佇列

佇列三排隊

```
isEmpty (): boolean {query}
enqueue (in newItem : QueueItemType)
dequeue () throw QueueException
getfront (out queueFront : QueueItemType)
        {query} throw QueueException
dequeue (out queueFront : QueueItemType) throw QueueException
```

字串轉數字

```
do { aQueue. dequeue (ch)
  } // while (ch is blank)
n=0
done = False
while (! done and ch is digit) {
  n = nx lot integer represented by ch
  if (aQueue. isEmpty () )
    done = True;
  else
    aQueue. dequeue (ch)
} // while
```

有小數点

```
if ( !done and ch = '.' ) {
  aQueue. dequeue (ch)
  p=0
  while ( ! done and ch is digit ) {
    n = n × 10 + integer of ch
    p ++
    if ( aQueue. isEmpty () )
      done = True;
    else
      aQueue. dequeue (ch)
  } // while
  n = n × (0.1)^p
} // if
```

```
isPal (in str : string ): boolean
 aQueue. createQueue ()
 aStack. createStack ()
for ( the next character ch in str ) {
  aQueue. enqueue (ch)
  aStack. push (ch)
} // for
charEqual = True
while ( ! aQueue. isEmpty () && charEqual )
```

法一、

```
{aQueue.dequeue(front)
 aStack.pop(top)
 if(front != top)
   charEqual = False
} //while
```

法二、

```
{aQueue.getFront(front)
 aStack.getTop(top)
 if(front = top){
   aQueue.dequeue
   aStack.pop()
 } //if
 else
   charEqual = False
} //while
```

link list 有 front 和 back

circular linked list 只有 back

Insert: back = (back + 1) % MAX_QUEUE;
item[back] = newItem
++count;

Delete: front = (front + 1) % MAX_QUEUE;
--count;

全空: count = 0

全滿: count = MAX_QUEUE

多宣告一個空間: MAX_QUEUE + 1
isFull

新增: enqueue(): aList.insert(aList.getLength()+1, newItem)

移除: dequeue(): aList.remove(1)

擷取: getFront(queueFront): aList.retrieve(1, queueFront)

事件驅動

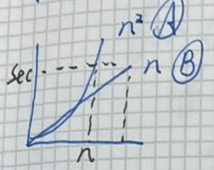
```
Simulate()
  Create an Empty  bankQueue; // represent the bank line
        "          eventList; // keep the future events
  Get the earliest arrival event X from input file
  Put X into eventList;
  while (eventList is not Empty) {
    newEvent = the earliest event in evenList
    if (newEvent is an arrival event)
      processArrival();
    else
      processDeparture();
  }//while
```

演算法效率

空間效率

時間效率

{ 實作
  電腦
  資料



A: 指數成長 slow

B: 線性成長 quick

1. $O(1)$ best
2. $O(\log_2 n)$
3. $O(n)$
4. $O(n \log_2 n)$
5. $O(n^2)$
6. $O(n^3)$
7. $O(2^n)$ worst

Stable Sort vs. UnStable sort

bubble
insertion
merge
radix

selection
quick
heap

bubble Sort

```
void bubbleSort (int A[], int n){
  for (pass = 1; pass < n; ++pass){
    for (int index=0; index < n-pass; index++){
      if (A[index] > A[index+1])
        swap (A[index], A[index+1]);
    }// for
  }// for
}// bubble Sort
```

Comparisons:

$n + \sum_{pass=1}^{n+1}(n-pass+1) + \sum_{pass=1}^{n-1}(n-pass)$

$= n+2[n\times(n-1) - n(n-1)/2] + (n+1) = n^2+n+1 \rightarrow O(n^2)$

核心比較次數:

$(n-1)+(n-2)+(n-3)+\cdots+1$

$= n(n-1)/2 = 0.5n^2 - 0.5n \rightarrow O(n^2)$

```
void selectionSort (int A[], int n){
  for (last = n-1; last >0; --last){
    int largest = indexOfLargest (A, last+1);
    swap (A[largest], A[last]);
  }// for
}// selectionSort ()
```

```
int indexOfLargest (int A[], int size){
  int indexSoFar = 0;
  for (index = 1; index < size; ++index)
    if (A[indexSoFar] < A[index])
      indexSoFar = index;
  return indexSoFar;
}//
```

Comparisons: $\sum_{size=n}^{2} (size - 1)$

$= (n-1) + (n-2) + \cdots + 1 = n(n-1)/2 \rightarrow O(n^2)$

```
void insertionSort (int A[], int n){
  for (inserted = 1; unsorted < n; ++unsorted){
    int loc = unsorted, nextItem = A[unserted];
    for (; (loc > 0) && (A[loc-1] > nextItem); --loc)
      A[loc] = A[loc-1];
    A[loc] = nextItem;
  }// for
}// insertionSort
```

```
void shellSort (int A[], int n){
  for (int h=n/2; h>0; h=h/2)
  for (int unsorted=h; unsorted<n; ++unsorted){
    int loc = unsorted;
    int nextItem = A[unsorted];
    for (; (loc>=h) && (A[loc-h] >nextItem); loc-=h)
      A[loc] = A[loc-h];
    A[loc] = nextItem;
  }// for
}// shellSort   it is not stable
```

MergeSort

先：分組　各組排序　後：合併

```
void mergeSort (DataType theArray[], int first, int last){
  if (first < last){
    int mid = (first + last)/2;
    mergeSort (theArray, first, mid);
    mergeSort (theArray, mid+1, last);
    merge (theArray, first, mid, last);
  }// if
}// mergeSort
```

```
void merge (DataType theArray[], int first, int mid, int last){
  DataType tempArray[MAX_SIZE]
  int first1 = first, last1 = mid;
  int index = fist
  for (; (first1 <= last1) && (first2 <= last2); ++index)
    if (theArray[first1] < theArray[first2]) {
      tempArray[index] = theArray[first1];
      ++first1;
    }//if
    else {
      tempArray[index] = theArray[first2];
      ++first2;
    }//
```

QuickSort

pivot 樞紐，軸

先：分組(軸的位置)

items < pivot

items >= pivot

Pivot is now incorrect sorted position

後：遞迴呼叫

QuickSort: it is not stable

Radix Sort 基數排列

MSD (Most Significant Digit)

排序時最重要的數

先：分組

後：串接

比較

	Worst case	Average case
Selection	n^2	n^2
Bubble	n^2	n^2
Insertion	n^2	n^2
MergeSort	$n * \log n$	$n * \log n$
QuickSort	n^2	$n * \log n$
RadixSort	n	n

樹

位置：list, stack, queue, binary tree

內容：sorted list, binary search tree

Parent - child 親子關係

Subtree 子樹

二元樹 binary tree

Full < Complete < Balanced

```
const int MAX_NODES = 100;
class TreeNode {
 private:
    TreeItemType item;
    int leftChild;
    int rightChild;
};
TreeNode tree[MAX_NODES];
int root; //樹根
int free; //閒置串列
leftChild = 2 * parent + 1
rightChild = 2 * parent + 2
parent = (child - 1)/2
```

Max 樹高：$h = \lceil \log_2(n+1) \rceil$

min 樹高 $h = \lceil \log_2(n) \rceil + 1$

N_2：有 2 個 children

N_0：leaves

$N_0 = N_2 + 1$

邊 $= 2 \times N_2 + 1 \times N_1$

點 = 邊 + 1

```
inorderTraversal (binaryTree root) {
  binaryTree treePtr = root;
  nodeStack aStack;
  while (!aStack.empty() || (treePtr != NULL)){
    while (treePtr != NULL) {
      aStack.push(treePtr);
      treePtr = treePtr->leftChild;
    } // while
    aStack.pop(treePtr)
    cout << treePtr->data << endl;
    treePtr = treePtr->rightChild
  } // while
} // inorder
```

```
preorderTraversal (binaryTree root){
  binaryTree treePtr = root;
  nodeStack aStack;
  while (!aStack.empty() || (treePtr != NULL))
  { while (treePtr != NULL) {
      cout << treePtr -> data << endl;
      aStack.push(treePtr -> rightChild);
      treePtr = treePtr -> leftChild;
    } //while
    aStack.pop (treePtr);
  } //while
} //preorder
```

心得：

期中考後，練習的題目困難度越來越高，就算5个檔案都对，第6个檔案也有可能会錯，所以要考慮的情況变得非常多。希望能藉由這些練習讓我的能力上升。