



THE CHINESE UNIVERSITY OF HONG KONG, SHENZHEN

PHY 1002

PHYSICS LABORATORY

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## Short Report: Rotational Inertia

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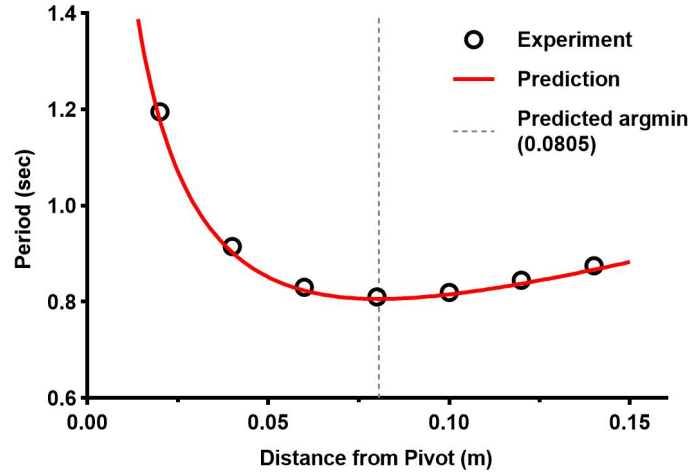
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# 1 Rectangular Bar Pendulum: Minimum Period

## 1.1 $x - T$ Plot



**Figure 1:** Relationship of pivot-CM distance  $x$  and period of the pendulum  $T$

## 1.2 Minimum Period

The following table records  $x_0$  ( $x$  that gives the minimum period) and  $T_{\min}$ , obtained both from the experiment and theory. The percentage differences of the experimental values from predictions are calculated for comparison.

	Experiment	Prediction	Relative Difference
$x_0$ (cm)	8.00	8.05	$-0.62\%$
$T_{\min}$ (s)	0.810	0.807	$+0.37\%$

**Table 1:** Values of  $x_0$  and corresponding minimum period  $T_{\min}$

The experimental values fit well with our theory.

## 2 Rotational Inertia of a Disk

### 2.1 Raw Data

$$T = 0.494 \pm 0.001 \text{ s}$$

$$M = 89.37 \pm 0.02 \text{ g}$$

$$d = R = 4.0 \pm 0.1 \text{ cm}$$

$$g = 9.78 \pm 0.01 \text{ N} \cdot \text{kg}^{-1}$$

### 2.2 Rotational Inertia about CM

The experimental value of rotational inertia about CM is given by

$$I_{\text{exp}} = \frac{T^2 M g d}{4\pi^2} - M d^2 = (7.31 \pm 0.20) \times 10^{-5} \text{ kg} \cdot \text{m}^2$$

and the theoretical value given by

$$I_{\text{theo}} = \frac{1}{2} M R^2 = (7.15 \pm 0.36) \times 10^{-5} \text{ kg} \cdot \text{m}^2$$

with a relative difference of

$$\frac{I_{\text{exp}} - I_{\text{theo}}}{I_{\text{theo}}} = 2.24 \%$$

## 3 Rotational Inertia of an Irregular Pendulum

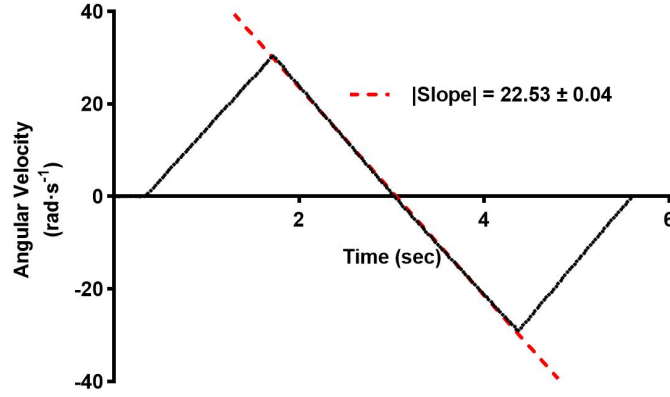
### 3.1 Raw Data

$$M = 10.07 \pm 0.02 \text{ g}$$

$$r = 1.4 \pm 0.1 \text{ cm}$$

$$g = 9.78 \pm 0.01 \text{ N} \cdot \text{kg}^{-1}$$

### 3.2 $t - \omega$ Plot and $I_{\text{CM}}$ of the Irregular Pendulum



**Figure 2:** Relationship of angular velocity  $\omega$  and time  $t$

A linear regression of the  $t - \omega$  curve during one period of acceleration yields

$$\alpha = |\dot{\omega}| = 22.53 \pm 0.04 \text{ rad} \cdot \text{s}^{-2}$$

The rotational inertia of the irregular pendulum about its CM can be found, via

$$I_{\text{CM}} = Mr\left(\frac{g}{\alpha} - r\right) = (5.92 \pm 0.41) \times 10^{-5} \text{ kg} \cdot \text{m}^2$$