

心得:

### 心得

CH1

在看完教學影片後讓更深刻的了解遞迴的運作，老師舉了許多的實例，收穫良多。

CH2.

在大一時就有聽過抽象化，卻不知道是什麼意思，在老師的講解後終於知道意思了，也懂了如何使用 class。

CH3.

在大一的時候最害怕碰到的就是 linked-list 了，老師細心的講解用列車來比喻讓我輕易的了解如何正確的使用。  
門牌等

CH4.

以前都沒有聽過前中序的觀念，讓我知道原來有別的運算方式，可以不用考慮括弧，沒有結合律等的優勢使用前、後序。

# CH1.

以遞迴找第k小的值：樞紐 第1章

想法：  
 找一個字當樞紐  $\rightarrow$   $\begin{matrix} <P & P & >P \end{matrix}$   
 使用二分法  
 找其中一邊

ex.  $k=4$   $\begin{matrix} 30 & 7 & 25 & 39 & 19 & 48 & 12 & 16 & 12 \\ 12 & 7 & 25 & 19 & 16 & 30 & 39 & 48 \end{matrix}$   
 48 and 39 大於 30  $\rightarrow$  放到最右邊  
 因 30 的位置  $> 4 \rightarrow$  後面的值不用看  
 可找到位置

排序

```

kSmall ( k : integer, onArray : ArrayType, first : integer, last : integer ) : ValueT,
if ( k < pivotIndex - first + 1 )
    return kSmall ( k, anArray, first, pivotIndex - 1 ) // 前半
else if ( k == pivotIndex - first + 1 )
    return p
else
    return kSmall ( k - (pivotIndex - first + 1), anArray, pivotIndex + 1, last ) // 後半
    
```

河內塔：

```

solveTowers ( count, source, destination, spare )
if ( count == 1 )
    print ( "Move from", source, "to", destination )
else {
    solveTowers ( count - 1, source, spare, destination );
    solveTowers ( 1, source, destination, spare );
    solveTowers ( count - 1, spare, destination, source );
}
    
```

ex. 3

```

Towers ( 3, A, C, B )
├── Towers ( 2, A, B, C )
│   ├── Towers ( 1, A, C, B )
│   │   └── Step 1
│   └── Step 2
│       ├── Towers ( 1, C, B, A )
│       │   └── Step 3
│       └── Towers ( 1, B, A, C )
│           └── Step 5
└── Step 4
    ├── Towers ( 2, B, C, A )
    │   ├── Towers ( 1, B, A, C )
    │   │   └── Step 5
    │   └── Step 6
    │       ├── Towers ( 1, A, C, B )
    │       │   └── Step 7
    │       └── Towers ( 1, A, C, B )
    │           └── Step 7
    └── Towers ( 1, A, C, B )
        └── Step 1
    
```



# Binary Recursion

求最大公因數:

```
gcd1 (int x, int y) {
    if (y == 0)
        return x;
    else if (y > x)
        return gcd1(x, y % x);
    else
        return gcd1(y, x % y);
} // gcd1()
```

ex.  $x=9, y=6$

$gcd1(6, 3) = 3$

$\downarrow$   
 $gcd1(3, 0) = 3$

$\downarrow$   
 $x=3, y=0$   
return 3

if ( $x \geq y$ ) 效率較高 (遞迴次數較少)

```
gcd2 (int x, int y) {
    if (! (x % y))
        return y;
    else
        return gcd2(y, x % y);
} // gcd2()
```

$gcd2(6, 3) = 3$

$\downarrow$   
 $x=6, y=3$   
return 3

## Binary search with an Array

想法: if (Array 只有一個值)

那個值就是最大;

else if (Array 不只一個值)

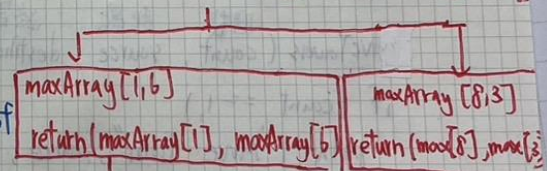
max Array (Array) is the maximum of

左右都要找 { max Array (left - 半的 array) 和  
max Array (right - 半的 array)

ex.

maxarray [1, 6, 8, 3]

return max (maxArray [1, 6], maxArray [8, 3])



```
int binarysearch (const int Array[], int first, int last, int value) {
```

```
    int index;
```

```
    if (first > last)
```

```
        index = -1; // 不是最終答案
```

```
    else {
```

```
        int mid = (first + last) / 2; // 記錄終點
```

```
        if (value == Array[mid])
```

```
            index = mid;
```

```
        else if (value < Array[mid]) left
```

```
            index = binarysearch (Array, first, mid - 1, value);
```

else

right

index = binarysearch (array,

mid + 1, last, value);

// else if

return index;

Binary recursion

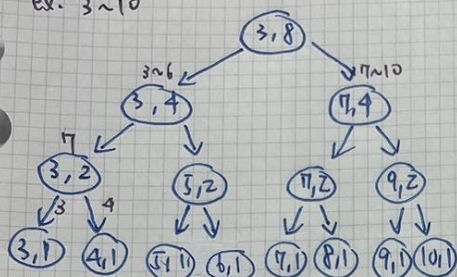
```
int sumB( int a, int n)
```

```
if (n == 1)
```

```
return a;
```

```
return sumB(a, n/2) + sumB(a+n/2, n-n/2)
```

ex.  $3 \sim 10$



費式數列:

$= \pi \sim 2$

$n^k$  at least double every other time

$n^k \geq 2^{k/2}$ , It is exponential (呼叫次數以指數成長)

ex.  $(5,3) \leftarrow (3,2) \leftarrow (2,1) \leftarrow (1,1) \leftarrow (1,0)$

Fibonacci(k)  $5 \rightarrow 4 \rightarrow 3 \rightarrow 2 \rightarrow 1$

```
if (k == 1)
```

```
return (k, 0) // base case: k=1  $\rightarrow (F_1, F_0)$ 
```

```
else
```

```
(i, j) = Fibonacci(k-1) //  $(F_{k-1}, F_{k-2})$ 
```

```
return (i+j, i) //  $(F_k = F_{k-1} + F_{k-2}, F_{k-1})$ 
```

(呼叫次數以線性成長)



## CH2.

第二章：

ADT (Abstract Data Type)

抽象化：不須要知道裡面的細節，直接拿來用

高內聚：highly cohesive modules desired

低耦合：loosely coupled modules desired

Concept：

描述：只須看懂用途就可使用 (specifications)

實作：製造的人才須要知道如何實作 (Implementation)

Data Abstraction：

Asks you to think what you can do to a collection of data independently of how you do it. (不須管如何達成目的)

ADT is composed of：

A collection of data

A set of operations on that data.

Specifying ADTs：Grocery list

Except for the first and last items in a list, each item has a unique predecessor (先行者) and a unique successor (後繼者)

Operation Contract for the ADT List

插入 insert (in index: integer, in newItem: ListItemType, out success: boolean)

刪除 remove (in index: integer, out success: boolean)

檢索 retrieve (in index: integer, out dataItem: ListItemType, out success: boolean)

reverseList (in alist: List, out source: boolean) 反轉整個序列

for (i = 1 to alist.getLength() - 1) {

alist.retrieve(i, dataItem, success);

alist.remove(i, success);

先刪後提

alist.insert(alist.getLength() - i + 2, dataItem, success);

} // for

The ADT Sorted List :

Maintain items in sorted order

Inserts and deletes items by their values, not their positions

新增 sortedInsert ( in newItem : ListItemType, out success : boolean )

移除 sortedRemove ( in index : integer, out success : boolean )

檢索 sortedRetrieve ( in index : integer, out dataItem : ListItemType, out success : boolean )

定位 locatePosition ( in anItem : ListItemType, out isPresent : boolean ) = integer { query ? }

C++ class :

An object is an instance of a class.

a class defines a new data type.

A class contains data members and methods 成員

By default, all members in a class are private

\* You can specify them as public

Constructors :

Create and initialize new instances of a class

Have the same name as the class.

No return type.

Destructors :

Destroys an instance of an object when the object's lifetime ends.

自動維護順序 (不實知道順序)



## 第3章

linked list

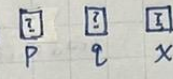
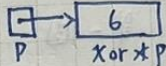

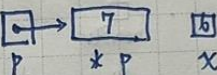
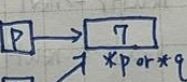
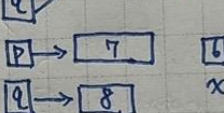

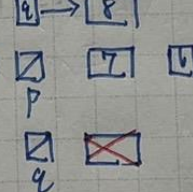
int x ;

p = new int ; 配製 (Dynamic allocation 動態配製)

p = &amp;x → 房子 x 的門牌 (address)

delete p ;

p = NULL ; 徹底刪除

(a) 申請空白門牌 int \*p, \*q ; (a) (b) 抄寫別人的門牌 p = &x ; (b) (c) 鳩佔鵲巢 \*p = 6 ; (c) (d) 配製 p = new int ; (d) (e) 堆放 \*p = 7 ; (e) (f) copy 另一張門牌 q = p (f) (g) 配製並堆放 q = new int ; (g) (h) 刪除 p = NULL ; X memory would leak (h) (i) 刪除 delete q ; (i) 

## 動態陣列配製

ex. int arraysize = 50 ;

double \* anArray = new double [arraysize] ;

delete [ ] oldArray ;

a node in a linked list usually a struct

```

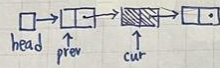
struct Node {
    int item;
    Node * next;
}; // end Node

Node * p;
p = new Node;

```

配製新的

Delete: 中間

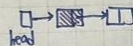


```

prev -> next = cur -> next;
or
prev -> next = prev -> next -> next; delete cur;
cur = NULL;

```

第一個

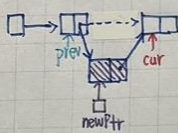


```

head = cur -> next;
cur -> next = NULL;
delete cur;
cur = NULL;

```

Insert: 中間

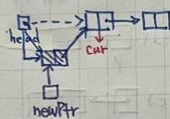


```

newPtr -> next = cur;
prev -> next = newPtr;

```

第一個

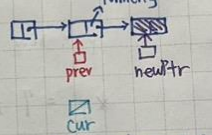


```

newPtr -> next = head;
head = newPtr;

```

尾巴



```

newPtr -> next = cur;
prev -> next = newPtr;

```

Visiting: (走訪)

Node \* prev, \* cur;

```

for (prev = NULL, cur = head; (cur != NULL) && (newValue > cur->item)); {
    prev = cur;
    cur = cur -> next;
}

```

List = List / const List & alist)

= size (alist.size)

```

{
    if (alist.head == NULL) // original is empty
        head = NULL;
    else {

```

head = new ListNode;

head -> item = alist.head -> item;

List Node \* newPtr = head;

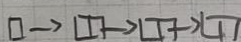
```

for (ListNode * origPtr = alist.head -> next; origPtr != NULL; origPtr = origPtr -> next) {
    newPtr -> next = new ListNode; newPtr = newPtr -> next; newPtr -> item = origPtr -> item; continue;
}

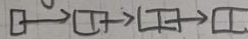
```

(Deep copy)

newPtr



origPtr



Double A.



```

} //end for
newPtr -> next = NULL;

find (int index) const {
    if ((index < 1) || (index > getLength(1)))
        return NULL;
    else {
        ListNode * cur = head;
        for (int skip = 1; skip < index; skip++)
            cur = cur -> next;
        return cur;
    } //else
} // find()

```

Array and 動態陣列 (linked list) 的比較

|                    |                        |
|--------------------|------------------------|
| Array = size 固定    | linked list = size 不定  |
| 較省空間               | 較花空間                   |
| retrieve 較慢        | retrieve/insert/delete |
| insert/delete 效率較差 | 較有效率                   |

Circular linked list :

```

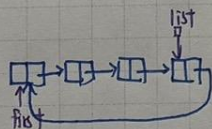
if (list != NULL) {
    Node * first = list -> next;
    Node * cur = first
}

```

```

do {
    show (cur -> item);
    cur = cur -> next;
} while (cur != first);
}

```



Dummy head Node =

★ Eliminate special case

```

for (prev = head, cur = prev -> next; (cur != NULL) &&
      (newValue > cur -> item);
     prev = cur,
     cur = cur -> next) {
    if (cur != NULL) { Delete
        prev -> next = cur -> next;
        cur -> next = NULL;
        delete cur;
        cur = NULL;
    }
}

```

newPtr -> next = cur; Insert  
prev -> next = NextPtr;

## 第 4 章

Infix expressions (中序)

ex.  $a \oplus b$ ,  $((a+b) \times c) / d$ 

Grammar:

中序:  $\langle \text{infix} \rangle = \langle \text{identifier} \rangle |$   
 $\langle \text{infix} \rangle \langle \text{operator} \rangle \langle \text{infix} \rangle$ 

Prefix expressions (前序)

ex.  $\oplus ab$ ,  $/ * + a b c d$ 特性:  
 一個前序式後面再接上非空字串  
 一定不是前序式

前序:

 $\langle \text{operator} \rangle = + | - | * | /$  $\langle \text{identifier} \rangle = a | b | c | \dots | z$  $\langle \text{prefix} \rangle = \langle \text{identifier} \rangle |$  $\langle \text{operator} \rangle \langle \text{prefix} \rangle \langle \text{prefix} \rangle$  $\langle \text{operator} \rangle = + | - | * | /$  $\langle \text{identifier} \rangle = a | b | \dots | z$ 

Postfix expressions (後序)

ex.  $ab \oplus$ ,  $a b + c * d /$ 

後序:

 $\langle \text{postfix} \rangle = \langle \text{identifier} \rangle |$  $\langle \text{postfix} \rangle \langle \text{postfix} \rangle \langle \text{operator} \rangle$  $\langle \text{operator} \rangle = + | - | * | /$  $\langle \text{identifier} \rangle = a | b | \dots | z$ 

前序、後序的 advantages:

沒有優先權

沒有結合律

沒有括弧

順序是唯一的

Backtracking (持續尋找路不通就跳回再找)