



University of Applied Sciences

HOCHSCHULE  
EMDEN·LEER

# Mobile Robotics

Prof. Dr.-Ing. Gavin Kane

# Sensors and Sensor Models

## Lecture Content

- Sensor Types
- Sensor Models
- Beam-based Sensors
- Scan-Based Sensors
- Image Based Sensors

# Sensors and Sensor Models

## What?

- Proprioceptive Sensors
  - measure signals internal to the system (robot),
    - e.g. Motor Speed, Battery, Wheel Load
- Exteroceptive Sensors
  - Information about the Robots Environment
  - Distance to Object, orientation of an object, status of object

## Exteroceptive Sensors - How?

- Passive Sensors
  - Touch Sensors (Tactile)
  - Camera
- Active Sensors
  - Laser Range Finder
  - Ultrasound
  - Time-of-Flight Camera
  - Structured Light

# Sensors and Sensor Models

## Touch Sensors

- Simple, Cheap, Reliable
- One Bit of Information per sensor
- Used to activate programmed reaction

## Tactile Sensors

- Complex and Expensive Sensors
- Can offer information such as:
  - Direction of Contact,
  - Force of Contact,
  - Size of Contact, and more
- Can be used for complex manipulation tasks, Reactive Grasping

# Sensors and Sensor Models

## Touch Sensors

- Simple, Cheap, Reliable
- One Bit of Information per sensor
- Used to activate programmed reaction



©iRobot 880

## Tactile Sensors

- Complex and Expensive Sensors
- Can offer information such as:
  - Direction of Contact,
  - Force of Contact,
  - Size of Contact, and more
- Can be used for complex manipulation tasks, Reactive Grasping



FHS-o8-o6 - Forschungszentrum  
Karlsruhe

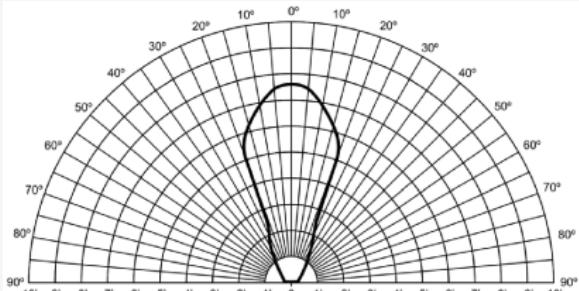
# Sensors and Sensor Models

## Ultrasound Sensors

- Emit an ultrasound signal
- Receive echo
- Time between transmission and response gives information of distance



PING))) Ultrasonic Distance Sensor

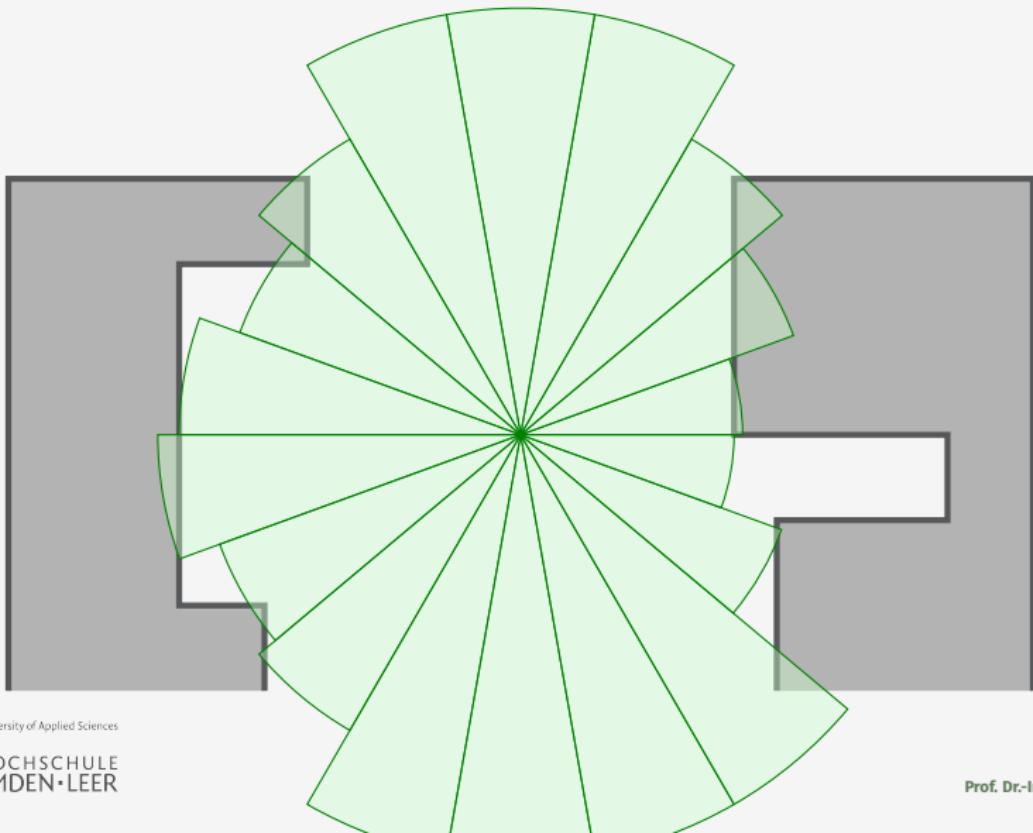


Ping))) Beam Profile

- Ultrasound "Beam" can be quite wide  $> 20$  deg
- Small Objects may not reflect enough signal
- Soft Objects may absorb sound waves
- Angled Objects may not reflect signal back enough (Specular Reflection)
- Multiple Sensors can have cross

# Sensors and Sensor Models

## Typical Ultrasonic Scan of a corridor



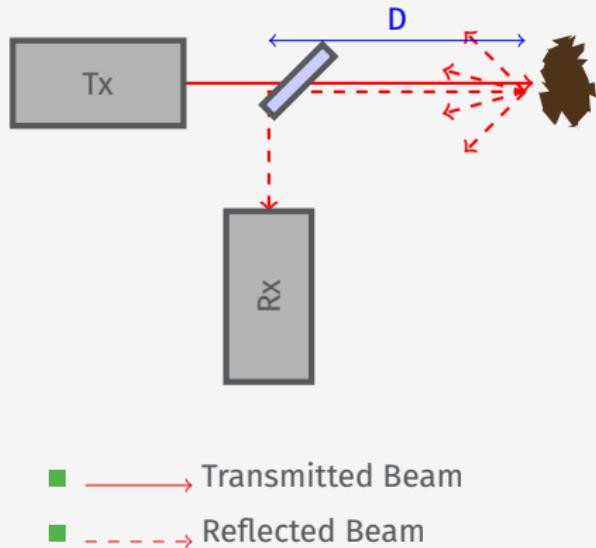
## Scan Operation

- Given a 20 degrees opening angle, 18 sensors are needed to cover the whole 360 degrees area around the robot.
- Assume the maximum range we are interested in be 10m.
- The time of flight then is  $2 \cdot \frac{10m}{330m/s} = 0.06s$
- A complete scan requires 1.08 s
- To allow frequent updates (necessary for high speed) the sensors have to be fired in parallel.
- This increases the risk of crosstalk

# Sensors and Sensor Models

## Laser Scanner

- Laser light instead of sound is used
- Transmitted and received beams are coaxial
- Receiver performs time-of-flight measurement:
  - Pulsed Laser
    - measurement of elapsed time directly
    - resolving picoseconds
    - current industry standard
  - Phase Shift Measurement
- Can perform 2D or 3D scans



# Sensors and Sensor Models

## 3D Laser Scanner Example

- Valedyne HDL-64E scans 2.2 Million Points per second
- 0.08 deg angular resolution
- < 2cm Accuracy
- 120m Range
- 64 Parallel Channels



Images Courtesy of Valedyne

# Sensors and Sensor Models

## Time of Flight Camera

- Operates with similar principle to phase measurement Lidar
- Uses a modulated infrared LED to produce a collimated light source
- every pixel of the Photonic Mixer Device (PMD) simultaneously records depth and light intensity



Image Courtesy of Odos imaging

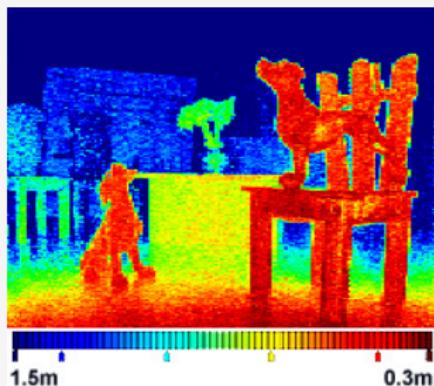


Image Courtesy of Shizuoka

# Sensors and Sensor Models

## Radar Sensor

- Gaining popularity in Autonomous Car Domain, already used in Adaptive Cruise Control
- Uses Radar at high frequency 76 - 77GHz
- Detection Range: 0.36m to 160m
- Varying Angle from  $> 40^\circ$  to  $< 15^\circ$

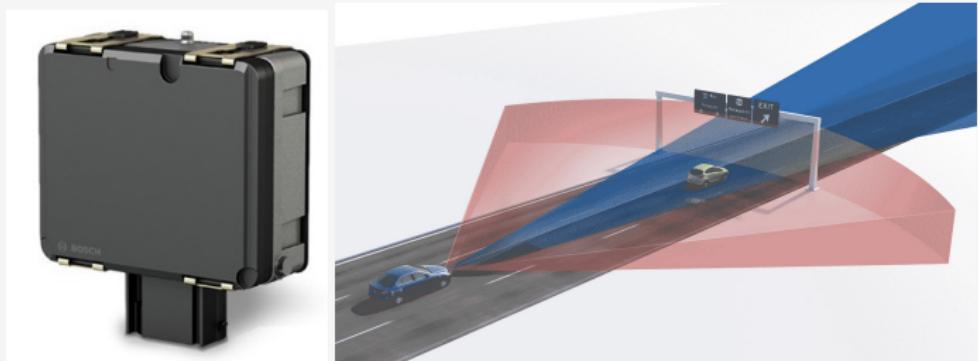


Image Courtesy of Bosch

# Sensors and Sensor Models

## Distance from Structured Light

- In order to obtain a 3D image with Structured Light, a series of musters is projected onto the target area.
- A normal Camera, specifically at a different angle to the projector, takes images of the object
- The distortion of the projected light, can be used to calculate the geometry of the projected object.



Image Courtesy of Automatic Modelling and Video Mapping Blogspot

# Sensors and Sensor Models

## Kinect I

- Kinect Projects a speckled pattern in Infrared into the scene.
- This image is detected by the infrared Camera.
- Each Speckle is surrounded by a unique pattern, allowing the projection to be mapped



Image Courtesy Microsoft

# Sensors and Sensor Models

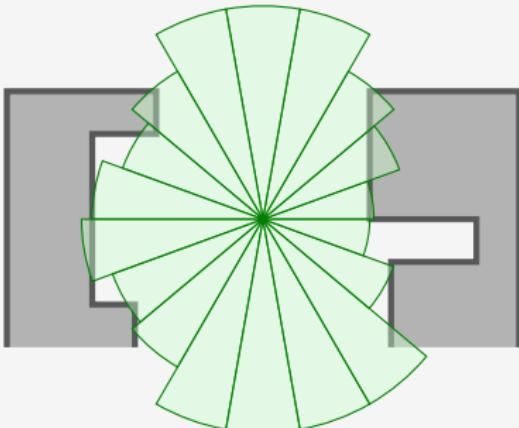
## The Challenges in Mobile Robotics Sensing

- Mobile Robot has to perceive, analyse and interpret the state of its environment.
- Measurements in a real world are dynamically changing and prone to error
- Examples:
  - Moving Items
  - Changing Illumination
  - Unknown surface properties, such as reflectivity of items
- Cross Sensitivity of Robot Sensor to Robot Pose and Robot Environment Dynamics
  - very difficult to model, appear as random errors

# Sensors and Sensor Models

## Proximity Sensors

- The central task is to determine  $P(z|x)$ , and later  $P(x|z)$
- i.e. The Probability of a Measurement "z", given the robot is at location "x"
- Question: Where do the probabilities come from?



# Sensors and Sensor Models

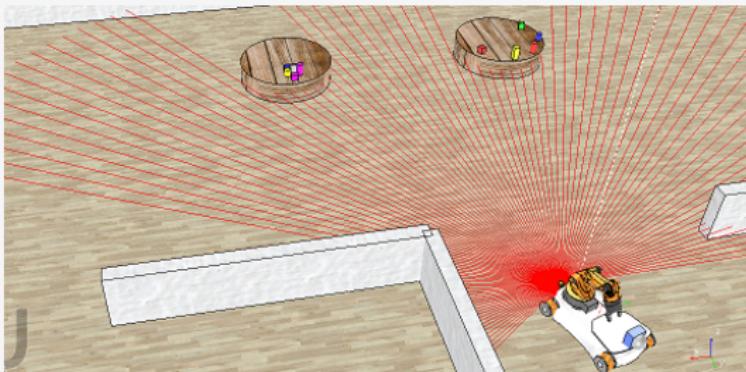
## Beam based Sensor Model

- Scan z consists of K Measurements.

$$z = z_1, z_2, z_3, \dots, z_K \quad (1)$$

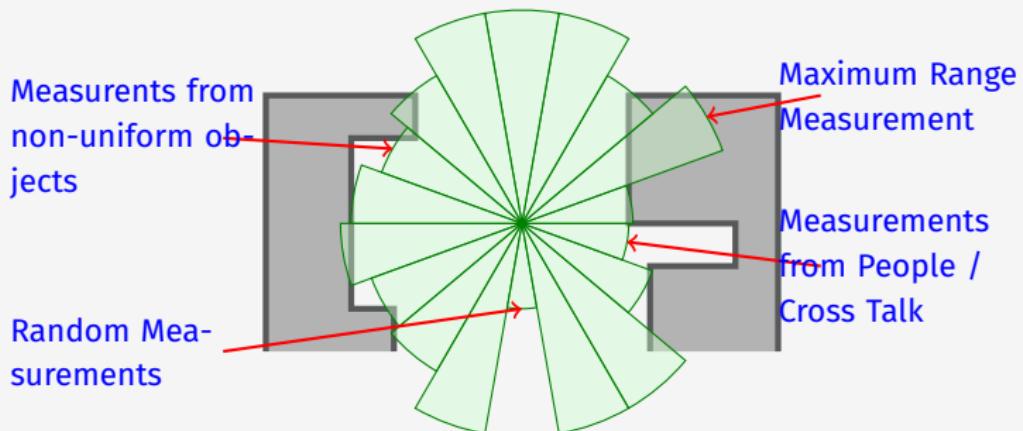
- Individual measurements are independent given the robot position.

$$P(z|x, m) = \prod_{k=1}^K P(z_k|x, m) \quad (2)$$



# Sensors and Sensor Models

## Typical Measurement Errors in Beam Measurements



# Sensors and Sensor Models

Measurements can be caused by:

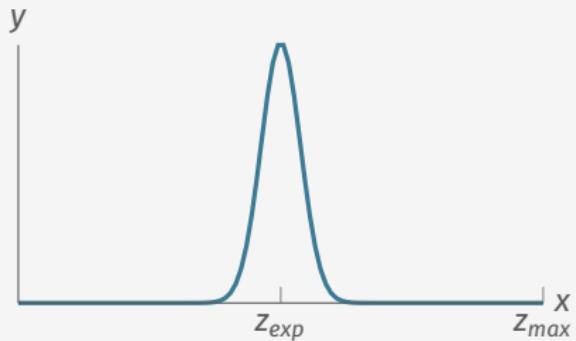
- a known object
- cross-talk
- an unexpected object
  - Furniture
  - Person
  - Part of Robot
  - Other Robot
- missing all objects
  - total reflection (at angle), e.g.  
Glass
  - total absorption

Noise is due to uncertainty:

- in measuring distance to known object
- in position of known object
- in position of additional objects
- in orientation of known object
- whether object is missed

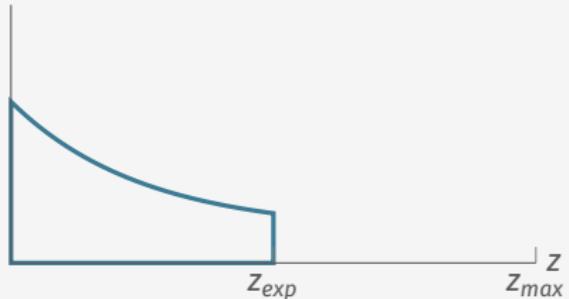
# Beam Based Proximity Model

## Measurement Noise



$$P_{hit}(z|x, m) = \eta \frac{1}{\sqrt{2\pi}b} e^{-\frac{1}{2} \frac{(z-z_{exp})^2}{b}} \quad (3)$$

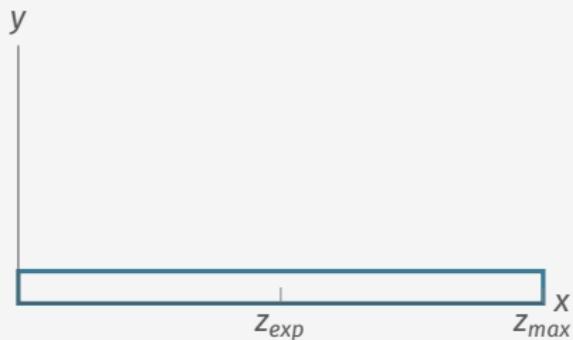
## Unexpected Obstacles



$$P_{unexp}(z|x, m) = \begin{cases} \eta \lambda e^{-\lambda z} & z < z_{exp} \\ 0 & \text{otherwise} \end{cases} \quad (4)$$

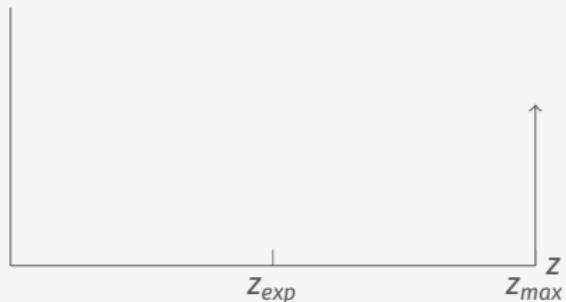
# Beam Based Proximity Model

## Random Measurement



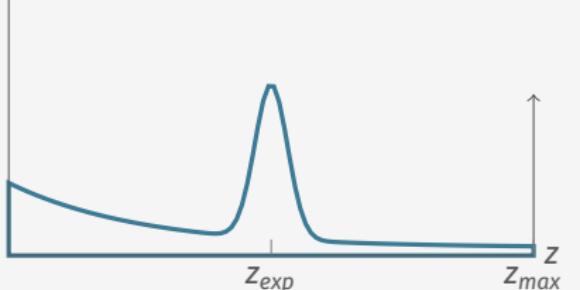
$$P_{rand}(z|x, m) = \eta \frac{1}{z_{max}} \quad z < z_{max} \quad (5)$$

## Maximum Range



$$P_{max}(z|x, m) = \delta(z - z_{max}) \quad (6)$$

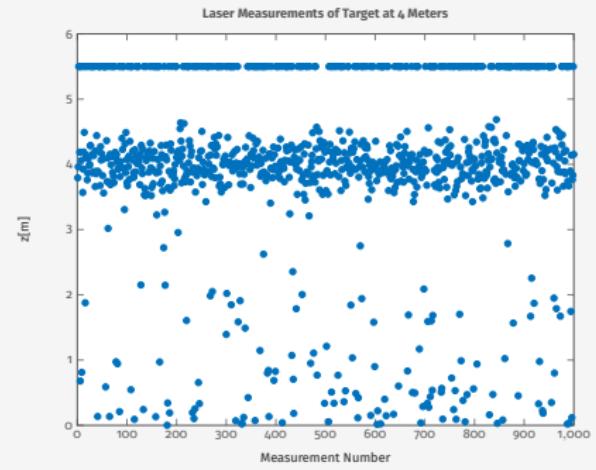
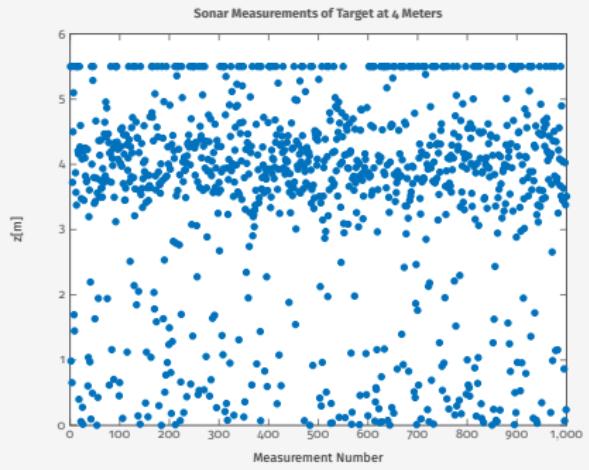
# Sensors and Sensor Models



$$P(z|x, m) = \begin{bmatrix} \alpha_{hit} \\ \alpha_{unexp} \\ \alpha_{max} \\ \alpha_{rand} \end{bmatrix}^T \cdot \begin{bmatrix} P_{hit}(z|x, m) \\ P_{unexp}(z|x, m) \\ P_{max}(z|x, m) \\ P_{rand}(z|x, m) \end{bmatrix} \quad (7)$$

How can the model parameters be determined?

# Sensors and Sensor Models



## Model Approximation

- Maximise Log Likelihood of the data

$$P(z|z_{exp})$$

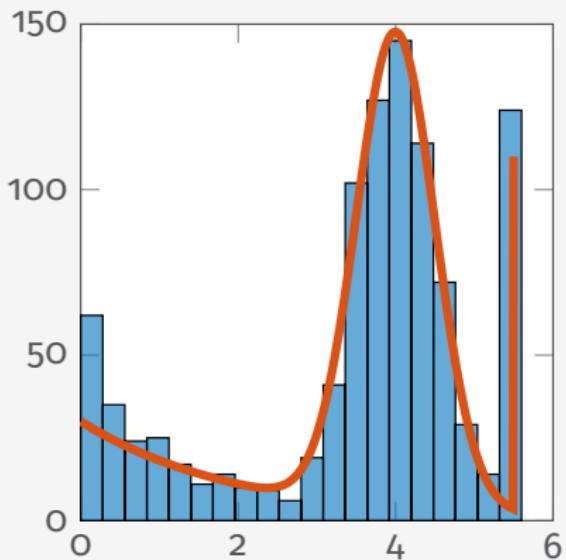
- Search space of n-1 parameters

- Hill climbing
- Gradient Descent
- Genetic Algorithms
- ...

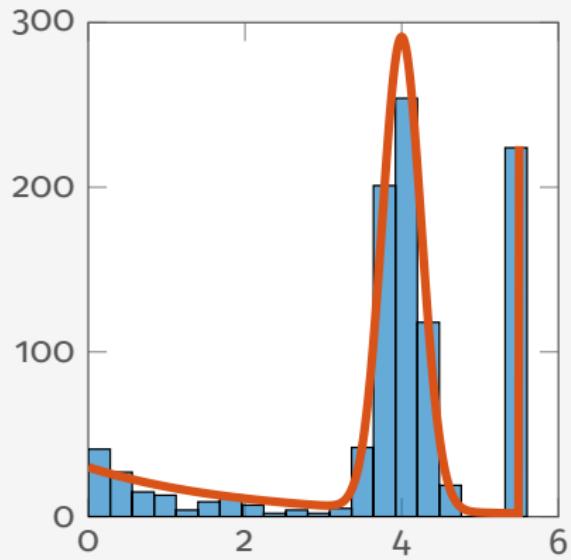
- Deterministically compute the n-th parameter to satisfy normalisation constraint

# Approximation Results

Sonar Measurements



Laser Measurements



# Sensors and Sensor Models

Scan in Building

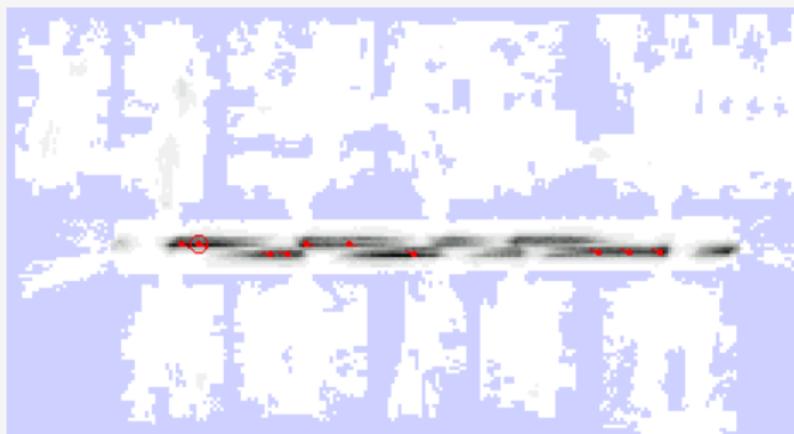
$z$



Source: Uni Freiburg, Wolfram

Likelihood of Measurement

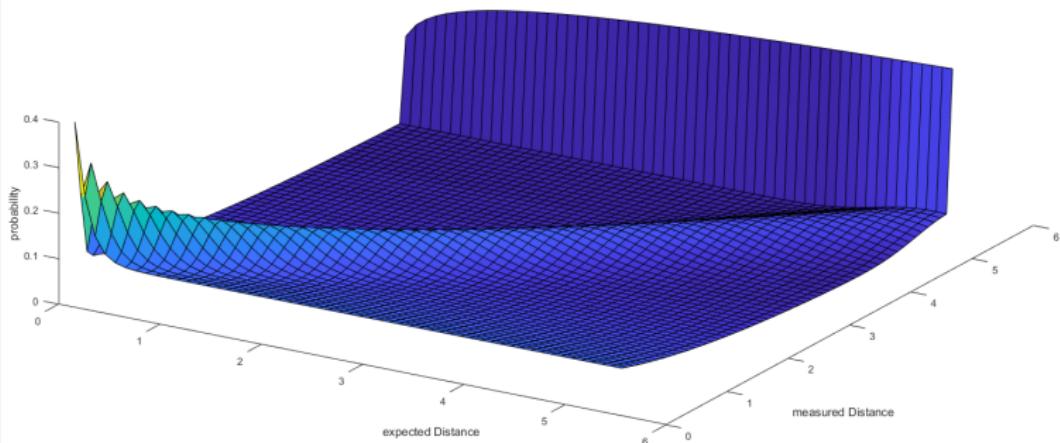
$P(z|x, m)$



Source: Uni Freiburg, Wolfram

# Sensors and Sensor Models

## Distribution as function of expected distance



Also as function of angle of incidence.

## Summary Beam-based Model

- Assumes independence between beams.
- Mathematical model for different causes for measurement errors
- Assumes no correlation between different causes
- Parameters can be learned from real data.
- Model should be learned for different distances and angles of incidence
- Determine expected distances by ray-tracing.
- Expected distances can be pre-processed for a given map
- Beam Model is not smooth for small obstacles or edges
- Beam Model is not very efficient

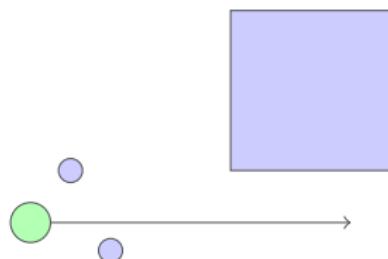
## Scan Based Model

- Scan Based Model calculates a probability based on a mixture of:
  - a Gaussian distribution with mean at distance to closest obstacle,
  - a uniform distribution for random measurements, and
  - a small uniform distribution for max range measurements.
  - Again, independence between different components is assumed.

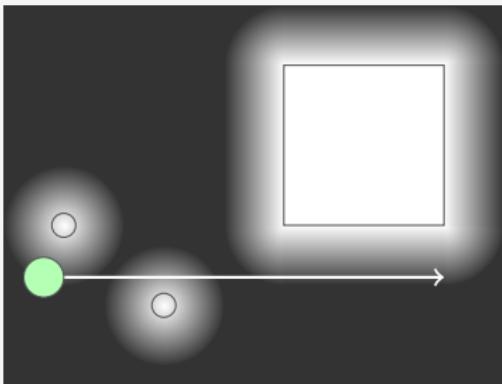
# Sensors and Sensor Models

Map

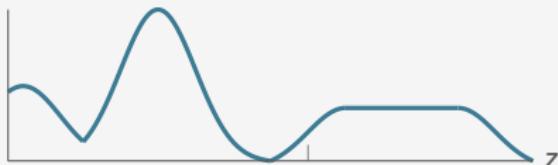
$m$



Likelihood Field



$$P(z|x, m)$$



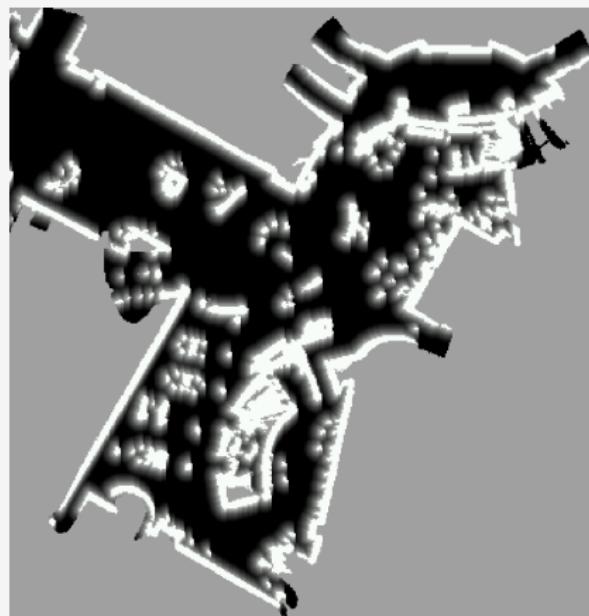
# Sensors and Sensor Models

Occupancy Map



Source: Uni Freiberg, Wolfram

Likelihood Map

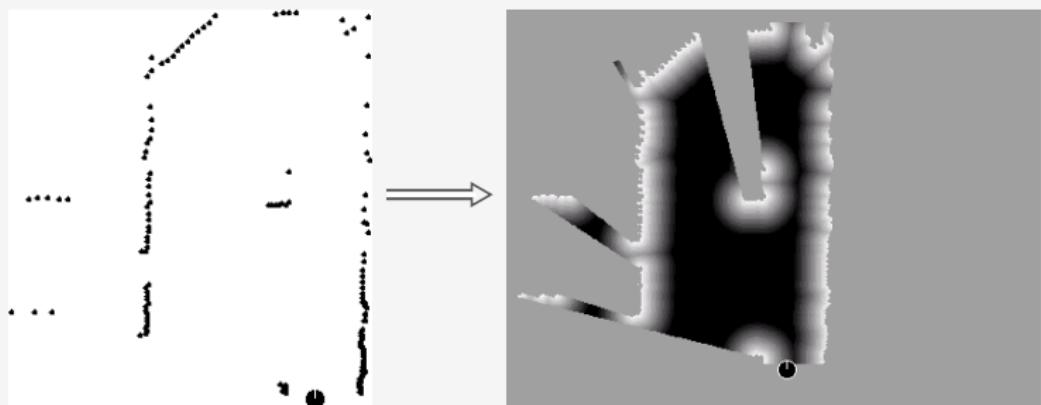


Source: Uni Freiberg, Wolfram

# Sensors and Sensor Models

## Scan Matching

- Extract Likelihood Map from Scan and use it to match additional scans



## Properties of Scan Models

- Highly Efficient, using 2D Tables only
- Smooth w.r.t. to small changes in robot position.
- Allows gradient descent, scan matching.
- Ignores physical properties of beams.
- Will it work for ultrasound sensors?

## Additional Models of Proximity Sensors

- **Map matching (sonar, laser):** generate small, local maps from sensor data and match local maps against global model.
- **Scan matching (laser):** map is represented by scan endpoints, match scan into this map.
- **Features (sonar, laser, vision):** Extract features such as doors, hallways from sensor data.

## Landmarks

### Landmarks

- Active beacons (e.g., radio, GPS)
- Passive (e.g., visual, retro-reflective)
- Standard approach is triangulation
- Sensor provides
  - distance, or
  - bearing, or
  - distance and bearing.

# Sensors and Sensor Models

## QR Code Markers



Source: IEEE RAS Summer School

## Colored Markers



Source: Uni Freiburg, Wolfram

# Sensors and Sensor Models

## Probabilistic Model

Algorithm for Landmark Detection Model:

$$P(z|x, m)$$

For Each Measurement of a Target  $i$

$$z = \langle d, \alpha \rangle, x = \langle x, y, z \rangle$$

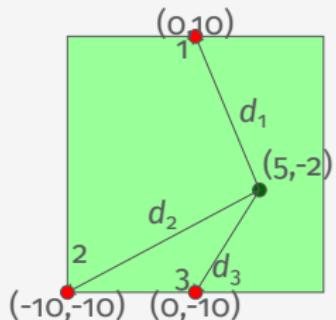
$$\hat{d} = \sqrt{(m_{x_i} - x)^2 + (m_{y_i} - y)^2} \quad (8)$$

$$\hat{\alpha} = \text{atan2}(m_{y_i} - y, m_{x_i} - x) - \theta \quad (9)$$

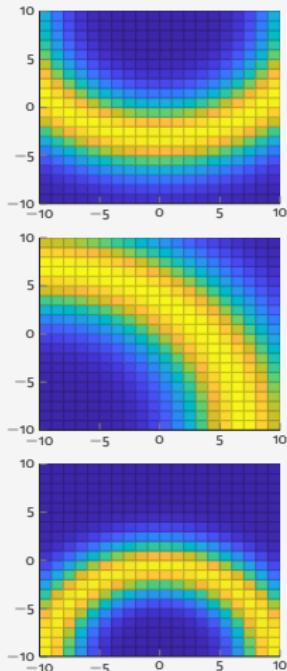
$$P(z|x, m) = \prod^i \Phi(\hat{d} - d, \sigma_d) \cdot \Phi(\hat{\alpha} - \alpha, \sigma_\alpha) \quad (10)$$

# Distance based Densities

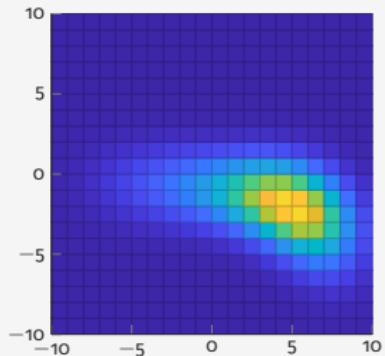
## Map



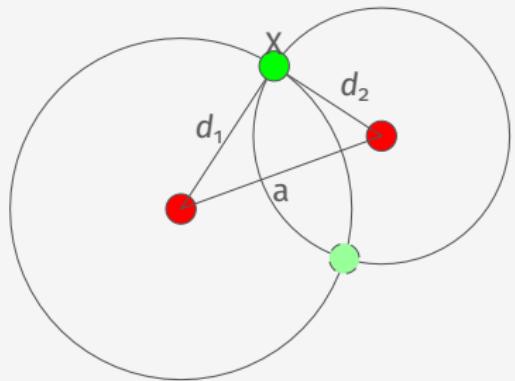
## Distance Densities



## Combined Probability



## Distance only Calculations



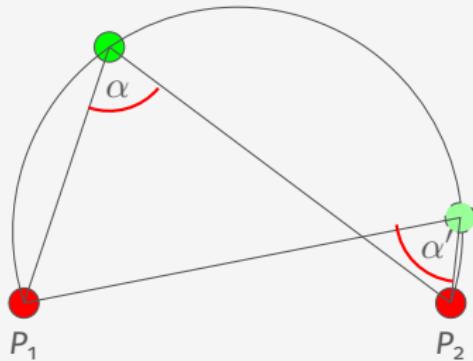
## Calculations

Using Trigonometry, including Cosine Rule and coordinates of markers to find intersections of distance circles.

- Beware of Ghost Positions
- Can be removed with multiple markers, odometry readings, or controlled movements

# Sensors and Sensor Models

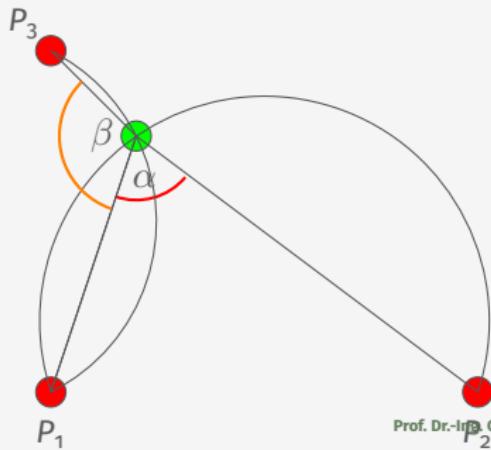
## Bearings only no uncertainty



## Calculations

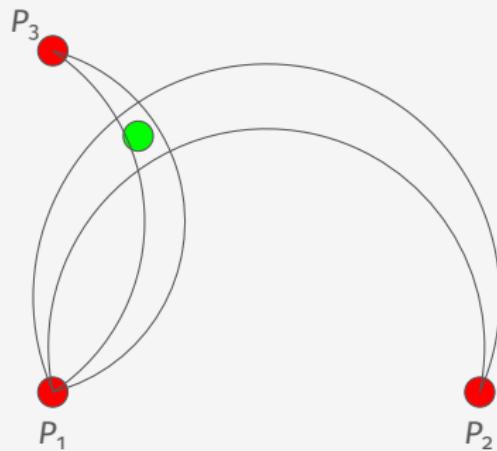
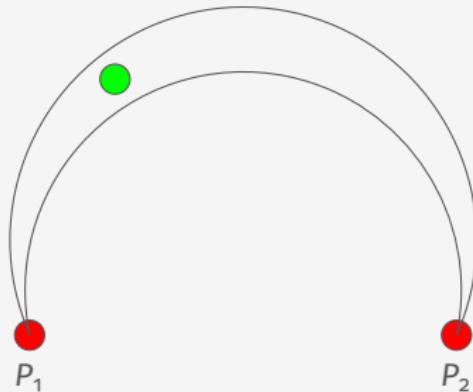
As before, using Trigonometry, including Cosine Rule and coordinates of markers to find intersections of distance circles.

- Beware of Ghost Positions
- Can be removed with multiple markers, odometry readings, or controlled movements



# Sensors and Sensor Models

## Bearings only with Uncertainty



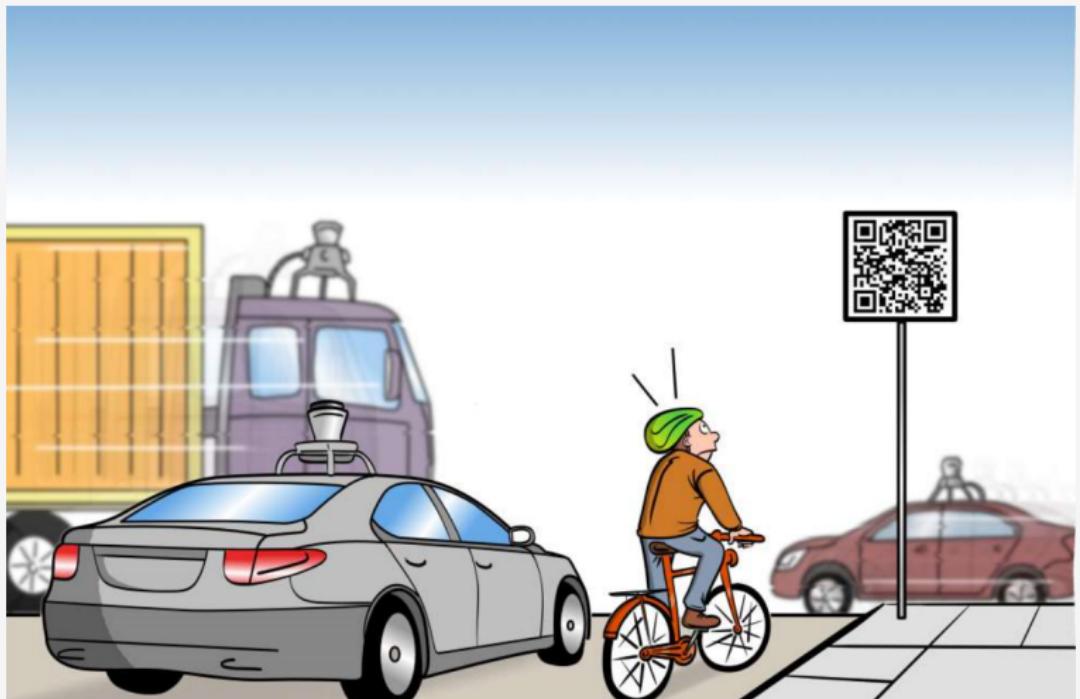
# Sensors and Sensor Models

## Summary of Sensor Models

- Explicitly modeling uncertainty in sensing is key to robustness.
- In many cases, good models can be found by the following approach:
  - Determine parametric model of noise free measurement.
  - Analyze sources of noise.
  - Add adequate noise to parameters (eventually mix in densities for noise).
  - Learn (and verify) parameters by fitting model to data.
  - Likelihood of measurement is given by “probabilistically comparing” the actual with the expected measurement.
- This holds for motion models as well.
- It is extremely important to be aware of the underlying assumptions!

# Sensors and Sensor Models

The Future??



Source: Christian Möller