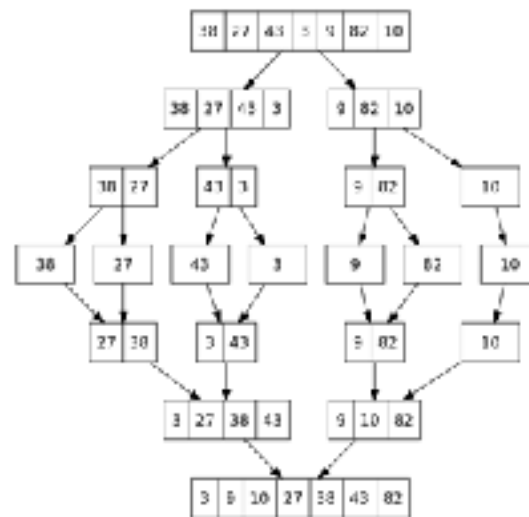




# Merge Sort

6 5 3 1 8 7 2 4

# Merge Sort



## Merge Sort (iterative)

1. Divide array of  $n$  elements into  $n$  arrays of 1 element
2. Merge neighboring arrays in sorted order
3. Repeat 2 until there's only one array

## Merge Sort (recursive)

1. If array is one element, good job it's sorted!
2. Otherwise, split the array and merge sort each half
3. Merge combined halves into sorted whole

# Big O

	Bubble Sort	Merge Sort
Time	$O(n^2)$	$O(n \cdot \log n)$
Space	$O(1)$	$O(n)$

## Why is merge sort faster?



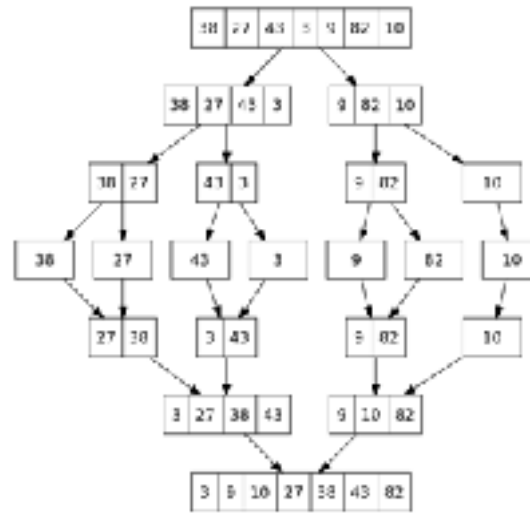


## Merge Sort Speedup

- Splitting a list into two sublists is a linear time operation
- Combining two lists that are each already sorted into one list that is sorted is a linear time operation
- There are  $\log_2(n)$  steps needed to go from  $n$  lists of one item each to one list of  $n$  items (and vice-versa)

$O(n)$  ops to split or merge

$O(\log n)$  times we split/merge



$$O(n) * O(\log n) = O(n \cdot \log n)$$

## Intuition?

- Divide and conquer: can efficiently handle subtasks, and also efficiently combine sorted lists.
- Reduce the possible comparisons dramatically – only have to compare certain pairs of elements (avoiding vast majority of possible pairs).