>
    mse_SB[i] <- results$fit_results$mse[4*i-2]</pre>
  if(results$fit_results$.method_name[4*i-1] == "bartMachine"&&
     as.numeric(results$fit results$.rep)[4*i-1]==i){
    time_BM[i] <- results$fit_results$time[[4*i-1]]</pre>
    mse_BM[i] <- results$fit_results$mse[4*i-1]</pre>
  if(results\fit_results\s.method_name[4*i] == "dbarts"&&
     as.numeric(results$fit_results$.rep)[4*i]==i){
    time_dbarts[i] <- results$fit_results$time[[4*i]]</pre>
    mse_dbarts[i] <- results$fit_results$mse[4*i]</pre>
  }
row BART <- data.frame(MSE mean = mean(mse BART), MSE se = sd(mse BART),
                        running_time_mean = mean(time_BART),
                        running_time_sd = sd(time_BART),
                        package_name = "BART")
row_SB <- data.frame(MSE_mean = mean(mse_SB), MSE_se = sd(mse_SB),</pre>
                        running_time_mean = mean(time_SB),
                        running_time_sd = sd(time_SB),
                        package_name = "SoftBart")
row_BM <- data.frame(MSE_mean = mean(mse_BM), MSE_se = sd(mse_BM),</pre>
                        running_time_mean = mean(time_BM),
```

result

package_name	running_time_sd	running_time_mean	MSE_se	${\tt MSE_mean}$	
BART	0.01707825	0.6325000	0.1441812	1.493237	1
${\tt SoftBart}$	0.32377976	14.9450000	0.1216852	1.245414	2
bartMachine	0.01711178	0.4786825	0.2328272	1.406950	3
dbarts	0.01290994	0.1550000	0.1401047	1.482073	4