Raymarching Distance Fields
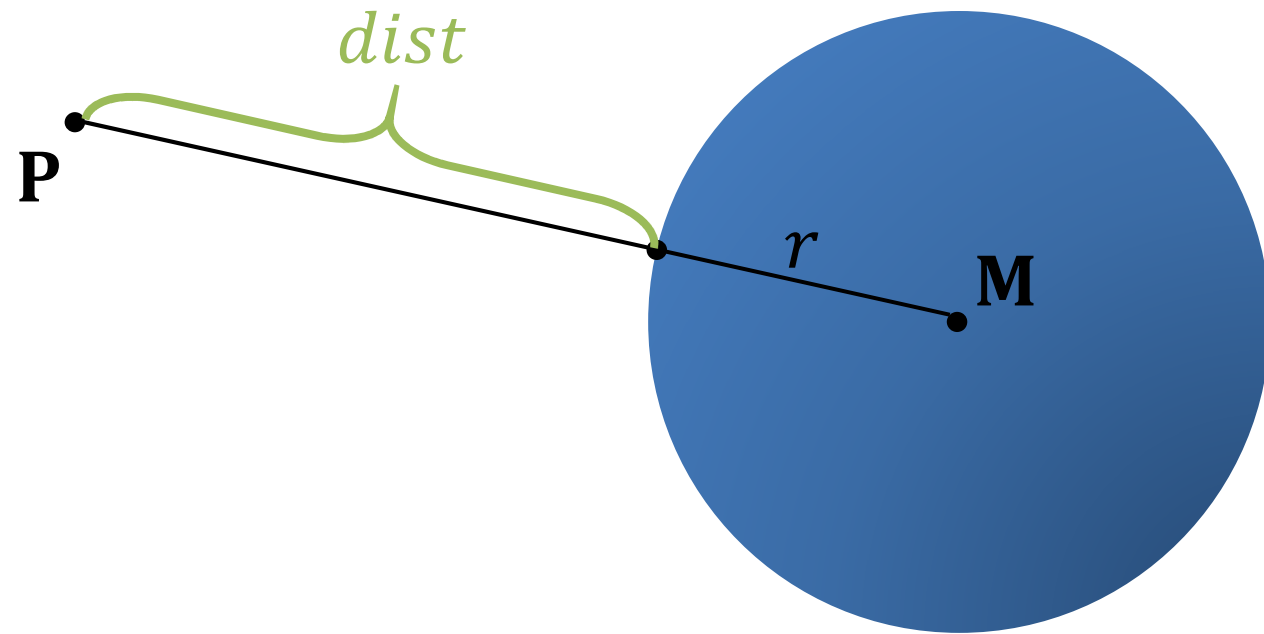
Distance Functions

- Distance function sphere
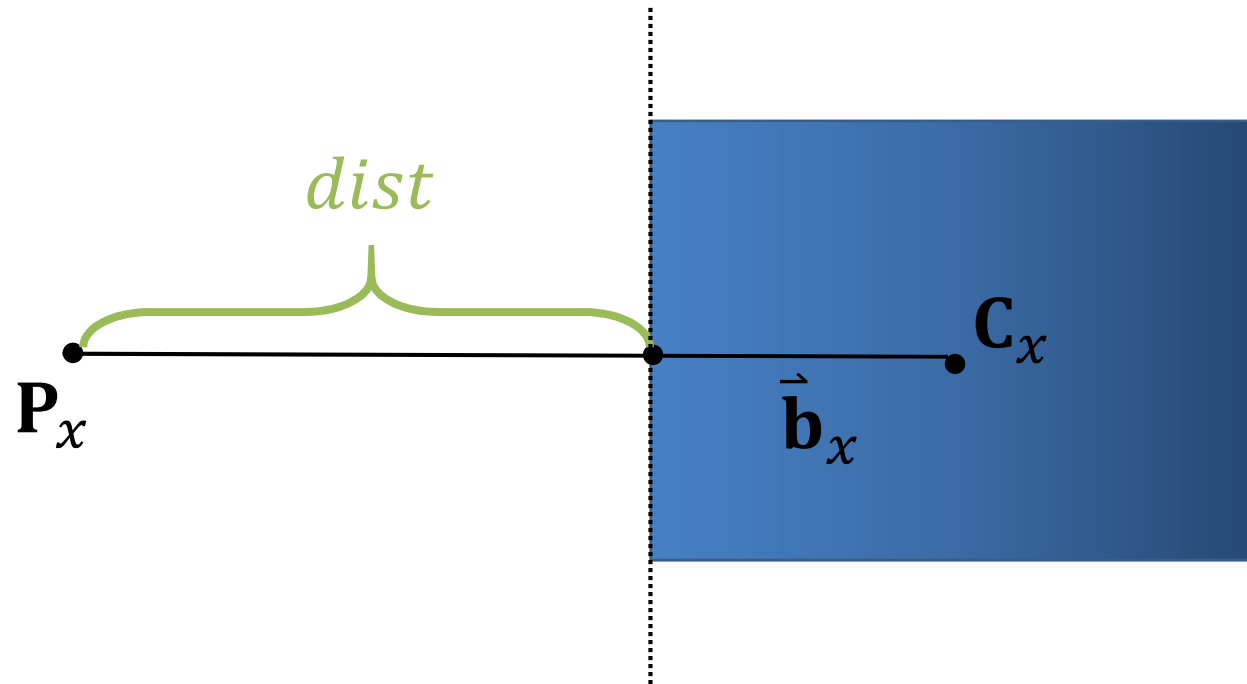 $$dist(\mathbf{P}) = \|\mathbf{P} - \mathbf{M}\| - r$$

Distance Functions
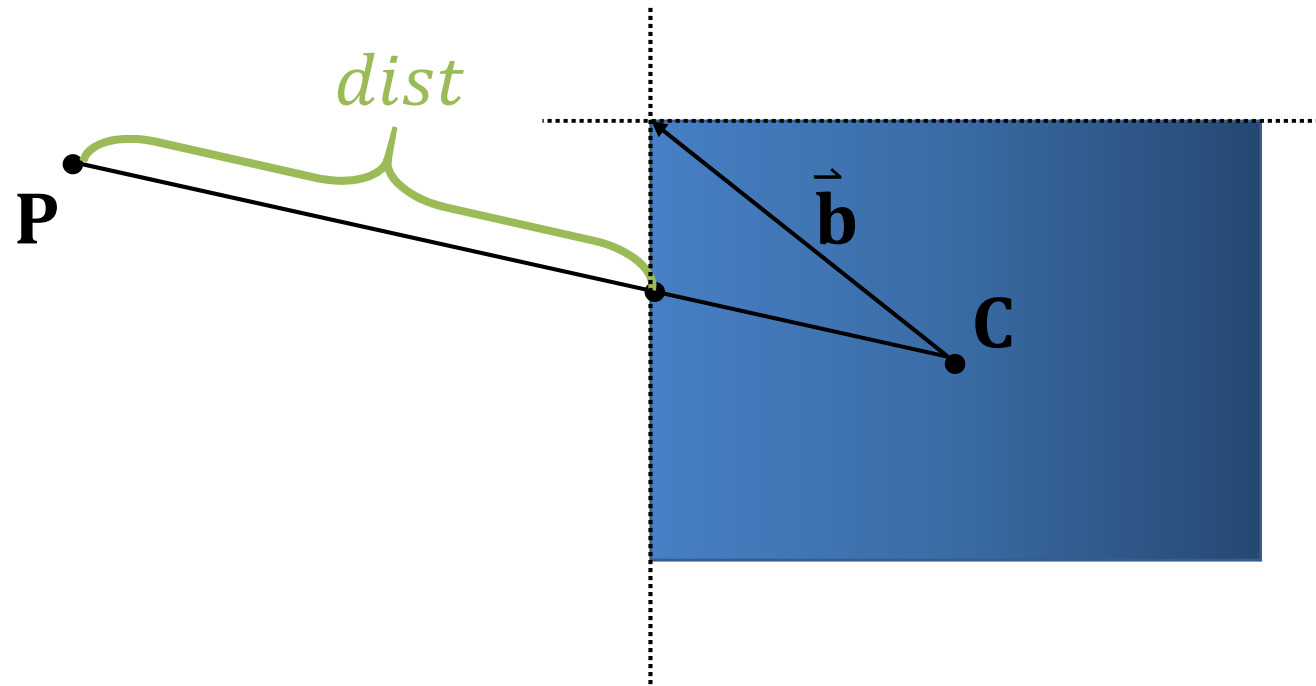
- Distance function box $- x$-direction

$$dist(\mathbf{P}_x) = \max\left(|\mathbf{P}_x - \mathbf{C}_x| - \vec{\mathbf{b}}_x, 0\right)$$
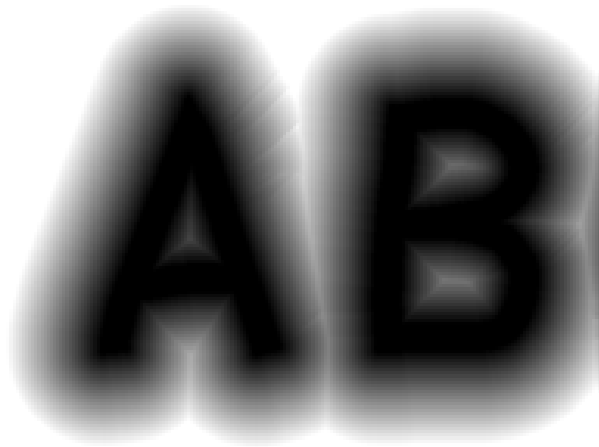
Distance Functions

- Distance function box

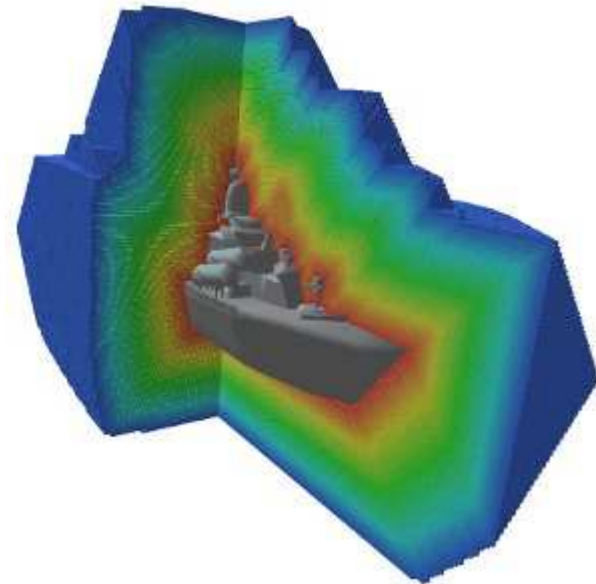$$dist(\mathbf{P}) = \left\| \max\left(|\mathbf{P} - \mathbf{C}| - \vec{\mathbf{b}}, \vec{\mathbf{0}} \right) \right\|$$
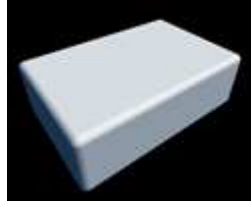
Distance Fields

$$\mathbb{R}^2 \to dist(\mathbb{R}^2)$$

$$\mathbb{R}^3 \to dist(\mathbb{R}^3)$$

Operations on Distance Fields

- Given $dist(\mathbb{R}^3) =$

 $= dist(repeat(\mathbb{R}^3)$
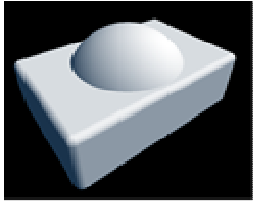
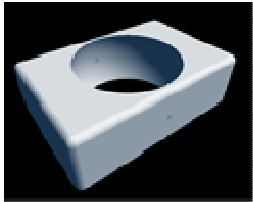- Repeat is $\mathrm{mod}\left(\mathbf{P}, \vec{\mathbf{b}}\right) - \frac{1}{2}\vec{\mathbf{b}}$

Operations on Distance Fields

- Given $dist_1(\mathbb{R}^3)$ and $dist_2(\mathbb{R}^3)$

 $= union\left(\;\;\;\;\;\;,\;\;\;\;\;\;\right)$

- The union is $\min(dist_1(\mathbb{R}^3), dist_2(\mathbb{R}^3))$

 $= substraction\left(\;\;\;\;\;\;,\;\;\;\;\;\;\right)$

- The substraction is $\max(-dist_1(\mathbb{R}^3), dist_2(\mathbb{R}^3))$

Raymarching Distance Fields

- $dist(\mathbf{P}_i)$