Assignment 3 (116 pts total)

Instructions

- This is an individual assignment. You are **not allowed** to discuss the problems with other students.
- Part of this assignment will be autograded by gradescope. You can use it as immediate feedback to improve your answers. You can resubmit as many times as you want.
- All your solution, code, analysis, graphs, explanations should be done in this same notebook.
- Please make sure to execute all the cells before you submit the notebook to the gradescope. You will not get points for the plots if they are not generated already.
- Please **do not** change the random seeds
- If you have questions regarding the assignment, you can ask for clarifications on Piazza. You should use the corresponding tag for this assignment.
- The deadline for submitting this assignment is 10:00
 PM on Sunday, November 5, 2023

This assignment has four parts. Part 1 will focus on the Monte Carlo method, you will learn:

1. To use the Monte Carlo method for control

Part 2 will focus on *prediction*. You will learn:

- 1. To use Monte Carlo estimates for prediction
- 2. To use Temporal difference methods for prediction
- To understand the relationship between the two, and unifying the algorithms

Part 3 will focus on Temporal Difference control methods. You will learn:

- 1. To use SARSA for optimal control
- 2. To use Q-learning for optimal control

Part 4 will focus on Deep Q-learning. You will learn:

1. To use and evaluate DQN for environments with continuous state spaces

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## INSTALL DEPENDENCIES
!pip install gymnasium
!pip install torch
!pip install matplotlib
!pip install tqdm

Requirement already satisfied: gymnasium in
/usr/local/lib/python3.10/dist-packages (0.29.1)
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Requirement already satisfied: numpy>=1.21.0 in
/usr/local/lib/python3.10/dist-packages (from gymnasium) (1.23.5)
Requirement already satisfied: cloudpickle>=1.2.0 in
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Requirement already satisfied: typing-extensions>=4.3.0 in
/usr/local/lib/python3.10/dist-packages (from gymnasium) (4.5.0)
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Requirement already satisfied: torch in
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Requirement already satisfied: filelock in
/usr/local/lib/python3.10/dist-packages (from torch) (3.12.2)
Requirement already satisfied: typing-extensions in
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Requirement already satisfied: sympy in
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Requirement already satisfied: networkx in
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Requirement already satisfied: jinja2 in
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(3.27.4.1)
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packages (from triton==2.0.0->torch) (16.0.6)
Requirement already satisfied: MarkupSafe>=2.0 in
/usr/local/lib/python3.10/dist-packages (from jinja2->torch) (2.1.3)
Requirement already satisfied: mpmath>=0.19 in
/usr/local/lib/python3.10/dist-packages (from sympy->torch) (1.3.0)
Requirement already satisfied: matplotlib in
/usr/local/lib/python3.10/dist-packages (3.7.1)
Requirement already satisfied: contourpy>=1.0.1 in
/usr/local/lib/python3.10/dist-packages (from matplotlib) (1.1.0)
Requirement already satisfied: cycler>=0.10 in
/usr/local/lib/python3.10/dist-packages (from matplotlib) (0.11.0)
Requirement already satisfied: fonttools>=4.22.0 in
/usr/local/lib/python3.10/dist-packages (from matplotlib) (4.42.1)
Requirement already satisfied: kiwisolver>=1.0.1 in
/usr/local/lib/python3.10/dist-packages (from matplotlib) (1.4.5)
Requirement already satisfied: numpy>=1.20 in
/usr/local/lib/python3.10/dist-packages (from matplotlib) (1.23.5)
Requirement already satisfied: packaging>=20.0 in
/usr/local/lib/python3.10/dist-packages (from matplotlib) (23.1)
Requirement already satisfied: pillow>=6.2.0 in
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Requirement already satisfied: pyparsing>=2.3.1 in
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Requirement already satisfied: python-dateutil>=2.7 in
/usr/local/lib/python3.10/dist-packages (from matplotlib) (2.8.2)
Requirement already satisfied: six>=1.5 in
/usr/local/lib/python3.10/dist-packages (from python-dateutil>=2.7-
>matplotlib) (1.16.0)
Requirement already satisfied: tqdm in /usr/local/lib/python3.10/dist-
packages (4.66.1)
!pip install otter-grader
!rm -rf public
!git clone https://github.com/chandar-lab/INF8250ae-assignments-2023
public
Requirement already satisfied: otter-grader in
/usr/local/lib/python3.10/dist-packages (5.2.2)
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Requirement already satisfied: jinja2 in
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Requirement already satisfied: pandas in
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Requirement already satisfied: PyYAML in
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Requirement already satisfied: python-on-whales in
/usr/local/lib/python3.10/dist-packages (from otter-grader) (0.65.0)
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Requirement already satisfied: docutils in
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Requirement already satisfied: sphinx in
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ipython->otter-grader) (3.0.39)
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Requirement already satisfied: entrypoints>=0.2.2 in
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Requirement already satisfied: fastjsonschema in
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/usr/local/lib/python3.10/dist-packages (from nbformat->otter-grader)
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(4.19.0)
Requirement already satisfied: python-dateutil>=2.8.1 in
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(2.8.2)
Requirement already satisfied: pytz>=2020.1 in
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(2023.3.post1)
Requirement already satisfied: numpy>=1.21.0 in
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Requirement already satisfied: pydantic!=2.0.*,<3,>=1.5 in
/usr/local/lib/python3.10/dist-packages (from python-on-whales->otter-
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(3.2.0)
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(3.4)
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(2.0.4)
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(2023.7.22)
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=3.0.1, <3.1.0, >=2.0.0->ipython->otter-grader) (0.2.6)
Requirement already satisfied: notebook>=4.4.1 in
/usr/local/lib/python3.10/dist-packages (from
widgetsnbextension~=3.6.0->ipywidgets->otter-grader) (6.5.5)
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Requirement already satisfied: snowballstemmer>=1.1 in
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Requirement already satisfied: nbclassic>=0.4.7 in
/usr/local/lib/python3.10/dist-packages (from notebook>=4.4.1-
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Requirement already satisfied: jupyter-server>=1.8 in
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>notebook>=4.4.1->widgetsnbextension~=3.6.0->ipywidgets->otter-grader)
(1.24.0)
Requirement already satisfied: notebook-shim>=0.2.3 in
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Requirement already satisfied: argon2-cffi-bindings in
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>notebook>=4.4.1->widgetsnbextension~=3.6.0->ipywidgets->otter-grader)
(21.2.0)
Requirement already satisfied: anyio<4,>=3.1.0 in
/usr/local/lib/python3.10/dist-packages (from jupyter-server>=1.8-
>nbclassic>=0.4.7->notebook>=4.4.1->widgetsnbextension~=3.6.0-
>ipywidgets->otter-grader) (3.7.1)
Requirement already satisfied: websocket-client in
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/usr/local/lib/python3.10/dist-packages (from jupyter-server>=1.8-
>nbclassic>=0.4.7->notebook>=4.4.1->widgetsnbextension~=3.6.0-
>ipywidgets->otter-grader) (1.6.2)
Requirement already satisfied: cffi>=1.0.1 in
/usr/local/lib/python3.10/dist-packages (from argon2-cffi-bindings-
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>otter-grader) (1.15.1)
Requirement already satisfied: sniffio>=1.1 in
/usr/local/lib/python3.10/dist-packages (from anyio<4,>=3.1.0-
>jupyter-server>=1.8->nbclassic>=0.4.7->notebook>=4.4.1-
>widgetsnbextension~=3.6.0->ipywidgets->otter-grader) (1.3.0)
Requirement already satisfied: exceptiongroup in
/usr/local/lib/python3.10/dist-packages (from anyio<4,>=3.1.0-
>jupyter-server>=1.8->nbclassic>=0.4.7->notebook>=4.4.1-
>widgetsnbextension~=3.6.0->ipywidgets->otter-grader) (1.1.3)
Requirement already satisfied: pycparser in
/usr/local/lib/python3.10/dist-packages (from cffi>=1.0.1->argon2-
cffi-bindings->argon2-cffi->notebook>=4.4.1-
>widgetsnbextension~=3.6.0->ipywidgets->otter-grader) (2.21)
Cloning into 'public'...
remote: Enumerating objects: 95, done.ote: Counting objects: 100%
(95/95), done.ote: Compressing objects: 100% (62/62), done.ote: Total
95 (delta 36), reused 78 (delta 22), pack-reused 0
## Initialize Otter
import otter
grader = otter.Notebook(colab=True, tests dir='./public/a3/tests')
import matplotlib.pyplot as plt
import random
import numpy as np
# Set seed
seed = 10
np.random.seed(seed)
random.seed(seed)
import warnings
warnings.filterwarnings('ignore')
```

Environment

Consider environment FloorIsLava, a Grid World variant of the FrozenLake-v0 environment (https://gymnasium.farama.org/environments/toy_text/frozen_lake/) from the OpenAI gym library. Assume that the agent here is navigating on a different planet, called Planet558, and the surface consists of mostly safe paths but with molten lava in certain tiles of the grid. The goal of the agent is to find the shortest path to safely reach the goal tile G from the start tile S on a 6x6 grid (or in general, any size). The safe walkable tiles are indicated by P and

the lava tiles are indicated by L. Going to the lava tile leads to the agent's destruction and termination of the episode.

Additionally, there is another tile T that magically teleports the agent to a new tile Z. The states are denoted by: $S = \{0, 1, 2, ..., 34, 35\}$ for a 6x6 grid.

The agent can move in the four cardinal directions, $A = \{left, down, right, up\}$, but the surface is slippery! Given a Slip_rate of $0 \le \xi < 1$, the agent will go in a random wrong direction with probability ξ .

The reward is -1 on all transitions, except for three cases that all result in the episode terminating: (1) The agent falling into a lava gets the agent a reward of -100, (2) The agent takes over 50 steps, after which the whole surface gets dissolved in lava and the agent gets a reward of -100, and (3) The agent reaches the goal state with a reward of 0. The discount factor for this environment should be set to $\gamma = 0.99$. The environment is implemented for you below.

Example 6x6 FloorIsLava environment

S	Р	Р	Р	T	Р
P	Р	Р	L	Р	S
P	Р	Р	P	Р	Р
Р	Ц	P	P	L	Р
P	Р	Z	P	L	Р
P	Р	Р	Р	G	Р

```
import sys
from contextlib import closing
from tqdm import tqdm
import torch
import copy
import numpy as np
from io import StringIO
import gymnasium as gym
from gymnasium import utils
from gymnasium import Env, spaces
from gymnasium.utils import seeding
LEFT = 0
DOWN = 1
RIGHT = 2
UP = 3
MAPS = {
    "2x2": ["SP", "PG"],
    "4x4-easy":["SPPP", "PLPP", "PPLL", "LPPG"],
    "4x4": ["SPPT", "PLPL", "PPLZ", "LPPG"],
    "6x6": [
        "SPPTPL",
        "PPPLPP"
        "PPPPPP",
```

```
"PLPPLP", "PPZPLP",
        "PPLPGP",
    ],
}
def categorical sample(prob n, np random):
    Sample from categorical distribution
    Each row specifies class probabilities
    prob n = np.asarray(prob n)
    csprob n = np.cumsum(prob n)
    return (csprob_n > np_random.random()).argmax()
class DiscreteEnv(Env):
   Has the following members
    - nS: number of states
    - nA: number of actions
    - P: transitions (*)
    - isd: initial state distribution (**)
    (*) dictionary of lists, where
     P[s][a] == [(probability, nextstate, reward, done), ...]
    (**) list or array of length nS
    def init (self, nS, nA, P, isd, max length=50):
        self.P = P
        self.isd = isd
        self.lastaction = None # for rendering
        self.nS = nS
        self.nA = nA
        self.action space = spaces.Discrete(self.nA)
        self.observation space = spaces.Discrete(self.nS)
        self.seed()
        self.s = categorical sample(self.isd, self.np random)
        self.max length = max length
    def seed(self, seed=None):
        self.np random, seed = seeding.np random(seed)
        return [seed]
    def reset(self):
```

```
self.s = categorical sample(self.isd, self.np random)
        self.lastaction = None
        self.t = 0
        info = \{\}
        return int(self.s), info
    def step(self, a):
        transitions = self.P[self.s][a]
        i = categorical_sample([t[0] for t in transitions],
self.np random)
        p, s, r, d = transitions[i]
        self.s = s
        self.lastaction = a
        trunc = False
        if self.t >= self.max length:
            d = True
            r = -100
        self.t += 1
        return (int(s), r, trunc, d, {"prob": p})
class FloorIsLava(DiscreteEnv):
    You are building small rovers to explore Planet558 and search for
rare minerals.
   Assume you have an accurate simulation model of the actual
environment in
    Planet558 (including the presence of lava regions at a particular
instant),
    and locations of mineral sites where the rovers have to
    reach and send signals back to Earth regarding the chemical
composition. You
    are required to load one of the rovers with a trained policy
corresponding
    to the specific Grid World problem that it has to encounter, where
the policy
    is obtained by training with a simulation model environment. Note
the slippery
    nature of the surface, which poses further problems for the rover.
    The surface is described using a grid like the following
        SPPT
        PLPL
        PPPL
        LZPG
    S : starting point, safe
    P : safe path tile
    L : lava, the rover falls to its doom
    T: teleport, a magical phenomenon that teleports the rover to a
different tile
    Z : teleport destination, the rover teleports to this location
```

```
when it encounters T
    G : goal, where the mineral site is located
    The episode ends when you reach the goal or fall in the lava.
    metadata = {"render.modes": ["human", "ansi"]}
    def init (self, desc=None, map name="4x4", slip rate=0.5):
        if map name not in MAPS:
            raise ValueError(f"Invalid map: {map name}")
        desc = MAPS[map name]
        self.desc = desc = np.asarray(desc, dtype="c")
        self.nrow, self.ncol = nrow, ncol = desc.shape
        self.reward range = (0, 1)
        nA = 4
        nS = nrow * ncol
        isd = np.array(desc == b"S").astype("float64").ravel()
        isd /= isd.sum()
        tele in = np.where(np.array(desc ==
b"T").astype("float64").ravel())[0] # teleportation state
        tele out = np.where(np.array(desc ==
b"Z").astype("float64").ravel())[0] # teleport destination state
        P = \{s: \{a: [] \text{ for a in } range(nA)\} \text{ for s in } range(nS)\}
        def to s(row, col):
            return row * ncol + col
        def inc(row, col, a):
            if a == LEFT:
                col = max(col - 1, 0)
            elif a == DOWN:
                row = \min(row + 1, nrow - 1)
            elif a == RIGHT:
                col = min(col + 1, ncol - 1)
            elif a == UP:
                row = max(row - 1, 0)
            return (row, col)
        def update probability matrix(row, col, action):
            newrow, newcol = inc(row, col, action)
            newstate = to s(newrow, newcol)
            newletter = desc[newrow, newcol]
            done = bytes(newletter) in b"GH"
            # reward = float(newletter == b"G")
            reward = -1
            # if newletter == b"H":
                  reward = -100
            done = False
```

```
return newstate, reward, done
        for row in range(nrow):
            for col in range(ncol):
                s = to s(row, col)
                for a in range(4):
                    li = P[s][a]
                    letter = desc[row, col]
                    if letter == b"G":
                        li.append((1.0, s, 0, True))
                    elif letter == b'L':
                        li.append((1.0, s, -100, True))
                    elif letter == b'T':
                        if s == tele in[0]:
                            li.append((1.0, tele out[0], -1, False))
                    else:
                        if slip rate > 0:
                            li.append((1 - slip_rate,
*update probability matrix(row, col, a)))
                            li.append((slip rate/3.0,
*update probability matrix(row, col, (a - 1) % 4)))
                            li.append((slip_rate/3.0,
*update probability matrix(row, col, (a + 1) % 4)))
                            li.append((slip_rate/3.0,
*update probability matrix(row, col, (a + 2) % 4)))
                        else:
                            li.append((1.0,
*update probability matrix(row, col, a)))
        super(FloorIsLava, self). init (nS, nA, P, isd)
    def render(self, mode="human"):
        outfile = StringIO() if mode == "ansi" else sys.stdout
        row, col = self.s // self.ncol, self.s % self.ncol
        desc = self.desc.tolist()
        desc = [[c.decode("utf-8") for c in line] for line in desc]
        desc[row][col] = utils.colorize(desc[row][col], "red",
highlight=True)
        if self.lastaction is not None:
            outfile.write(
                   ({})\n".format(["Left", "Down", "Right", "Up"]
[self.lastaction])
        else:
            outfile.write("\n")
        outfile.write("\n".join("".join(line) for line in desc) + "\
n")
        if mode != "human":
```

```
with closing(outfile):
    return outfile.getvalue()
```

Part 0 - Helper Methods (5pts)

First, let us define some helper methods that will be useful for the entire assignment. We give here three methods that you may use or not use at any point of the assignment

```
def random_policy(state):
    """
    Input: state (int) [0, .., 35]
    output: action (int) [0,1,2,3]
    return np.random.randint(0,4)

def plot_many(experiments, label=None, color=None):
    mean_exp = np.mean(experiments, axis=0)
    std_exp = np.std(experiments, axis=0)
    plt.plot(mean_exp, color=color, label=label)
    plt.fill_between(range(len(experiments[0])), mean_exp + std_exp,
mean_exp - std_exp, color=color, alpha=0.1)

def random_argmax(value_list):
    """ a random tie-breaking argmax """
    values = np.asarray(value_list)
    return np.argmax(np.random.random(values.shape) *
(values==values.max()))
```

Question 0.1 - Creating some helper methods (5pts)

Question 0.1a (2 pts)

Implement an epsilon-greedy policy over the state-action values of an environment.

Note: Please make use of the random_argmax function for only this part, and NOT Part 4.

Question 0.1b (3 pts)

b) Create a function <code>generate_episode</code> which takes as input a policy π (like the one outputted by <code>question 1a</code>), the environment, and the boolean <code>render</code> which renders every step of the episode in text form (rendering the episode is as easy as calling <code>env.render()</code>). The output of this function should return the tuple states, actions, rewards containing the states, actions, and rewards of the generated episode following π .

```
def generate episode(policy:callable, env:gym.Env, render=False):
    Input:
        policy (int -> int): policy taking a state as an input and
outputs a given action
        env (DiscreteEnv): The FloorIsLava environment
        render (bool): Whether or not to render the episode
    Returns:
        states (list): the sequence of states in the generated episode
        actions (list): the sequence of actions in the generated
episode
        rewards (list): the sequence of rewards in the generated
episode
    states = []
    rewards = []
    actions = []
    terminated = False
    truncated = False
    obs, info = env.reset()
    states.append(obs)
    if render:
```

Part 1 - Monte Carlo Methods (15 pts)

Consider in this section the 6x6 version of the FloorIsLava environment, with a slip_rate of 0.1. Again, make sure to use a discount factor of y = 0.99 for all your experiments. This environment can be instantiated with env = FloorIsLava(map_name="6x6", slip rate=0.1)

Question 1.1 (15 pts)

Question 1.1a (5pts)

Implement the first-visit Monte Carlo (for ϵ -soft policies) control algorithm to find the approximate optimal policy $\pi \approx \pi_{\epsilon}$.

Given your implementation of fv mc estimation, we can now do control.

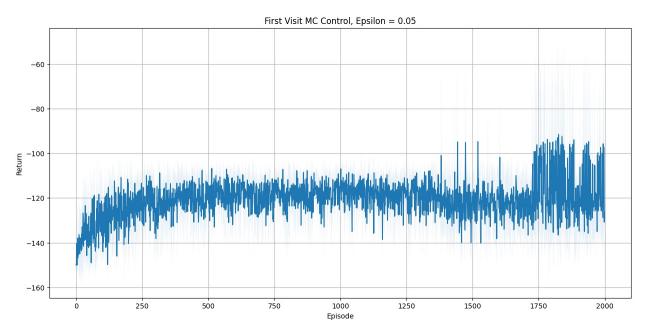
```
def fv_mc_control(env, epsilon=0.05, num_episodes=100, discount=0.99):
   # Initialize memory of estimated state-action returns
    state action returns = [[[] for j in range(env.action space.n)]
for i in range(env.observation space.n)]
   all_returns = []
    for j in range(num episodes):
        state action values = [[np.mean(a) for a in s] for s in
state action returns]
        policy = make eps greedy policy(state action values, epsilon)
        states, actions, rewards = generate episode(policy, env)
        visited states returns = fv mc estimation(states, actions,
rewards, discount)
        for sa in visited states returns:
            s, a = sa
            state action returns[s]
[a].append(visited states returns[sa])
        all returns.append(np.sum(rewards))
    state action values = [[np.mean(a) for a in s] for s in
state action returns]
    return state action values, all returns
```

Question 1.1b - Plotting (3pts)

Let ϵ = 0.05, run the algorithm for 2000 episodes, and repeat this experiment for 5 different runs. Plot the average undiscounted return across the 5 different runs with respect to the number of episodes (x-axis is the 2000 episodes, y-axis is the return for each episode)

```
env = FloorIsLava(map_name="6x6", slip_rate=0.1)
# Set seed
```

```
seed = 10
env.seed(seed)
np.random.seed(seed)
random.seed(seed)
all sa values, all returns = [], []
for t in range(5):
    sa values, returns = fv mc control(env, epsilon=0.05,
num episodes=2000)
    all sa values.append(sa values)
    all returns.append(returns)
plt.figure(figsize=(15,7))
plt.xlabel('Episode')
plt.ylabel('Return')
plt.title('First Visit MC Control, Epsilon = 0.05')
plt.grid()
plot many(all returns)
```



Question 1.1c (2 pts)

Visualize an episode during evaluation with the last learned state-action value tables using the code below. For clarity, let's evaluate an episode with 0 slip_rate and $\epsilon = 0$. In the absence of a slip-rate and exploration, what is the return of the optimal policy for all 5 learned state-action value tables?

```
# Visualize path
env = FloorIsLava(map_name="6x6", slip_rate=0.)
optimal_policy = make_eps_greedy_policy(all_sa_values[-1], epsilon=0.)
```

```
s, a, r = generate_episode(optimal_policy, env, render=True)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Down)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Up)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Left)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Down)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Right)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Down)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
```

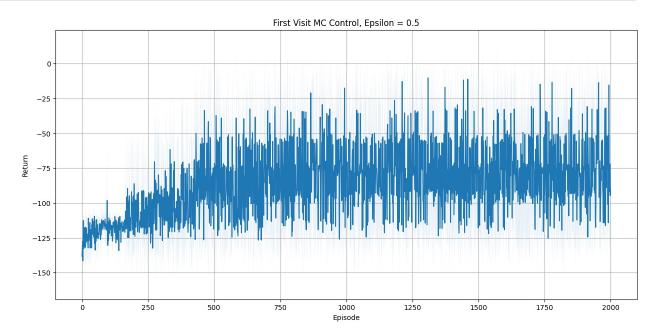
```
PPZPLP
PPLPGP
  (Left)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
 (Left)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
 (Left)
SPPTPL
PPPLPP
PPPPP
PLPPLP
PPZPLP
PPLPGP
 (Up)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Left)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
 (Left)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
 (Down)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
```

```
PPZPLP
PPLPGP
  (Left)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
 (Right)
SPPTPL
PPPLPP
PPPPP
PLPPLP
PPZPLP
PPLPGP
  (Down)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Up)
SPPTPL
PPPLPP
PPPPP
PLPPLP
PPZPLP
PPLPGP
# Getting the return during evaluation
env = FloorIsLava(map_name="6x6", slip_rate=0.)
for t in range(5):
    optimal policy = make eps greedy policy(all sa values[t],
epsilon=0.)
    s, a, r = generate_episode(optimal_policy, env, render=False)
    print('Return is ' + str(np.sum(r)))
Return is -123
Return is -104
Return is -116
Return is -150
Return is -108
```

Question 1.1d - Plotting again (2pts)

Now repeat the exercise from b), but set $\epsilon = 0.5$.

```
env = FloorIsLava(map name="6x6", slip rate=0.1)
# Set seed
env.seed(seed)
np.random.seed(seed)
random.seed(seed)
all sa values c, all returns c = [], []
for t in range(5):
    sa values, returns = fv mc control(env, epsilon=0.5,
num episodes=2000)
    all_sa_values_c.append(sa_values)
    all returns c.append(returns)
plt.figure(figsize=(15,7))
plt.xlabel('Episode')
plt.ylabel('Return')
plt.title('First Visit MC Control, Epsilon = 0.5')
plt.grid()
plot many(all returns c)
```



```
# Visualize path taken
env = FloorIsLava(map_name="6x6", slip_rate=0.)
optimal_policy = make_eps_greedy_policy(all_sa_values_c[-1],
epsilon=0.)
s, a, r = generate_episode(optimal_policy, env, render=True)
```

```
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Right)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
 (Right)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Right)
SPPTPL
PPPLPP
PPPPP
PLPPLP
PPZPLP
PPLPGP
 (Down)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Right)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
 (Down)
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
(Right)
```

```
SPPTPL
PPPLPP
PPPPPP
PLPPLP
PPZPLP
PPLPGP
  (Right)
SPPTPL
PPPLPP
PPPPP
PLPPLP
PPZPLP
PPLPGP
# Get evaluation return
for t in range(5):
    env = FloorIsLava(map name="6x6", slip rate=0.)
    optimal_policy = make_eps_greedy_policy(all_sa_values_c[t],
epsilon=0.)
    s, a, r = generate episode(optimal policy, env, render=False)
    print('Return is ' + str(np.sum(r)))
Return is -150
Return is -7
Return is -9
Return is -7
Return is -7
```

Question 1.1e (3pts)

Based on the returns obtained from policies from the learned sate-action value tables, compare the learning performances with $\epsilon = 0$ and $\epsilon = 0.5$. In which case the agent learns better, i.e. does higher exploration encourage better policies? What do you notice while visualizing the suboptimal policies? Briefly explain why in 1 to 3 sentences.

Higher exploration with ϵ =0.5 leads to better learning performance, as it converges in 500 episodes with an average return of around -75, compared to ϵ =0, which converges in 250 episodes but achieves only an average return of -120 to -100. The increased variance in ϵ =0.5 signifies more extensive exploration, allowing the agent to escape suboptimal policies and find better ones

Part 2 - Prediction: Unifying Monte Carlo methods and Temporal Difference Learning (46 pts)

Consider in this section the same 6x6 FloorIsLava environment with a slip_rate of 0.1. Use a discount factor of γ = 0.99. We will be working with the same random policy used above for all questions in this part: $\pi(a \lor s)$ =0.25 for all a and s.

Question 2.1 - MC (10 pts)

Question 2.1a (5 pts)

Implement the *Every visit Monte Carlo prediction* algorithm in order to estimate $V^{\pi}(s)$.

```
def ev_mc_estimate(states, actions, rewards, discount):
    Input:
        states (list): states of an episode generated from
generate episode
        actions (list): actions of an episode generated from
generate episode
        rewards (list): rewards of an episode generated from
generate episode
        discount (float): discount factor
    Returns visited states returns (dictionary):
        Keys are all the states visited in an the given episode
        Values is a list of the estimated MC return of a given state.
            i.e: if a state is visited 3 times in an episode, there
are 3 estimated returns of that state.
    visited state returns = {}
    # TO IMPLEMENT
    G = 0
    for t in range(len(states)-2, -1, -1):
        G = discount * G + rewards[t]
        if states[t] not in visited state returns:
            visited state returns[states[t]] = [G]
        else:
            visited_state_returns[states[t]].append(G)
    return visited state returns
grader.check("question 2.1a")
question 2.1a results: All test cases passed!
```

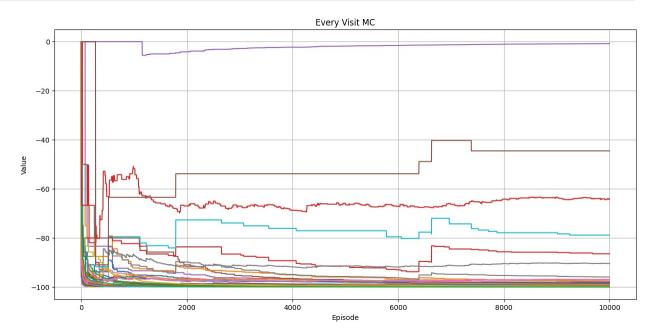
```
def ev_mc_pred(policy, env, num_episodes=100, discount=0.99):
    state_returns = [[0] for i in range(env.observation_space.n)]
    state_values_trace = []
    for j in (range(num_episodes)):
        states, actions, rewards = generate_episode(policy, env)
        visited_state_returns = ev_mc_estimate(states, actions,
rewards, discount)
    for s in visited_state_returns:
        state_returns[s].extend(visited_state_returns[s])
    state_values_trace.append([np.mean(s) for s in state_returns])
    return state_values_trace
```

Question 2.1b - Plotting (5 pts)

Train the algorithm for 10000 episodes, and plot the learning curves for each s of $V^{\pi}(s)$ over the number of episodes. The result should be 1 figure, with 36 curves plotted inside it (one for each state, x-axis is the 10000 episodes, y-axis is the current estimate of $V^{\pi}(s)$)

```
env = FloorIsLava(map name="6x6", slip rate=0.1)
# Set seed
seed = 10
env.seed(seed)
np.random.seed(seed)
random.seed(seed)
ev_state_vals = ev_mc_pred(random policy, env, num episodes=10000,
discount=0.99)
plt.figure(figsize=(15,7))
plt.xlabel('Episode')
plt.ylabel('Value')
plt.title('Every Visit MC')
plt.grid()
plt.plot(ev state vals)
[<matplotlib.lines.Line2D at 0x7f4eb4f31600>,
 <matplotlib.lines.Line2D at 0x7f4eb4dca020>,
 <matplotlib.lines.Line2D at 0x7f4eb4dc8760>,
 <matplotlib.lines.Line2D at 0x7f4eb4dc9300>,
 <matplotlib.lines.Line2D at 0x7f4eb4f33cd0>,
 <matplotlib.lines.Line2D at 0x7f4eb4f313f0>,
 <matplotlib.lines.Line2D at 0x7f4eb4f30a30>,
 <matplotlib.lines.Line2D at 0x7f4eb4f32110>,
 <matplotlib.lines.Line2D at 0x7f4eb4f33a00>,
 <matplotlib.lines.Line2D at 0x7f4eb4f33a30>,
 <matplotlib.lines.Line2D at 0x7f4eb4f33d00>,
 <matplotlib.lines.Line2D at 0x7f4eb4f313c0>,
 <matplotlib.lines.Line2D at 0x7f4eb4f33970>,
```

```
<matplotlib.lines.Line2D at 0x7f4eb4f30af0>,
<matplotlib.lines.Line2D at 0x7f4eb4f312a0>,
<matplotlib.lines.Line2D at 0x7f4eb4f311b0>,
<matplotlib.lines.Line2D at 0x7f4eb4f30c40>,
<matplotlib.lines.Line2D at 0x7f4eb4f30b20>,
<matplotlib.lines.Line2D at 0x7f4eb4f308b0>,
<matplotlib.lines.Line2D at 0x7f4eb4f32020>,
<matplotlib.lines.Line2D at 0x7f4eb4f30070>,
<matplotlib.lines.Line2D at 0x7f4eb4f31e40>,
<matplotlib.lines.Line2D at 0x7f4eb4f31ea0>,
<matplotlib.lines.Line2D at 0x7f4eb4f320e0>,
<matplotlib.lines.Line2D at 0x7f4f5cc80eb0>,
<matplotlib.lines.Line2D at 0x7f4f6f8777f0>,
<matplotlib.lines.Line2D at 0x7f4eb516ab00>,
<matplotlib.lines.Line2D at 0x7f4eb516acb0>,
<matplotlib.lines.Line2D at 0x7f4eb516aef0>,
<matplotlib.lines.Line2D at 0x7f4eb516b640>,
<matplotlib.lines.Line2D at 0x7f4eb516b9a0>,
<matplotlib.lines.Line2D at 0x7f4eb516a470>,
<matplotlib.lines.Line2D at 0x7f4eb516a4d0>,
<matplotlib.lines.Line2D at 0x7f4eb516bb50>,
<matplotlib.lines.Line2D at 0x7f4eb516aa70>,
<matplotlib.lines.Line2D at 0x7f4eb516be80>]
```



Question 2.2 - TD(0) (10 pts)

Question 2.2a (5 pts)

Implement the $\mathsf{TD}(0)$ prediction algorithm to estimate $V^{\pi}(s)$.

```
def td0(policy, env, step size=0.1, num episodes=100, discount=0.99):
    Input:
        policy (int -> int): policy to evaluate
        env (DiscreteEnv): FloorIsLava environment
        step size (float): step size alpha of td learning
        num episodes (int): number of episodes to run the algorithm
for
        discount (float): discount factor
    Returns state values trace (list of lists):
        Value estimates of each state at every episode of training.
    Do not modify state values trace. JUST UPDATE state values.
        state values keep tracks of the value of each state. Each
index of state values represents one state.
    state values = [0 for i in range(env.observation space.n)]
    state values trace = []
    for j in (range(num episodes)):
        # TO IMPLEMENT
        done = False
        obs, info = env.reset()
        while not done:
            action = policy(obs)
            new obs, reward, , done, info = env.step(action)
            if done:
                state values[obs] = state values[obs] + step size *
(reward - state values[obs])
                break
            state values[obs] = state values[obs] + step size *
(reward + discount * state values[new obs] - state values[obs])
            obs = new obs
        state values trace.append([s for s in state values])
    return state values trace
grader.check("question 2.2a")
question 2.2a results: All test cases passed!
```

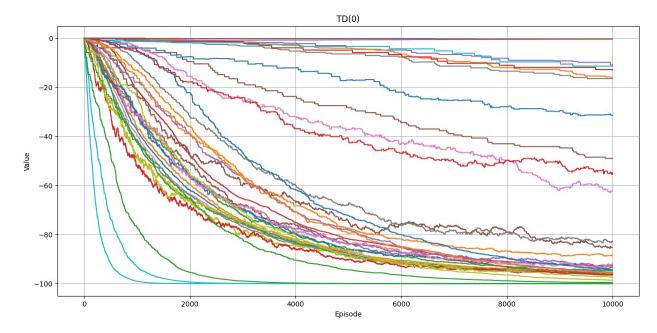
Question 2.2b - Plotting (5 pts)

Use a step size $\alpha = 0.01$. Train the algorithm for 10000 episodes as well, and plot the same figure as in the previous question ($V^{\pi}(s)$ for each s over the number of episodes).

```
env = FloorIsLava(map_name="6x6", slip_rate=0.1)
# Set seed
seed = 10
```

```
env.seed(seed)
np.random.seed(seed)
random.seed(seed)
td_state_vals = td0(random_policy, env, step_size=0.01,
num_episodes=10000)

plt.figure(figsize=(15,7))
plt.plot(td_state_vals)
plt.xlabel('Episode')
plt.ylabel('Value')
plt.title('TD(0)')
plt.grid()
```



Question 2.3 - TDN (12 pts)

Question 2.3a (5pts)

Now, implement the *n-step* TD algorithm to estimate $V^{\pi}(s)$.

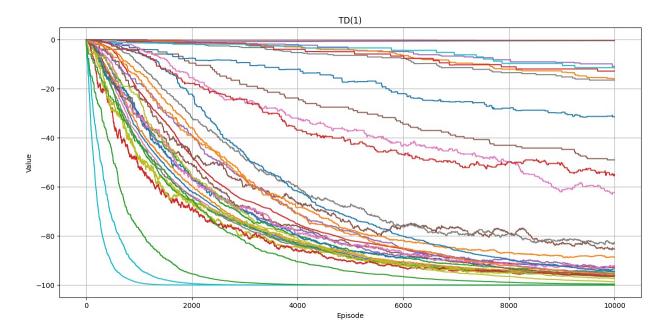
```
def tdn(policy, env, n, step_size=0.1, num_episodes=100,
discount=0.99):
    Input:
        policy (int -> int): policy to evaluate
        env (DiscreteEnv): FloorIsLava environment
        n (int): Number of steps before bootstrapping for td(n)
algorithm
        step_size (float): step size alpha of td learning
        num_episodes (int): number of episodes to run the algorithm
```

```
for
        discount (float): discount factor
    Returns state values trace (list of lists):
        Value estimates of each state at every episode of training.
    Do not modify state values trace. JUST UPDATE state values.
        state_values keep tracks of the value of each state. Each
index of state values represents one state.
    state values = [0 for i in range(env.observation space.n)]
    state values trace = []
    for j in (range(num episodes)):
        # TO IMPLEMENT
        obs, info = env.reset()
        T = float('inf')
        t = 0
        episode rewards = []
        episode states = [obs]
        episode actions = []
        while True:
            if t < T:
                action = policy(obs)
                obs, reward, _, done, info = env.step(action)
                episode actions.append(action)
                episode states.append(obs)
                episode rewards.append(reward)
                if done:
                    T = t + 1
            tau = t - n
            if tau >= 0:
                G = sum(discount**(i-tau) * episode rewards[i] for i
in range(tau, min(tau+n+1, T)))
                if tau + n+1 < T:
                    G = G + discount**(n+1) *
state values[episode states[tau+n+1]]
                state values[episode states[tau]] =
state values[episode states[tau]] + step size * (G -
state values[episode states[tau]])
            if tau == T - 1:
                break
            t = t + 1
        state values trace.append([s for s in state values])
    return state values trace
grader.check("question 2.3a")
question 2.3a results: All test cases passed!
```

Question 2.3b - Plotting (2 pts)

Use a step size of α = 0.01. This algorithm should take the additional hyper-parameter n to determine how much to bootstrap. Now set n = 0, and train the algorithm for 10000 episodes. Plot the the same figure as before ($V^{\pi}(s)$) for each s over the number of episodes)

```
env = FloorIsLava(map_name="6x6", slip_rate=0.1)
# Set seed
seed = 10
env.seed(seed)
np.random.seed(seed)
random.seed(seed)
tdn1_state_vals = tdn(random_policy, env, n=0, step_size=0.01,
num_episodes=10000)
plt.figure(figsize=(15,7))
plt.plot(tdn1_state_vals)
plt.xlabel('Episode')
plt.ylabel('Value')
plt.title('TD(1)')
plt.grid()
```



Question 2.3c (3 pts)

Compare this figure to TD (0) and Every visit Monte Carlo Prediction. Which algorithm do you expect this figure to look similar to? Does it, why or why not?

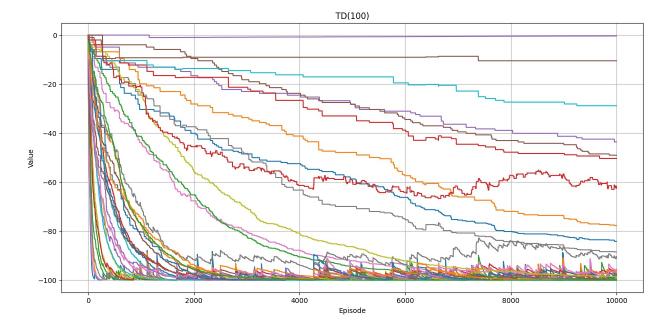
The figure for TD(1) is likely to resemble the TD(0) algorithm more closely than Every Visit Monte Carlo Prediction. This is because TD(1) is an off-policy algorithm, similar to TD(0), which updates values based on a one-step look-ahead, and both these methods can adjust quickly to changes in state values. In contrast, Every Visit Monte Carlo Prediction often requires a more extensive

exploration process and can have higher variance. However, TD(1) may not look exactly like TD(0) due to its temporal difference aspect, which may result in values that are somewhat shifted towards -100, as you expect, but not nearly as much as Every Visit Monte Carlo.

Question 2.3d - Plotting (2 pts)

Using the same implementation of *n-step* $\overline{\text{TD}}$, estimate $V^{\pi}(s)$ using n=100 instead (still with $\alpha=0.01$ and 10000 episodes). Again, plot the same figure as before ($V^{\pi}(s)$) for each s over the number of episodes).

```
env = FloorIsLava(map_name="6x6", slip_rate=0.1)
# Set seed
seed = 10
env.seed(seed)
np.random.seed(seed)
random.seed(seed)
tdn100_state_vals = tdn(random_policy, env, n=100, step_size=0.01,
num_episodes=10000)
plt.figure(figsize=(15,7))
plt.plot(tdn100_state_vals)
plt.xlabel('Episode')
plt.ylabel('Value')
plt.title('TD(100)')
plt.grid()
```



Question 2.4 - Unifying (14 pts)

The intuition is that n-step \overline{TD} should generalize both Monte Carlo prediction and \overline{TD} (0). We saw in the previous question that it does not seem to be equivalent to MC prediction. Modify

your n-step TD algorithm such that when n = 100, it becomes equivalent to Every visit Monte Carlo prediction. Hint: This has to do with the step size α .

Question 2.4a (3 pts)

Before implementing this modified TDN, identify what the new formula for α should be.

Every visit Monte Carlo:
$$V\left(S_{t}\right) = V\left(S_{t}\right) + E\left[R_{t+1} + \gamma R_{t+2} + \ldots + \gamma^{n} R_{t+n} - V\left(S_{t}\right)\right]$$

TD(n):
$$V(S_t) = V(S_t) + \alpha (R_{t+1} + \gamma R_{t+2} + ... + \gamma^n V(S_{t+n}) - V(S_t))$$

Let's define m to be the number of time the state S_t has been visited so far.

To make TD(n) act like Every visit Monte Carlo, we need to make set $n=\infty$ and set $\alpha=\frac{1}{m}$

Thus:
$$V(S_t) = V(S_t) + \frac{1}{m} * (R_{t+1} + \gamma R_{t+2} + ... + \gamma^n V(S_{t+n}) - V(S_t))$$

Question 2.4b (5 pts)

Now implement the modified_tdn method that uses this new step size. Most of this method is the same as tdn.

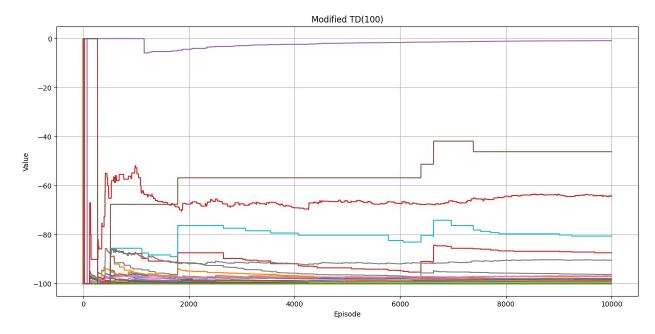
```
def modified tdn(policy, env, n, num episodes=100, discount=0.99):
    This function should largely be equivalent to the tdn function
implemented in Ouestion 3.
    The only difference is the step size will be dynamically changed
using your formula in Q5a).
    You may copy paste most lines in the previous implementation.
    Input:
        policy (int -> int): policy to evaluate
        env (DiscreteEnv): FloorIsLava environment
        n (int): Number of steps before bootstrapping for td(n)
algorithm
        step size (float): step size alpha of td learning
        num episodes (int): number of episodes to run the algorithm
for
        discount (float): discount factor
    Returns state values trace (list of lists):
        Value estimates of each state at every episode of training.
    Do not modify state values trace. JUST UPDATE state values and
state visitation.
        state values keep tracks of the value of each state. Each
index of state values represents one state.
    state values = [0 for i in range(env.observation space.n)]
```

```
state visitation = [0 for i in range(env.observation space.n)]
    state values trace = []
    for j in (range(num episodes)):
        # TO IMPLEMENT
        obs, info = env.reset()
        T = float('inf')
        t = 0
        episode rewards = []
        episode states = [obs]
        episode actions = []
        while True:
            if t < T:
                action = policy(obs)
                obs, reward, _, done, info = env.step(action)
                episode actions.append(action)
                episode states.append(obs)
                episode rewards.append(reward)
                if done:
                    T = t + 1
            tau = t - n
            if tau >= 0:
                G = sum(discount**(i-tau) * episode rewards[i] for i
in range(tau, min(tau+n+1, T)))
                if tau + n+1 < T:
                    G = G + discount**(n+1) *
state_values[episode states[tau+n+1]]
                tau state = episode states[tau]
                state visitation[tau state] =
state visitation[tau state] + 1
                state_values[tau_state] = state values[tau state] +
1/state_visitation[tau_state] * (G - state_values[tau_state])
            if tau == T - 1:
                break
            t = t + 1
        state values trace.append([s for s in state values])
    return state values trace
grader.check("question 2.4b")
question 2.4b results: All test cases passed!
```

Question 2.4c - Plotting (3 pts)

Now plot the same plot as in the previous questions with n=100, and compare it with the *Every Visit MC prediction* algorithm. You should now see that their behaviors match.

```
env = FloorIsLava(map_name="6x6", slip_rate=0.1)
# Set seed
seed = 10
env.seed(seed)
np.random.seed(seed)
random.seed(seed)
mod_tdn100_state_vals = modified_tdn(random_policy, env, n=100,
num_episodes=10000)
plt.figure(figsize=(15,7))
plt.plot(mod_tdn100_state_vals)
plt.xlabel('Episode')
plt.ylabel('Value')
plt.title('Modified TD(100)')
plt.grid()
```



Question 2.4d (3 pts)

Compare this new figure to TD(0) and Every visit Monte Carlo Prediction. Do you notice that it closely resembles the latter?

TD(100) closely resembles Every Visit Monte Carlo Prediction as expected when n is set to a large value like 100 because it approaches the behavior of averaging over all visits to the state, similar to Every Visit Monte Carlo. While TD(0) performs updates based on a single-step lookahead, TD(100) effectively performs long-term look-ahead and behaves more like Every Visit Monte Carlo in terms of convergence to expected returns.

Part 3 - Temporal Difference Control Methods (30 pts)

Continuing with the same FloorIsLava environment as before with 0 slip_rate this time, we will investigate various TD-control methods in this section. In this question you need to implement a training procedure similar to the generate_episode function in Part 0, but instead of running a fixed policy, you need to ensure that the agent is trained (i.e., value estimate is updated) throughout the learning phase.

First, carefully read and understand the code provided for a base class that will serve as the parent class for all learning agents you will implement in this section.

```
class Agent():
    def init (self):
        pass
    def agent_init(self, agent_init_info):
        """Setup for the agent called when the experiment first
starts.
        agent init info (dict), the parameters used to initialize the
agent. The dictionary contains:
            num states (int): The number of states,
            num actions (int): The number of actions,
            epsilon (float): The epsilon parameter for exploration,
            step size (float): The step-size,
            discount (float): The discount factor,
        }
        np.random.seed(agent init info['seed'])
        random.seed(agent init info['seed'])
        # Store the parameters provided in agent init info.
        self.num actions = agent init info["num actions"]
        self.num_states = agent_init_info["num_states"]
        self.epsilon = agent init info["epsilon"]
        self.step size = agent init info["step size"]
        self.discount = agent init info["discount"]
        # Create an array for action-value estimates and initialize it
to zero.
        self.q = np.zeros((self.num_states, self.num_actions))
    def get_current_policy(self):
        Returns the epsilon greedy policy of the agent following the
```

```
previous implementation of
        make eps greedy policy
        Returns:
            Policy (callable): fun(state) -> action
        return make_eps_greedy_policy(self.q, epsilon=self.epsilon)
    def agent step(self, prev_state, prev_action, prev_reward,
current_state, done):
        """ A learning step for the agent given a state, action,
reward, next state and done
        Args:
            prev_state (int): the state observation from the
enviromnents last step
            prev action (int): the action taken given prev state
            prev reward (float): The reward received for taking
prev action in prev state
            current state (int): The state received for taking
prev action in prev state
            done (bool): Indicator that the episode is done
        Returns:
            action (int): the action the agent is taking given
current state
        raise NotImplementedError
```

Question 3.1 - Helper methods (3 pts)

Implement the method train_episode, that is similar in function to the generate_episode, except it takes an agent as an argument instead of the policy, and simultaneously trains the agent while generating an episode. (Hint, make use of the agent step method of the Agent class to both get an action and train the agent.)

```
def train_episode(agent, env):
    Input:
        agent (Agent): an agent of the class Agent implemented above
        env (DiscreteEnv): The FloorIsLava environment
    Returns:
        states (list): the sequence of states in the generated episode
        actions (list): the sequence of actions in the generated

episode
    rewards (list): the sequence of rewards in the generated

episode
    """

states = []
    rewards = []
    actions = []
```

```
done = False
    current state, _ = env.reset()
    action = agent.get current policy()(current state)
    actions.append(action)
    states.append(current state)
    while not done:
        # TO IMPLEMENT
        new_state, reward, _, done, _ = env.step(action)
        action = agent.agent step(current state, action, reward,
new state, done)
        actions.append(action)
        states.append(new state)
        rewards.append(reward)
        current_state = new_state
    return states, actions, rewards
grader.check("question 3.1")
question 3.1 results: All test cases passed!
```

We then provide the code to train an agent using this newly written method.

```
def td control(agent class, epsilon, step size, run, num episodes=100,
discount=0.99):
    agent info = {
        "num_actions": 4,
        "num states": 36,
        "epsilon": epsilon,
        "step size": step size,
        "discount": discount,
        "seed": run
    agent = agent class()
    agent.agent init(agent info)
    env = FloorIsLava(map name="6x6", slip rate=0.)
    # Set seed
    seed = run
    env.seed(seed)
    np.random.seed(seed)
    random.seed(seed)
    all returns = []
    for j in (range(num episodes)):
        states, actions, rewards = train episode(agent, env)
        all returns.append(np.sum(rewards))
```

Question 3.2 - SARSA (8 pts)

Question 3.2a (5 pts)

Implement the SARSA control algorithm. Recall the update rule given s, a, r, s', a':

$$Q(s,a) \leftarrow Q(s,a) + \alpha [r + \gamma Q(s',a') - Q(s,a)]$$

And make sure to handle terminal states correctly.

```
class SarsaAgent(Agent):
    def agent step(self, prev state, prev action, prev reward,
current_state, done):
        """ A learning step for the agent given SARS
            prev_state (int): the state observation from the
environments last step
            prev action (int): the action taken given prev state
            prev reward (float): The reward received for taking
prev action in prev state
            current state (int): The state received for taking
prev action in prev state
            done (bool): Indicator that the episode is done
            action (int): the action the agent is taking given
current state
        # TO IMPLEMENT
        q s a = self.q[prev state, prev action]
        action = self.get current policy()(current_state)
        self.q[prev_state, prev_action] = q_s_a + self.step_size *
(prev reward + self.discount * (1-int(done)) * self.q[current state,
action] - q_s_a)
        # ----
        return action
grader.check("question 3.2a")
question 3.2a results: All test cases passed!
```

Question 3.2b - Evaluating (3 pts)

Let's run the SARSA algorithm on our 0 slip rate environment. We set $\epsilon = 0.5$, $\alpha = 0.1$, $\gamma = 0.99$, and run the algorithm 5 times over 10000 episodes.

```
## Running SARSA on the environment on 5 different seeds

epsilon = 0.5 #@param {allow-input: true}
step_size = 0.1 #@param {allow-input: true}
discount = 0.99 #@param
num_runs = 5 #@param {allow-input: true}
num_episodes = 10000 #@param {allow-input: true}

sarsa_returns = []
sarsa_agents = []
for t in range(num_runs):
    returns, agent = td_control(agent_class=SarsaAgent,
epsilon=epsilon, step_size=step_size, run=t,
num_episodes=num_episodes, discount=discount)
    sarsa_returns.append(returns)
    sarsa_agents.append(agent)
```

Now let's evaluate our agents with 0 exploration.

```
## Evaluating the agent with 0 exploration, i.e epsilon=0

sarsa_optimal_returns = []
for t in range(num_runs):
    env = FloorIsLava(map_name="6x6", slip_rate=0.)
    optimal_policy = make_eps_greedy_policy(sarsa_agents[t].q,
epsilon=0.)
    s, a, r = generate_episode(optimal_policy, env, render=False)
    print('Optimal return for seed {0} is {1}'.format(t, np.sum(r)))
    sarsa_optimal_returns.append(np.sum(r))

Optimal return for seed 0 is -7
Optimal return for seed 1 is -150
Optimal return for seed 3 is -150
Optimal return for seed 4 is -7
```

Question 3.3 - Q-learning (8 pts)

Question 3.3a (5 pts)

Implement the Q-learning control algorithm. Recall the update rule:

$$Q(\mathbf{s}, a) \leftarrow Q(\mathbf{s}, a) + \alpha \left[r + \gamma \max_{a'} Q(\mathbf{s'}, a') - Q(\mathbf{s}, a) \right)$$

And make sure to handle terminal states correctly

```
#@title Q-learning
```

```
class OLearningAgent(Agent):
    def agent step(self, prev state, prev action, prev reward,
current_state, done):
        """ A learning step for the agent given SARS
        Args:
            prev state (int): the state observation from the
environments last step
            prev action (int): the action taken given prev state
            prev reward (float): The reward received for taking
prev action in prev state
            current state (int): The state received for taking
prev action in prev state
            done (bool): Indicator that the episode is done
        Returns:
            action (int): the action the agent is taking given
current state
        # TO IMPLEMENT
        # -----
        q_s_a = self.q[prev_state, prev_action]
        action = self.get current policy()(current state)
        if done:
            self.q[prev state, prev action] = q s a + self.step size *
(prev reward - q s a)
        else:
            self.q[prev state, prev action] = q s a + self.step size *
(prev reward + self.discount * np.max(self.q[current state]) - q s a)
        return action
grader.check("question 3.3a")
question 3.3a results: All test cases passed!
```

Question 3.3b - Evaluating (3 pts)

Let's run the Q-learning algorithm on our 0 slip rate environment. We set ϵ = 0.5, α = 0.1, γ = 0.99, and run the algorithm 5 times over 10000 episodes.

```
## Running Q-learning on the environment on 5 different seeds

epsilon = 0.5 #@param {allow-input: true}
step_size = 0.1 #@param {allow-input: true}
discount = 0.99 #@param
num_runs = 5 #@param {allow-input: true}
num_episodes = 10000 #@param {allow-input: true}

q_returns = []
q_agents = []
```

```
for t in range(num_runs):
    returns, agent = td_control(agent_class=QLearningAgent,
epsilon=epsilon, step_size=step_size, run=t,
num_episodes=num_episodes, discount=discount)
    q_returns.append(returns)
    q_agents.append(agent)
```

Again, we evaluate the agent with 0 exploration

```
## Evaluating the agent with 0 exploration, i.e epsilon=0

q_optimal_returns = []
for t in range(num_runs):
    env = FloorIsLava(map_name="6x6", slip_rate=0.)
    optimal_policy = make_eps_greedy_policy(q_agents[t].q, epsilon=0.)
    s, a, r = generate_episode(optimal_policy, env, render=False)
    print('Optimal return for seed {0} is {1}'.format(t, np.sum(r)))
    q_optimal_returns.append(np.sum(r))

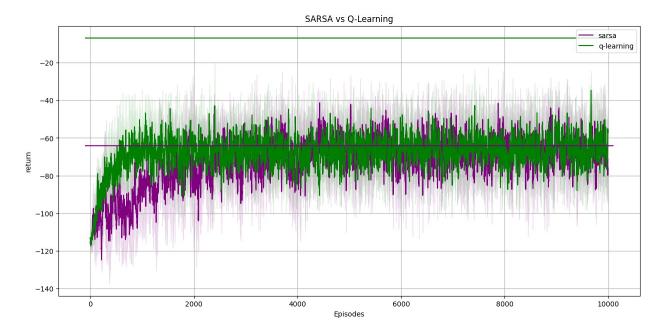
Optimal return for seed 0 is -7
Optimal return for seed 1 is -7
Optimal return for seed 3 is -7
Optimal return for seed 4 is -7
```

Question 3.4 - Plotting everything (5 pts)

Now let us plot the learning curves of our algorithms, and their final optimal returns given a deterministic policy.

```
def moving avg(stuff, window):
    return np.convolve(stuff, np.ones(window)/window, mode='valid')
plt.figure(figsize=(15,7))
plot_many([moving_avg(r, 10) for r in sarsa_returns], label='sarsa',
color='purple')
plot many([moving avg(r, 10) for r in q returns], label='q-learning',
color='green')
# plot_many([moving_avg(r, 10) for r in esarsa_returns],
label='expected sarsa', color='orange')
plt.hlines([np.mean(q_optimal_returns)], -100, 10100, color='green')
plt.hlines([np.mean(sarsa optimal returns)], -100, 10100,
color='purple')
# plt.hlines([np.mean(esarsa optimal returns)], -100, 10100,
color='orange')
plt.legend()
plt.grid()
plt.xlabel('Episodes')
plt.vlabel('return')
plt.title('SARSA vs Q-Learning')
```

Text(0.5, 1.0, 'SARSA vs Q-Learning')



Question 3.5 - Analysis (6 pts)

Question 3.5a (3 pts)

Out of the two algorithms, which one prefers safer and more conservative (or cautious) policies in the learning phase? Which prefers aggressive policies?

SARSA tends to prefer safer and more conservative policies during the learning phase. This is because SARSA follows an on-policy approach, where it learns the value of state-action pairs while following the same policy it's trying to improve. Since SARSA updates values based on its current policy, it typically avoids taking unnecessary risks during learning.

On the other hand, Q-learning prefers more aggressive policies during learning. This often leads to Q-learning exploring and learning policies that are more willing to take risks and aim for higher rewards, even if those actions might be riskier.

Quesiton 3.5b (3 pts)

Despite the learning curve of *Q-learning* being similar to that of SARSA, why does it seem to have a better return during evaluation?

Q-learning appears to have a better return during evaluation compared to SARSA, despite similar learning curves, due to its off-policy nature. Q-learning updates Q-values by assuming it follows the optimal policy, even if it's not, which makes it more explorative and likely to discover better actions in the long run.

SARSA, on the other hand, follows the current policy during learning, and this can lead to more conservative estimates of Q-values. It tends to take into account the exploration strategy it's following, which can be less aggressive compared to Q-learning's approach.

Part 4 -- Deep Q-learning (20 points)

Question 4.1 - DQN

In the previous sections, you've been storing Q-values for each state in a lookup table. This becomes quite difficult when learning in environments with large or even infinite state spaces. To address this problem, we'll study Deep Q-Learning (DQN), an algorithm that combines some of the principles you've learned earlier in the assignment with function approximation from neural networks.

Question 4.1a (15 points)

Implement the get_action and compute_targets for the DQNAgent class below.

For get_action, you need to write an epsilon greedy policy that selects a random action with probability epsilon, and selects the action with the highest Q-value according to the agent with probability (1-epsilon).

For compute_targets, you need to compute the 1-step targets for all the transitions given using the agent's target network. The target should be computed as:

$$max_{a' \in A}r + \gamma Q_{taraet}(s', a')$$

if s' is not a terminal state, and r if it is a terminal state.

```
class ReplayBuffer:
    """This class implements a replay buffer for experience replay.
You do not need to
    implement anything here."""
    def __init__(self, buffer_size, observation_space, action_space):
        self.buffer size = buffer size
        self.observations = np.zeros(
            (buffer size,) + observation space.shape,
dtype=observation space.dtype
        self.next observations = np.zeros(
            (buffer size,) + observation space.shape,
dtype=observation space.dtype
        self.actions = np.zeros(
            (buffer size,) + action space.shape,
dtype=action space.dtype
        self.rewards = np.zeros((buffer size,), dtype=np.float32)
        self.terminated = np.zeros((buffer size,), dtype=np.uint8)
        self.position = 0
        self.num added = 0
    def add(self, observation, action, reward, next observation,
```

```
terminated):
        Adds a new experience tuple to the replay buffer.
        Parameters:
            - observation (np.ndarray): The current observation.
            - action (int): The action taken.
            - reward (float): The reward received.
            - next observation (np.ndarray): The next observation.
            - terminated (bool): Whether the episode terminated after
this experience.
        Returns:
            - None
        self.observations[self.position] = observation
        self.next observations[self.position] = next observation
        self.actions[self.position] = action
        self.rewards[self.position] = reward
        self.terminated[self.position] = terminated
        self.position = (self.position + 1) % self.buffer size
        self.num added += 1
    def sample(self, batch size):
        Samples a batch of experiences from the replay buffer.
        Parameters:
            - batch size (int): The number of experiences to sample.
        Returns:
            - observations (np.ndarray): The current observations.
Shape (batch size,
              observation dim)
            - actions (np.ndarray): The actions taken. Shape
(batch_size, action_dim)
            - rewards (np.ndarray): The rewards received. Shape
(batch size,)

    next observations (np.ndarray): The next observations.

Shape (batch_size,
              observation dim)
            - terminated (np.ndarray): Whether the episode terminated
after this
              experience.
        0.00
        buffer size = min(self.num added, self.buffer size)
        indices = np.random.randint(0, buffer size, size=batch size)
        return (
            self.observations[indices],
            self.actions[indices].
```

```
self.rewards[indices],
            self.next_observations[indices],
            self.terminated[indices],
        )
class DQNAgent:
    def init (
        self,
        observation_space,
        action space,
        epsilon,
        learning starts at,
        learning frequency,
        learning rate,
        discount factor,
        buffer_size,
        target update frequency,
        batch size,
    ):
        self.observation space = observation space
        self.action space = action space
        self.network = self.build network(observation space,
action_space)
        self.target network =
copy.deepcopy(self.network).requires grad (False)
        self.replay buffer = ReplayBuffer(
            buffer size=buffer size,
            observation space=observation space,
            action space=action space,
        self.epsilon = epsilon
        self.learning starts at = learning starts at
        self.learning frequency = learning frequency
        self.discount factor = discount factor
        self.optimizer = torch.optim.Adam(self.network.parameters(),
lr=learning rate)
        self.loss fn = torch.nn.MSELoss()
        self.target update frequency = target update frequency
        self.batch size = batch size
    def build network(self, observation space, action space):
        Builds a neural network that maps observations to Q-values for
each action.
        input dimension = observation space.shape[0]
        output dimension = action space.n
        return torch.nn.Sequential(
```

```
torch.nn.Linear(input dimension, 256),
            torch.nn.ReLU(),
            torch.nn.Linear(256, 256),
            torch.nn.ReLU(),
            torch.nn.Linear(256, output dimension),
        )
    def get action(self, state):
        """\overline{I}mplements epsilon greedy policy. With probability epsilon,
take a random
        action. Otherwise, take the action that has the highest O-
value for the
        current state. For sampling a random action from the action
space, take a look
        at the API for spaces:
https://gymnasium.farama.org/api/spaces/#the-base-class.
        Do not hardcode the number of actions you are sampling from.
        Parameters:
            - state (np.ndarray): The current state.
        Returns:
            - action (int): The action to take.
        # TO IMPLEMENT
        # -----
        if np.random.random() < epsilon:</pre>
            return self.action space.sample()
        state = torch.from numpy(state)
        values = self.network(state)
        return torch.argmax(values).item()
    def update(self, experience, step):
        Adds the experience to the replay buffer and performs a
training step.
        Parameters:
            - experience (dict): A dictionary containing the keys
"observation"
              "action", "reward", "next observation", "terminated",
and "truncated".
        self.replay buffer.add(
            experience["observation"],
            experience["action"],
            experience["reward"],
```

```
experience["next observation"],
            experience["terminated"],
        )
        metrics = \{\}
        if step > self.learning starts at and step %
self.learning frequency == 0:
            metrics = self.perform training step()
        if step % self.target update frequency == 0:
self.target network.load state dict(self.network.state dict())
        return metrics
    def perform training step(self):
            observations,
            actions,
            rewards,
            next observations,
            terminated,
        ) = self.replay buffer.sample(self.batch size)
        observations = torch.Tensor(observations)
        actions = torch.Tensor(actions).long()
        rewards = torch.Tensor(rewards)
        next observations = torch.Tensor(next observations)
        terminated = torch.Tensor(terminated)
        q values = self.network(observations).gather(1,
actions.unsqueeze(1)).squeeze()
        with torch.no grad():
            targets = self.compute targets(rewards, next observations,
terminated)
        loss = self.loss fn(q values, targets)
        self.optimizer.zero_grad()
        loss.backward()
        self.optimizer.step()
        return {
            "loss": loss.item(),
            "q values": q values.mean().detach().numpy()
        }
    def compute_targets(self, rewards, next_observations, terminated):
        Computes the target Q-values for a batch of transitions. Make
sure to use the
        target network for this computation. If the episode
terminated, the target
        Q-value should be the reward, otherwise the reward plus the
discounted
        maximum target Q-value for the next state.
```

```
In order to do this efficiently, you should not use a for loop
or any if
        statements, but instead use tensor operations and the fact
that (1 - terminated)
        will be 0 for all the terminal transitions.
        Parameters:
            - rewards (torch.Tensor): The rewards received for each
transition in the
                batch. Shape (batch size,)
            - next observations (torch.Tensor): The next observations
for each
                transition in the batch. Shape (batch size,
observation dim)
            - terminated (torch.Tensor): Whether the episode
terminated after each
                transition in the batch. Shape (batch size,)
        Returns:
            - targets (torch.Tensor): The targets for each transition
in the batch.
                Shape (batch size,)
        0.000
        # TO IMPLEMENT
        # -----
        q values = self.target network(next observations)
        return rewards + self.discount factor * q values.max(dim=1)[0]
* (1 - terminated)
grader.check("question 4.1a")
question 4.1a results: All test cases passed!
```

Question 4.1b (5 points) - Evaluating and Plotting

Run your DQN agent below on the classic Cartpole environment. The goal in this environment is to balance a pole on top of a cart. The input space is a 4-dimensional state representing the position and velocity of the cart and the pole angle. Since this is a continuous environment, we cannot do simple tabular Q-learning, and need to use function approximation (in this case with neural networks). Your agent should be able to get the maximum return (500) over the course of training. It is ok if it periodically diverges. Run the agent, and generate the plots in the next cell. Include these plots in your PDF report.

```
env = gym.make("CartPole-v1")
agent = DQNAgent(
   observation_space=env.observation_space,
   action_space=env.action_space,
   epsilon=.1,
```

```
learning starts at=500,
    learning frequency=10,
    learning rate=.001,
    discount factor=0.99,
    buffer size=1000,
    target_update_frequency=100,
    batch size=128,
)
NUM STEPS = 100000
LOG FREQUENCY = 2000
episode rewards = []
losses = []
q vals = []
episode reward = 0
state, _ = env.reset()
for step in range(NUM STEPS):
    action = agent.get action(state)
    next_state, reward, terminated, truncated, _ = env.step(action)
    episode reward += reward
    metrics = agent.update(
        {
            "observation": state,
            "action": action,
            "reward": reward,
            "next observation": next_state,
            "terminated": terminated,
            "truncated": truncated,
        },
        step,
    state = next state
    if terminated or truncated:
        episode rewards.append(episode reward)
        episode reward = 0
        episode_length = 0
        state, _ = env.reset()
    if step % L\overline{O}G FREQUENCY == 0:
        if 'loss' in metrics:
            losses.append(metrics["loss"])
            q vals.append(metrics["q values"])
        print(
            "Step: {0}, Average Return: {1:.2f}".format(
                step, np.mean(episode rewards[-10:]))
Step: 0, Average Return: nan
```

```
Step: 2000, Average Return: 38.00
Step: 4000, Average Return: 89.70
Step: 6000, Average Return: 146.50
Step: 8000, Average Return: 93.90
Step: 10000, Average Return: 124.20
Step: 12000, Average Return: 154.60
Step: 14000, Average Return: 157.90
Step: 16000, Average Return: 132.70
Step: 18000, Average Return: 157.50
Step: 20000, Average Return: 172.70
Step: 22000, Average Return: 176.90
Step: 24000, Average Return: 55.70
Step: 26000, Average Return: 130.30
Step: 28000, Average Return: 135.30
Step: 30000, Average Return: 219.30
Step: 32000, Average Return: 124.20
Step: 34000, Average Return: 122.00
Step: 36000, Average Return: 97.80
Step: 38000, Average Return: 129.70
Step: 40000, Average Return: 158.60
Step: 42000, Average Return: 167.40
Step: 44000, Average Return: 144.50
Step: 46000, Average Return: 129.70
Step: 48000, Average Return: 85.10
Step: 50000, Average Return: 155.90
Step: 52000, Average Return: 190.30
Step: 54000, Average Return: 169.10
Step: 56000, Average Return: 144.80
Step: 58000, Average Return: 132.80
Step: 60000, Average Return: 109.90
Step: 62000, Average Return: 168.70
Step: 64000, Average Return: 90.50
Step: 66000, Average Return: 80.00
Step: 68000, Average Return: 80.70
Step: 70000, Average Return: 89.10
Step: 72000, Average Return: 100.00
Step: 74000, Average Return: 109.60
Step: 76000, Average Return: 80.00
Step: 78000, Average Return: 50.60
Step: 80000, Average Return: 64.60
Step: 82000, Average Return: 90.60
Step: 84000, Average Return: 135.80
Step: 86000, Average Return: 86.60
Step: 88000, Average Return: 65.00
Step: 90000, Average Return: 91.00
Step: 92000, Average Return: 94.50
Step: 94000, Average Return: 62.40
Step: 96000, Average Return: 48.20
Step: 98000, Average Return: 54.10
```

```
def smooth(array, n running average=10):
    return np.convolve(np.array(array),
np.ones(n running average)/n running average, mode="full")[:-
(n running average-1)]
plt.figure(figsize=(6, 9))
plt.subplot(3, 1, 1)
plt.plot(smooth(episode rewards))
plt.ylabel("Episode Returns")
plt.xlabel("Episode")
plt.subplot(3, 1, 2)
plt.plot((np.arange(len(losses)) + 1) * LOG_FREQUENCY, smooth(losses))
plt.ylabel("Loss")
plt.xlabel("Steps")
plt.subplot(3, 1, 3)
plt.plot((np.arange(len(q_vals)) + 1) * LOG_FREQUENCY, smooth(q_vals))
plt.ylabel("Q-Values")
plt.xlabel("Steps")
plt.show()
```

