

✓ 恭喜！您通过了！

下一项



1 / 1 分

1。

Recall the derivation of EM algorithm. In our notation, X is observable data, Z is latent variable and θ is a vector of model parameters. We introduced $q(Z)$ — an arbitrary distribution over the latent variable. Choose the correct expressions for the marginal log-likelihood $\log p(X | \theta)$:



$$\int q(Z) \log \frac{p(X, Z | \theta)}{q(Z)} dZ + \int q(Z) \log \frac{q(Z)}{p(Z | X, \theta)} dZ$$

正确

$$\begin{aligned} & \int q(Z) \log \frac{p(X, Z | \theta)}{q(Z)} dZ + \int q(Z) \log \frac{q(Z)}{p(Z | X, \theta)} dZ = \\ & \int q(Z) \log p(X, Z | \theta) dZ - \int q(Z) \log q(Z) dZ + \\ & + \int q(Z) \log q(Z) dZ - \int q(Z) \log p(Z | X, \theta) dZ = \\ & = \int q(Z) \log \frac{p(X, Z | \theta)}{p(Z | X, \theta)} dZ = \int q(Z) \log p(X | \theta) dZ = \log p(X | \theta) \end{aligned}$$



$$\log \int p(X, Z | \theta) dZ$$

正确

Z is integrated out:

$$\log \int p(X, Z | \theta) dZ = \log p(X | \theta)$$



$$\mathbb{E}_{q(Z)} \log p(X, Z | \theta) - \mathbb{E}_{q(Z)} \log p(Z | X, \theta)$$

正确

$$\begin{aligned} & \mathbb{E}_{q(Z)} \log p(X, Z | \theta) - \mathbb{E}_{q(Z)} \log p(Z | X, \theta) = \\ & = \mathbb{E}_{q(Z)} \log \frac{p(X, Z | \theta)}{p(Z | X, \theta)} = \mathbb{E}_{q(Z)} \log p(X | \theta) = \log p(X | \theta) \end{aligned}$$

EM algorithm

测验, 4 个问题



$$\int q(Z) \log p(X|\theta) dZ$$

4/4 分 (100%)

正确

$\log p(X|\theta)$ does not depend on Z .

$$\int q(Z) \log p(X|\theta) dZ = \log p(X|\theta)$$



1 / 1 分

2.

In EM algorithm, we maximize variational lower bound

$\mathcal{L}(q, \theta) = \log p(X|\theta) - \text{KL}(q||p)$ with respect to q (E-step) and θ (M-step) iteratively. Why is the maximization of lower bound on E-step equivalent to minimization of KL divergence?



Because uncomplete likelihood does not depend on $q(Z)$



正确

Revise [E-step details](#) video



Because we cannot maximize lower bound w.r.t. $q(Z)$



Because posterior becomes tractable



Because of Jensen's inequality



1 / 1 分

3.

Select correct statements about EM algorithm:



E-step can always be performed analytically



未选择的是正确的



M-step can always be performed analytically



未选择的是正确的

EM algorithm

测验, 4 个问题



EM algorithm always converges

正确

Revise [M-step details](#) video

4/4 分 (100%)



Complete likelihood is always a convex function as a function of parameters

未选择的是正确的



EM algorithm always converges to a global optimum

未选择的是正确的



1 / 1 分

4。

Consider $p(x) = \mathcal{N}(\mu, \sigma_1)$ and $q(x) = \mathcal{N}(\mu, \sigma_2)$. Calculate KL divergence between these two gaussians $KL(p||q)$ (hint: note that KL divergence is an expectation):



$$\log \frac{\sigma_2}{\sigma_1} - \frac{1}{2} + \frac{\sigma_1^2}{2\sigma_2^2}$$

正确

$$\begin{aligned} KL(p||q) &= \mathbb{E}_p \log \frac{\mathcal{N}(x|\mu, \sigma_1^2)}{\mathcal{N}(x|\mu, \sigma_2^2)} = \mathbb{E}_p \log \frac{(\sqrt{2\pi\sigma_1^2})^{-1} \exp\left(-\frac{(x-\mu)^2}{2\sigma_1^2}\right)}{(\sqrt{2\pi\sigma_2^2})^{-1} \exp\left(-\frac{(x-\mu)^2}{2\sigma_2^2}\right)} = \\ &= \mathbb{E}_p \left[\log \frac{\sigma_2}{\sigma_1} + \log \frac{\exp\left(-\frac{(x-\mu)^2}{2\sigma_1^2}\right)}{\exp\left(-\frac{(x-\mu)^2}{2\sigma_2^2}\right)} \right] = \mathbb{E}_p \left[\log \frac{\sigma_2}{\sigma_1} - \frac{(x-\mu)^2}{2\sigma_1^2} + \frac{(x-\mu)^2}{2\sigma_2^2} \right] = \\ &= \log \frac{\sigma_2}{\sigma_1} - \frac{\mathbb{E}_p(x-\mu)^2}{2\sigma_1^2} + \frac{\mathbb{E}_p(x-\mu)^2}{2\sigma_2^2} = \log \frac{\sigma_2}{\sigma_1} - \frac{\sigma_1^2}{2\sigma_1^2} + \frac{\sigma_1^2}{2\sigma_2^2} = \log \frac{\sigma_2}{\sigma_1} - \frac{1}{2} + \frac{\sigma_1^2}{2\sigma_2^2} \end{aligned}$$



$$\log \frac{\sigma_1}{\sigma_2} + \frac{\sigma_1^2 - \sigma_2^2}{\sigma_1^2 + \sigma_2^2}$$



$$\log \frac{\sigma_1}{\sigma_2} + \frac{\sigma_2^2}{\sigma_1^2}$$



$$\log \frac{\sigma_2^2}{\sigma_1^2} - \frac{\sigma_1^2}{2\sigma_2^2}$$

EM algorithm

4/4 分 (100%)

测验, 4 个问题

