

An aerial photograph of Zurich, Switzerland, showing a river flowing through the city, surrounded by dense urban development and green spaces. The image is used as a background for the slide.

Why More Information Is Not Always Better Braess Paradox and Information Supply

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Introduction

- **Braess Paradox**

- More options (road infrastructure) can lead to worse societal outcomes (congestion)

- **Research Question**

- Does Braess Paradox also happen for more information?
- **More Information = Better Outcomes?**

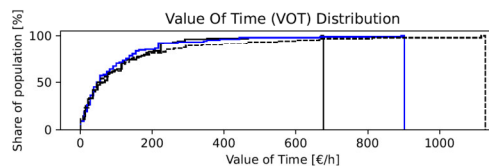
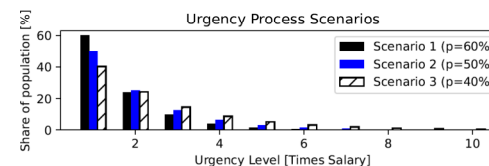
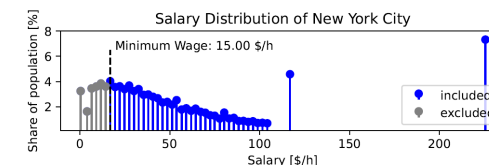
- **Background**

- More available real-time traffic information in the advent of internet
- Does this lead to better traffic situations?
- Should rational drivers consider external information?

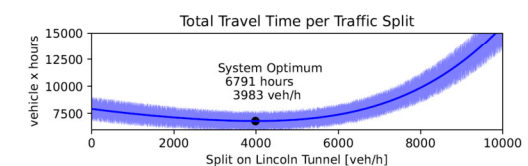
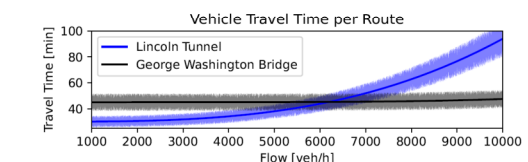
Case Study: Route Choice Behaviour in New York (1/2)

- New York and New Jersey are connected via two routes
- The route via Lincoln Tunnel is shorter and faster
- But if too many drivers use it, it gets congested, thus travel time increases

- Nash-equilibrium = Wardrop's equilibrium
 - **Behaviour: Rational drivers choose routes that minimize their own costs**
 - Leads to: Drivers choose Lincoln Tunnel until both routes similar travel times/costs
 - Chasing similar travel times gives worse average than what the system optimum would be



(A) Population Model



(B) Travel Time Model

Case Study: Route Choice Behaviour in New York (2/2)

Our algorithm that models route choice behaviour of rational driver population

Algorithm 1 Simulation of Drivers' Daily Route Choice

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1: for each day do
2:   for each driver do
3:      $\hat{T}_A, \hat{T}_B \leftarrow \text{EstimationScheme}(\mathcal{I}_A^P, \mathcal{I}_A^R, \mathcal{I}_B^P, \mathcal{I}_B^R, w^P, w^R)$ 
4:      $\hat{C}_A, \hat{C}_B \leftarrow \text{Cost}(\hat{T}_A, \hat{T}_B)$ 
5:     if  $\hat{C}_A < \hat{C}_B$  then
6:        $\text{Choice} \leftarrow A$ 
7:     else if  $\hat{C}_B < \hat{C}_A$  then
8:        $\text{Choice} \leftarrow B$ 
9:     else
10:       $\text{Choice} \leftarrow \text{random}(A, B)$ 
11:    end if
12:    if  $\text{random}(0, 1) \leq \gamma$  then
13:      if  $\text{Choice} = A$  then
14:         $\text{Choice} \leftarrow B$ 
15:      else if  $\text{Choice} = B$  then
16:         $\text{Choice} \leftarrow A$ 
17:      end if
18:    end if
19:    Driver Takes Route:  $\text{Choice}$ 
20:  end for
21:  Update Information Sets:  $\mathcal{I}_A^P, \mathcal{I}_A^R, \mathcal{I}_B^P, \mathcal{I}_B^R$ 
22: end for

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We supply drivers with different amounts of information

- Travel times based on personal experiences
- Historical travel times reported by authority
- Different time horizons

Four different travel time estimation schemes

Scheme	Formula
Plain Average	$\hat{T}_r^I = \frac{1}{h} \sum_{v \in \mathcal{I}} v$
Geometric Weights	$\hat{T}_r^I = \frac{1}{h} \sum_{v \in \mathcal{I}} (v \times w_v)$ with $w_v = \frac{1}{v_j}$
Exponential Weights	$\hat{T}_r^I = \frac{1}{h} \sum_{v \in \mathcal{I}} (v \times w_v)$ with $w_v = \exp(v_j)$
Maximum Scheme	$\hat{T}_r^I = \max_{v \in \mathcal{I}}(v)$

Results

Depending on how much information gets processed, different convergence schemes

Information sources

- Personal Experiences → Stable Equilibria ①
- Reported, Historical Data → Oscillations ②

Information Horizon

- Longer horizon → Equilibrium Stability ③
- Shorter horizon → Faster Convergence ④

Conclusion

- More reported information does not necessarily support the population to converge to its equilibrium
- Choice of different models does not change the position of equilibrium in our simulation

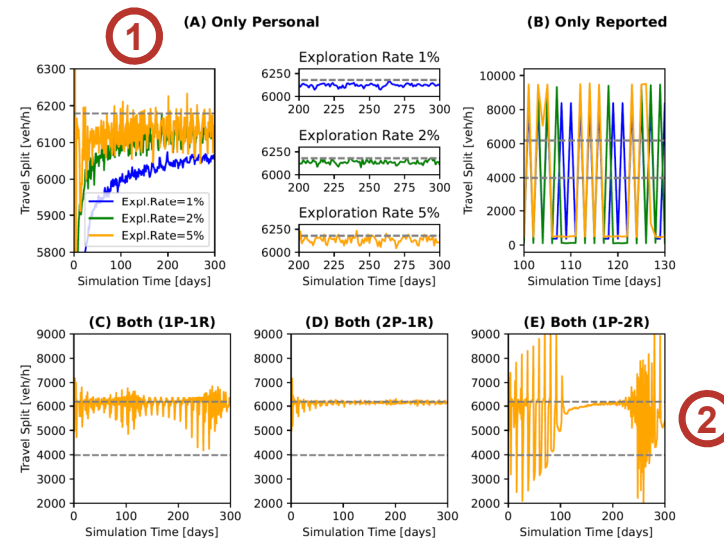


Figure 3.1: Plain Average (Horizon 10)

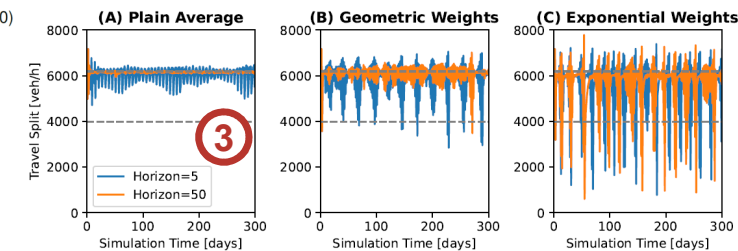


Figure 3.2: Different Weighting Schemes Compared (2P-1R, 5% Exploration Rate)

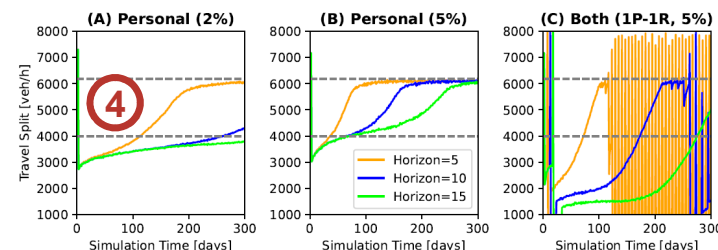


Figure 3.3: Maximum Scheme

Outlook / Future Works

- Heterogeneous populations with different information availability and travel time estimation schemes
- More routes & options and more complex information
- Systematic misinformation to push user equilibrium towards system optimum?

