

## Austrian Olympiad in Informatics

Wien Contest 2023

QSORT • v1.0

## Quicksort

Quicksort is a simple sorting algorithm that works well in practice, but is not quite as quick from a theoretical point of view. In this task we will have a further look at this property.

Quicksort is a recursive algorithm:

- choose a pivot element p
- move the smaller elements of the to the left of the pivot p
- move the bigger elements to the right of the pivot p
- sort the sections right and left to the pivot p with recursive calls



The maximum recursion depth can be used as a runtime approximation.

To implement Quicksort in C++, there is a standard template library function called std:: stable\_partition, which partitions an array in a left and right half, without rearranging the elements within each half relative to the other ("stable"). What the algorithm is doing behind the scenes isn't relevant for this task.

```
auto mid = std::stable_partition(bgn, end, [p](int x) {
   return x < p;
});</pre>
```

Here the area of from bgn to end exclusive is rearranged, in such a way that all elements < p are to the left and all other elements are to the right of p. The return value of the call in mid points to the first element satisfying >= p.

For the task we will be considering the following quicksort implementation:

```
#include <algorithm>
template <class Iterator>
```



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The function is called with two iterators <sup>1</sup> on a range of integers sorting these. The return value represents the maximum recursion depth. Two points that might be useful to point out:

- the first element is choosen as the pivot.
- the pivot element p is placed at mid, as it is the first element and stable\_partition is a stable algorithm.

Can you use these properties to design input data, such that the algorithm *exactly* reaches the recursion depth k. You are given n and k. Find an arbitrary permutation of  $1, 2, \ldots n$ , for which quicksort reaches the recursion depth k. If there is none print -1 instead.

#### Input

One line with n and k.

#### Output

an permutatoin from  $1, 2, \dots n$  or -1, if there is no solution. If there are multiple solutions, output any one of them.

### Examples

Input	Output	Comments
5 5	1 2 3 4 5	Here all elements are shifted to the right

Input	Output	Comments
4 3	2 1 3 4	alternative solutions are: e.g.: 2 1 4 3 or 3 1 2 4.

Input	Output	Comments
2 1	-1	Both 1 2 and 2 1 have a recursion depth of 2.

## Scoring

In general it holds that:  $1 \le k \le n \le 10^5$ .

Subtask 1 (15 Points):  $n \le 10$ 

Subtask 2 (10 Points):  $n \leq 20$ 

i.e. a.begin() and a.end() of a std::vector<int> a.



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Subtask 3 (10 Points):  $n \le 100$ 

Subtask 4 (15 Points):  $n \le 500$ 

Subtask 5 (10 Points):  $n \le 3000$ 

Subtask 6 (10 Points): k = n (worst case)

Subtask 7 (10 Points):  $k = \lceil \log_2 n \rceil$  (best case)

Subtask 8 (20 Points): No additional constraints

#### Constraints

Time limit: 1 s Memory limit: 256 MB