

叩元 5 堆疊

type  $abc \leftarrow dde \leftarrow ef \leftarrow fg$

新增删除一笔资料

while (not end of line)

是否為空

{ Read a new character ch

if (ch is not ' $\leftarrow$ ') {

Add ch to the ADT

else if (the ADT is not empty)

Remove the last item from the ADT

else

Ignore '←'

3 1/2 white

□ Operation Contract for the ADT stack

is Empty() : boolean      是否为空

push (in new Item: StackItem Type) 新增一筆

pop() throw StackException 移除最近一算

getTop(out stackTop: stackItemType) 获取最近算

pop() out stackTop: stackItemType) 獲取後移除最近一筆

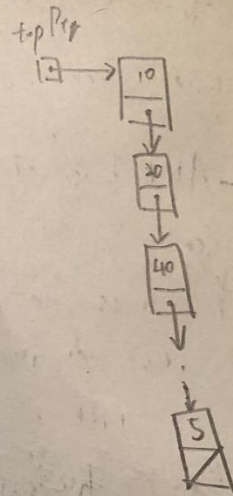
# ADT stack - Pointer-based Implementation

Void stack::push(const StackItemType & newItem)

```
{ try
{ StackNode *newPtr = new StackNode;
  newPtr->item = newItem;
  newPtr->next = topPtr;
  topPtr = newPtr;
}
```

} // try

} // end push



Void stack::pop()

```
{ if (!isEmpty())
```

```
{ StackNode *temp = topPtr;
```

```
  topPtr = topPtr->next;
```

```
  temp->next = NULL;
```

```
  delete temp;
```

```
} // if
```

```
} // pop
```

Void stack::getTop(StackItemType & stackTop)

```
{ if (!isEmpty())
```

```
  stackTop = topPtr->item;
```

```
} // getTop
```

Void stack::pop(StackItemType & stackTop)

```
{ if (!isEmpty())
```

```
{ getTop();
```

```
  pop();
```

```
} // if
```

```
} // pop
```

- Pointer-based implementation is more efficient

- ADT list approach reuses an already implemented class

□ Much simpler to write

□ Saves programming time

心得：堆疊算是滿直接的存資料方式，也就是先進後出，在某些特別的處理資料就可以利用堆疊來存放資料，尤其是會用到前，中，後序的情況，通常都會使用堆疊。

單元

□ ADT

isEmpty

enqueue

dequeue

getFront

dequeue

環狀

Void

{ Que

new

if

else

{

}

}



## 單元 6 Queue 佇列三排隊

□ ADT queue operations

class

isEmpty() 是否為空

enqueue (in newItem: QueueItem Type) 新增

dequeue() 移除

getFront(out queueFront: QueueItem Type) 擷取

dequeue(out queueFront: QueueItem Type) 擷取後移除

環狀佇列: 新增

Void Queue::enqueue(const QueueItem Type& newItem)

{ QueueNode \*newPtr = new QueueNode;

newPtr->item = newItem;

if (isEmpty())

newPtr->next = newPtr;

else

{ newPtr->next = backPtr->next;

backPtr->next = newPtr;

}

backPtr = newPtr;

}

環狀佇列: 移除

```
Void Queue::dequeue() throw(QueueException)
{ if (isEmpty())
    throw ...;
  else
  { QueueNode *tempPtr = backPtr->next;
    if (backPtr == backPtr->next)
      backPtr = NULL;
    else backPtr->next = temp->next;
    tempPtr->next = NULL;
    delete tempPtr;
  } // else
} // dequeue()
```

心得: 我覺得佇列跟堆疊有美相似, 所以在  
剛學時並不會有大困難的地方, 只是需要  
注意佇列的執行方式與堆疊相反, 佇列  
是先進先出, 主要還是判斷條件的部分需  
要小心。

## 單元 7 演算法

### □ Analysis of algorithms

- Time efficiency 時間效率
- space efficiency 空間效率

### □ Difficulties

- Implementation

- Computer

- Dataset

□ Enables comparison between two algorithms

- Algorithm A requires time proportional to  $n^2$

- B to  $n$

□ Algorithm B is faster than Algorithm A

-  $n^2$  and  $n$  are growth-rate functions

- Algorithm A is  $O(n^2)$  - order  $n^2$

- Algorithm B is  $O(n)$  - order  $n$

- 1.  $O(1)$  常數
- 2.  $O(\log n)$  對數
- 3.  $O(n)$  線性
- 4.  $O(n \log n)$
- 5.  $O(n^2)$  平方
- 6.  $O(n^3)$  立方
- 7.  $O(2^n)$  指數

- Big O notation

### □ Properties of growth-rate functions

-  $O(n^3 + 2n)$  is  $O(n^3)$ : ignore low-order terms 忽略低次項

-  $O(5f(n)) = O(f(n))$ : ignore multiplicative constant 忽略常數

-  $O(f(n)) + O(g(n)) = O(f(n) + g(n))$



□ Worst-case analysis 最多

— the maximum time an algorithm require to solve problem of size  $n$

□ Average-case analysis 平均

— the average time

□ Best-case analysis 最少

— the minimum time

□ Sequential search 循序搜尋

□ Look each item, stop when the desired item is found, or the data is end

— Efficiency

Worst :  $O(n)$

average :  $O(n)$

best :  $O(1)$

## □ Binary search

### - Strategy

- divide array in half, determine which half could contain the item, and discard the another

### - Efficiency

□ Worst:  $O(\log n)$

best:  $O(1)$

## □ Simple Sort

氣泡排序: 兩兩比較

選擇排序: 找到最小的排到前面

插入排序: 將 item 插入適當的位置

## □ Faster Sort

- Mergesort: 先 → 分組各自排序  
                   $O(n \log n)$  後 → 再合併再排序

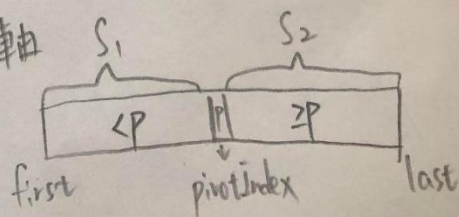
### - Quicksort

#### □ strategy

- choose a pivot 樞紐, 軸

先: 分組 (軸的位置)

後: 遞迴呼叫





## □ Radix Sort

### □ Strategy

- Decompose the sort key by the radix 分解取部分值

□ Treats a key as a character string 分配至對應容器

□ Repeatedly assign the keys into groups (buckets) according to the  $i$ th character

心得：演算法在程式中扮演非常重要的角色，經常會被使用，對我而言，看到有使用遞迴的演算法經常需要思考一下才能理解，演算法是一項很好用的工具。

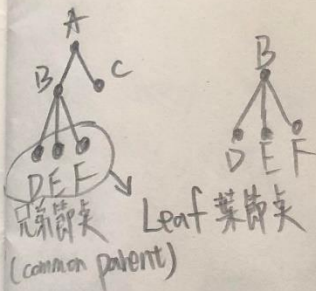
## 單元 8 二元樹

□ Trees are composed of nodes and edges

- Parent-child relationship between two nodes

- Ancestor-descendant relationships among nodes

□ Subtree of a tree: Any nodes and its descendants



□ Ancestor of node B

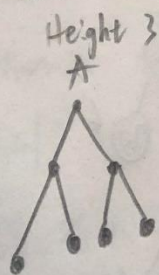
- A node on path from root to B

□ Descendant of node B

- // from B to a leaf

□ Height of Trees 樹高

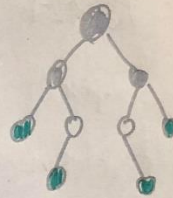
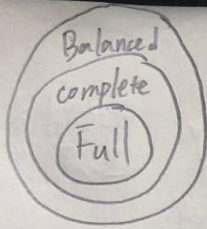
- Number of nodes along the longest path from root to leaf



# 最大階層 = 樹高

□ A binary tree of height  $h$  is full if

- Node at levels  $< h$  have two children each



□ Notes

$N_2$  = 3 nodes with two children

$N_0$  = 4 Leaves

$- N_0 = N_2 + 1$ ?

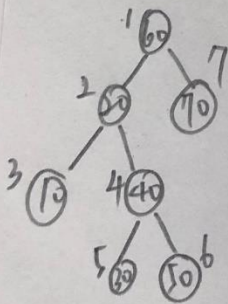
$B$  = 8 Branches (edges)

$- B = |E| = 2 * N_2 + 1 * N_1$

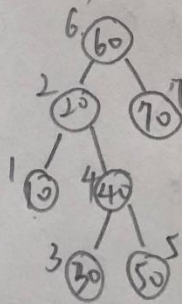
$- N_0 + N_2 + N_1 = |V| = |E| + 1 = 2 * N_2 + 1 * N_1 + 1$

$\Rightarrow N_0 = N_2 + 1$

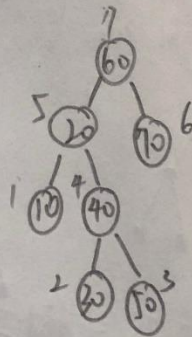
Traversal of a Binary Tree



preorder (60, 20, 10, 40, 30, 50, 70)



Inorder (10, 20, 30, 40, 50, 60, 70)



Postorder (10, 30, 50, 40, 20, 70, 60)

traverse (

if (

{

tr

tr

}

}

□ A bin

左 <

operation

Retrieval

Insertion

Deletion

Traversal

心得

3 解

能

式



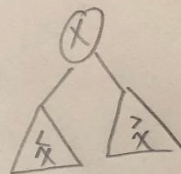
```

traverse (BinaryTree) {
    if (not empty)
    {
        traverse (Left subtree) ← 前序
        traverse (Right subtree) ← 中序
    } // if
} //

```

□ A binary search tree

左 < x < 右



operation	Average case	Worst case
Retrieval	$O(\log n)$	$O(n)$
Insertion	$O(\log n)$	$O(n)$
Deletion	$O(\log n)$	$O(n)$
Traversal	$O(n)$	$O(n)$

心得: 在大一時有接觸過二元樹, 當時只有表面的了解, 但現在又再次接觸後, 更加了解到二元樹有其他型態, 以及不同的列印順序, 我認為這其中困難的是, 在寫程式要特別留意不能丟失父節點。