ECE-302 PROJECT 3 EXTRA CREDIT

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March 28, 2021

Poisson Distribution

$$f(k) = \frac{\lambda^k e^{-\lambda}}{k!} \tag{1}$$

$$L(\lambda_1, \lambda_2) = \prod_{i=1}^n \frac{\lambda_1^{k_i} e^{-\lambda_1}}{k_i!} + \prod_{i=n+1}^N \frac{\lambda_2^{k_i} e^{-\lambda_2}}{k_i!}$$
(2)

$$= e^{-n\lambda_1} \prod_{i=1}^n \frac{\lambda_1^{k_i}}{k_i!} + e^{-n\lambda_2} \prod_{i=n+1}^N \frac{\lambda_2^{k_i}}{k_i!}$$
 (3)

$$LL(\lambda_{1}, \lambda_{2}) = -n\lambda_{1} + \sum_{i=1}^{n} k_{i} \ln \lambda_{1} - \sum_{i=1}^{n} \ln k_{i}!$$

$$-n\lambda_{2} + \sum_{i=n+1}^{N} k_{i} \ln \lambda_{2} - \sum_{i=n+1}^{N} \ln k_{i}!$$
(4)

Partial Derivatives:

$$LL'(\lambda_1) = -n + \sum_{i=1}^{n} \frac{k_i}{\lambda_1}$$
 (5)

$$LL'(\lambda_2) = -n + \sum_{i=n+1}^{N} \frac{k_i}{\lambda_2}$$
(6)

Maximizing log likelihood:

$$-n + \sum_{i=1}^{n} \frac{k_i}{\lambda_1} = 0 \tag{7}$$

$$\lambda_1 = \frac{1}{n} \sum_{i=1}^n k_i \tag{8}$$

$$-n + \sum_{i=n+1}^{N} \frac{k_i}{\lambda_2} = 0 \tag{9}$$

$$\lambda_2 = \frac{1}{n} \sum_{i=n+1}^{N} k_i \tag{10}$$