

Taller 2

1. $P_0 = 0$
 $K = 1, 2, 3, 4, 5$

a) $2x + 8y - z = 11$
 $5x - 12y + z = 10$
 $-x + y + 14z = 3$

Paso 1: despejar una variable de cada ecuación

$$x = \frac{11 + z - 8y}{2}$$

$$y = -\left[\frac{10 - z - 5x}{12}\right] \Rightarrow y = \frac{5x + z - 10}{12}$$

$$z = \frac{3 + x - y}{14}$$

Paso 2: $x^{(0)}$, $y^{(0)}$, $z^{(0)}$

Paso 3 $x^{(1)} = \frac{11 + z^{(0)} - 8y^{(0)}}{2} = \frac{11}{2}$

0 $y^{(1)} = \frac{5\left(\frac{11}{2}\right) + 0 - 10}{12} = \frac{35}{24}$

$$z^{(1)} = \frac{3 + x^{(0)} - y^{(0)}}{14} = \frac{3 + \frac{11}{2} - \frac{35}{24}}{14} = \frac{169}{336}$$

Paso 4: Repetir paso 3 hasta llegar a la aproximación deseada.

1 $x^{(2)} = \frac{11 + z^{(1)} - 8y^{(1)}}{2} = \frac{11 + \frac{169}{336} - 8\left(\frac{35}{24}\right)}{2} = \frac{-55}{672}$

$$y^{(2)} = \frac{5x^{(2)} + z^{(1)} - 10}{12} = \frac{5\left(\frac{-55}{672}\right) + \frac{169}{336} - 10}{12} = \frac{-317}{384}$$

$$z^{(2)} = \frac{3 + x^{(2)} - y^{(2)}}{14} = \frac{3 + \left(\frac{-55}{172}\right) - \left(\frac{-317}{389}\right)}{14} = 0.2674053997$$

$$x^{(3)} = \frac{11 + z^{(2)} - 8y^{(2)}}{2} = 8.73579$$

$$y^{(3)} = \frac{5x^{(3)} + z^{(2)} - 10}{12} = 2.91219$$

$$z^{(3)} = \frac{3 + x^{(3)} - 8y^{(3)}}{14} = 0.64959$$

$$x^{(4)} = \frac{11 + z^{(3)} - 8y^{(3)}}{2} = -5.81651$$

$$y^{(4)} = \frac{5x^{(4)} + z^{(3)} - 10}{12} = -3.20733$$

$$z^{(4)} = \frac{3 + x^{(4)} - 8y^{(4)}}{14} = 0.02970$$

$$x^{(5)} = \frac{11 + z^{(4)} - 8y^{(4)}}{2} = 18.34793$$

$$y^{(5)} = \frac{5x^{(5)} + z^{(4)} - 10}{12} = 6.81182$$

$$z^{(5)} = \frac{3 + x^{(5)} - 8y^{(5)}}{14} = 1.03794$$

$$x^{(6)} = \frac{11 + z^{(5)} - 8y^{(5)}}{2} = 21.72832$$

$$y^{(6)} = \frac{5x^{(6)} + z^{(5)} - 10}{12} = -9.59197$$

$$z^{(6)} = \frac{3 + 16x^{(6)} - 8y^{(6)}}{2} = -0.61686$$

$$2. a) 9A + 20B + 5C = 139'500'000$$

$$30A + 150B + 30C = 894'000'000$$

$$0.01A + 0.002B + 0.3C = 2'372'800$$

$$b) \begin{array}{ccc|c} 9 & 20 & 5 & 139'500'000 \\ 30 & 150 & 30 & 894'000'000 \\ 0.01 & 0.002 & 0.3 & 2'372'800 \end{array}$$

$$(E_2 - \frac{10}{3}E_1) \rightarrow$$

$$(E_3 - \frac{1}{900}E_1) \rightarrow$$

$$\begin{array}{ccc|c} 9 & 20 & 5 & 139'500'000 \\ 0 & 250/3 & 40/3 & 429'000'000 \\ 0 & -91/4500 & 53/180 & 221'7800 \end{array} \quad \begin{array}{l} \\ \\ (E_3 + \frac{91}{37500}E_2) \rightarrow \end{array}$$

$m_{32} = -\frac{91}{37500}$

$$\begin{array}{ccc|c} 9 & 20 & 5 & 139'500'000 \\ 0 & 250/3 & 40/3 & 429'000'000 \\ 0 & 0 & \frac{3721}{12500} & 2321904 \end{array}$$

$$c) C = \frac{2321904 \times 12500}{3721} = 7800000$$

$$B = \frac{3 \times 429'000'000 - 40/3C}{250} = 3'900'000$$

$$A = \frac{139'500'000 - 20B - 5C}{9} = 2'500'000$$

$$3. a) 15x - y + z = 12$$

$$2x + 8y - z = 11$$

$$-x + y + 4z = 3$$

Paso 1: Despejar una variable de cada ecuación

$$x = \frac{12 + y - z}{15}$$

$$y = \frac{11 + z - 2x}{8}$$

$$z = \frac{3 + x - y}{4}$$

$$x^{(0)} = (0, 0, 0)$$

$$x^{(1)} = \frac{12 + y^0 - z^0}{15} = \frac{12}{15}$$

$$z^{(1)} = \frac{3 + x^{(1)} - y^{(0)}}{4} = 0.65095$$

$$y^{(1)} = \frac{11 + z^0 - 2x^0}{8} = \frac{11}{8}$$

$$x^{(2)} = \frac{12 + y^{(1)} - z^{(1)}}{15} = 0.83956$$

$$z^{(2)} = \frac{3 + x^0 - y^0}{4} = \frac{3}{4}$$

$$y^{(2)} = \frac{11 + z^{(1)} - 2x^{(1)}}{8} = 1.24472$$

$$x^{(2)} = \frac{12 + y^{(1)} - z^{(1)}}{15} = 0.84167$$

$$z^{(3)} = \frac{3 + x^{(1)} - y^{(1)}}{4} = 0.64886$$

$$y^{(2)} = \frac{11 + z^0 - 2x^0}{8} = 1.25875$$

$$z^{(2)} = \frac{3 + x^{(1)} - y^{(1)}}{4} = 0.60625$$

$$x^{(3)} = \frac{12 + y^{(2)} - z^{(2)}}{15} = 0.84419$$

$$y^{(3)} = \frac{11 + z^{(2)} - 2x^{(2)}}{8} = 1.24036$$

$$z^{(3)} = \frac{3 + x^{(2)} - y^{(2)}}{4} = 0.64323$$

$$x^{(4)} = \frac{12 + y^{(3)} - z^{(3)}}{15} = 0.83981$$

$$y^{(4)} = \frac{11 + z^{(3)} - 2x^{(3)}}{8} = 1.24436$$

4. a) Demostrar $\vec{x} \cdot \vec{y} = 0$

$$\cos \theta = \frac{\vec{x} \cdot \vec{y}}{|\vec{x}| |\vec{y}|}$$

Si $\vec{x} \cdot \vec{y}$ son ortogonales, entonces $\theta = \frac{\pi}{2}$

$$\cos \frac{\pi}{2} = \frac{\vec{x} \cdot \vec{y}}{|\vec{x}| |\vec{y}|} \rightarrow 0 = \frac{\vec{x} \cdot \vec{y}}{|\vec{x}| |\vec{y}|} \rightarrow 0 = \vec{x} \cdot \vec{y}$$

$$\text{si } \vec{x} \cdot \vec{y} = 0$$

$$\frac{\cos \theta = 0}{|\vec{x}| |\vec{y}|} \rightarrow \cos \theta = 0 \quad (0 \leq \theta \leq 180^\circ)$$

$$\theta = \frac{\pi}{2}$$

b) Buscar dos vectores diferentes \vec{y} y \vec{z} que sean ortogonales a $\vec{x} = (4, -7, 5, 9)$

$$\bullet (4, -7, 5, 9) \cdot (a, b, c, d) = 0 \quad \vec{y} = (1, 2, 3, 5/9) \checkmark$$

$$4a - 7b + 5c + 9d = 0$$

$$\text{Si } a=1, b=2 \text{ y } c=3$$

$$4 - 14 + 15 + 9d = 0$$

$$9d = -5$$

$$d = -5/9$$

$$\text{Si } a=1, b=2 \text{ y } d=3$$

$$4 - 14 + 5c + 27 = 0$$

$$5c = 19$$

$$c = \frac{19}{5}$$

$$\vec{x} \cdot \vec{y} = 4 \cdot 1 + (-7 \cdot 2) + 5 \cdot 3 + 9 \cdot \frac{5}{9} = 0$$

$$\vec{z} = (1, 2, -\frac{19}{5}, 3) \checkmark$$

$$\vec{x} \cdot \vec{z} = 4 \cdot 1 + (-7 \cdot 2) + 5 \left(-\frac{19}{5}\right) + 9 \cdot 3$$

$$\vec{x} \cdot \vec{z} = 0$$

$$\bullet \vec{x} = (6, 2, -3, -3) \rightarrow$$

$$\text{Si } a=1, b=2 \text{ y } c=3$$

$$6 + 4 - 9 - 3d = 0$$

$$-3d = -1$$

$$d = \frac{1}{3}$$

$$\vec{y} = (1, 1, 3, \frac{1}{3}) \checkmark$$

$$(6, 2, -3, -3) \cdot (a, b, c, d) = 6a + 2b - 3c - 3d$$

$$\vec{x} \cdot \vec{y} = 6 \cdot 1 + 2 \cdot 2 + (-3 \cdot 3) + (-3 \cdot \frac{1}{3}) = 0$$

5. $b=1, c=2, y=3, z=3$ $\vec{z} = (\frac{13}{6}, 1, 2, 3) \checkmark$

$-6a + 2b - 6c - 9d = 0$

$6a = \frac{13}{6}$
 $a = \frac{13}{36}$

$\vec{x} \cdot \vec{z} = \left[6 \cdot \frac{13}{6}\right] + 2 \cdot 1 + (-3 \cdot 2) + (-3 \cdot 3)$

$\vec{x} \cdot \vec{z} = 0$

5. a) $T + C + R + A = 700$

$T + 2C = 0.3R \rightarrow T + 2C - 0.3R = 0$

$0.1T + 0.3C + 0.34R + 0.4A = 480$

$C + 985 = 2R + 0.35A$

$T + C + R + A = 700$

$T + 2C - 0.3R = 0$

$0.1T + 0.3C + 0.34R + 0.4A = 480$

$C - 2R - 0.35A = -985$

$AX = \begin{bmatrix} 1 & 1 & 1 & 1 & 1 \\ 1 & 2 & -0.3 & 0 & 0 \\ 0.1 & 0.3 & 0.34 & 0.4 & \\ 0 & 1 & -2 & -0.35 & \end{bmatrix} B = \begin{bmatrix} 700 \\ 0 \\ 480 \\ -985 \end{bmatrix}$

b) $\begin{bmatrix} 1_{11} & 0 & 0 & 0 \\ 1_{21} & 1_{22} & 0 & 0 \\ 1_{31} & 1_{32} & 1_{33} & 0 \\ 1_{41} & 1_{42} & 1_{43} & 1_{44} \end{bmatrix} \begin{bmatrix} U_{11} & U_{12} & U_{13} & U_{14} \\ 0 & U_{22} & U_{23} & U_{24} \\ 0 & 0 & U_{33} & U_{34} \\ 0 & 0 & 0 & U_{44} \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & -0.3 & 0 \\ 0.1 & 0.3 & 0.34 & 0.4 \\ 0 & 1 & -2 & -0.35 \end{bmatrix}$

$$L_{11} U_{11} = 1 \rightarrow U_{11} = 1 \quad y \quad U_{12} = 1$$

$$L_{12} U_{12} = 1 \rightarrow U_{12} = 1$$

$$L_{13} U_{13} = 1 \rightarrow U_{13} = 1$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ L_{21} & L_{22} & 0 & 0 \\ L_{31} & L_{32} & L_{33} & 0 \\ L_{41} & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & U_{22} & U_{23} & U_{24} \\ 0 & 0 & U_{33} & U_{34} \\ 0 & 0 & 0 & U_{44} \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & -0.3 & 0 \\ 0.1 & 0.3 & 0.84 & 0.4 \\ 0 & 1 & -2 & -0.36 \end{bmatrix}$$

$$L_{21} U_{11} = 1 \quad y \quad L_{31} U_{11} = 0.1 \quad y \quad L_{41} U_{11} = 0$$

$$L_{21} = 1 \quad L_{31} = 0.1 \quad y \quad L_{41} = 0$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & L_{22} & 0 & 0 \\ 0.1 & L_{32} & L_{33} & 0 \\ 0 & L_{42} & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & U_{22} & U_{23} & U_{24} \\ 0 & 0 & U_{33} & U_{34} \\ 0 & 0 & 0 & U_{44} \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & -0.3 & 0 \\ 0.1 & 0.3 & 0.84 & 0.4 \\ 0 & 1 & -2 & -0.36 \end{bmatrix}$$

Ahora, para a_{22}

$$L_{21} U_{12} + L_{22} U_{22} = a_{22} \quad si \quad L_{22} = 1$$

$$1 + L_{22} U_{22} = 2 \rightarrow U_{22} = 1$$

$$L_{31} U_{12} + L_{32} U_{22} = 0.3$$

$$0.1 + L_{32} = 0.3 \rightarrow L_{32} = 0.2$$

$$L_{21} U_{13} + L_{22} U_{23} = 0$$

$$L_{21} U_{13} + L_{22} U_{23} = -0.3$$

$$1 + U_{23} = -0.3$$

$$U_{23} = -0.3 - 1$$

$$U_{23} = -1.3$$

$$L_{21}U_{12} + L_{22}U_{22} = 1$$

$$0 + L_{22} = 1 \rightarrow L_{22} = 1$$

$$L_{21}U_{14} + L_{22}U_{24} = 0.84$$

$$0 + U_{24} = 0.84$$

$$U_{24} = 0.84$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0.1 & 0.2 & 1 & 0 \\ 0 & 1 & L_{43} & L_{44} \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 1 & -1.3 & -1 \\ 0 & 0 & U_{33} & U_{34} \\ 0 & 0 & 0 & U_{44} \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & -0.3 & 0 \\ 0.1 & 0.2 & 0.84 & 0.4 \\ 0 & 1 & -2 & -0.3 \end{bmatrix}$$

$$L_{31}U_{13} + L_{32}U_{23} + L_{33}U_{33} = 0.84$$

$$S_i \quad L_{33} = 1$$

$$0.1 + 0.2(-1.3) + U_{33} = 0.84$$

$$U_{33} = 0.84 + 0.16 = 1$$

$$L_{31}U_{14} + L_{32}U_{24} + L_{33}U_{34} = 0.4$$

$$0.1 + -0.2 \quad U_{34} = 0.4$$

$$-1.3 \quad U_{34} = 0.5$$

$$L_{34} = -0.1$$

$$L_{41}U_{12} + L_{42}U_{22} + L_{43}U_{32} = -2$$

$$0 - 1.3 + L_{43} = -2 \rightarrow L_{43} = -2 + 1.3 = -0.9$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0.1 & 0.2 & 1 & 0 \\ 0 & 1 & -0.9 & L_{44} \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 1 & -1.3 & -1 \\ 0 & 0 & 1 & 0.5 \\ 0 & 0 & -0.9 & U_{44} \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & -0.3 & 0 \\ 0.1 & 0.2 & 0.84 & 0.4 \\ 0 & 1 & -2 & -0.3 \end{bmatrix}$$

$$L_{41}U_{14} + L_{42}U_{24} + L_{43}U_{34} + L_{44}U_{44} = -0.35$$

$$0 + -1 - 0.35 + L_{44} = -0.35$$

$$L_{44}U_{44} = -0.35$$

$$+ L_{44} = -0.35$$

$$L_{44} = -0.35 + 0.35 + 1$$

$$L_{44} = 1$$

$$S_i \quad L_{44} = 1$$

$$\left[\begin{array}{cccc|cccc} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & -1.3 & -1 \\ 0.1 & 0.2 & 1 & 0 & 0 & 0 & 1 & 0.5 \\ 0 & 1 & -0.9 & 1 & 0 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[\begin{array}{cccc|cccc} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 1 & -0.9 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & -0.9 & 0 & 0 & 1 & 0.5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array} \right]$$

c) $By = b$

$$T = 700$$

$$T = 700$$

$$C = -900$$

$$T + C = 0$$

$$0.1(700) + 0.2(-900) + D = 480$$

$$0.1T + 0.2C + R = 480$$

$$R = 480 - 70 + 140$$

$$R = 550$$

$$C - 0.9R + A = -985$$

$$-900 - 0.9(550) + A = -985$$

$$A = -985 + 900 + 385$$

$$A = 100$$

$$y = \{ 700, -900, 550, 100 \}$$

$$UX = y$$

$$T + C + R + A = 700$$

$$A = 100$$

$$C - 1.3R - A = -900$$

$$R = 550 - 50$$

$$R = 500$$

$$R + 0.5A = 550$$

$$C = 1.3(500) - 100 = -900$$

$$C = -900 + 100 + 650$$

$$C = 50$$

$$A = 100$$

$$T + 50 + 500 + 100 = 700$$

$$T = 50$$

$$6. \quad A = \begin{bmatrix} -5 & 6 & 10 & 12 \\ 15 & 3 & 28 & 1 \\ 10 & -12 & -20 & -24 \end{bmatrix} \quad B = \begin{bmatrix} 7 & -6 & 3 \\ -6 & 2 & 11 \\ 10 & -12 & -20 \\ 6 & 17 & 3 \end{bmatrix}$$

$$C = \begin{bmatrix} 14 & 8 & 1 \\ 5 & 4 & 1 \\ 2 & 25 & 6 \end{bmatrix}$$

a) Determinant $AB + C \rightarrow AB + C$

$$AB = 3 \times 3 \quad A = 3 \times 4 \quad B = 4 \times 3$$

$$\boxed{\quad} = \boxed{\quad}$$

$$C_{11} = A_{11}B_{11} + A_{12}B_{21} + A_{13}B_{31} + A_{14}B_{41} =$$

$$C_{11} = -5 \cdot 7 + 6 \cdot (-6) + 10 \cdot 10 + 12 \cdot 6 = 101$$

$$C_{12} = A_{11}B_{12} + A_{12}B_{22} + A_{13}B_{32} + A_{14}B_{42}$$

$$C_{12} = -5 \cdot (-6) + 6 \cdot 2 + 10 \cdot (-12) + 12 \cdot 17 = 132$$

$$C_{13} = A_{11}B_{13} + A_{12}B_{23} + A_{13}B_{33} + A_{14}B_{43}$$

$$C_{13} = -5 \cdot 3 + 6 \cdot 11 + 10 \cdot (-20) + 12 \cdot 3 = -118$$

$$C_{21} = A_{21}B_{11} + A_{22}B_{21} + A_{23}B_{31} + A_{24}B_{41}$$

$$C_{21} = 15 \cdot 7 + 3 \cdot (-6) + 28 \cdot 10 + 1 \cdot 6 = 373$$

$$C_{22} = A_{21}B_{12} + A_{22}B_{22} + A_{23}B_{32} + A_{24}B_{42}$$

$$C_{22} = 15 \cdot (-6) + 3 \cdot 2 + 28 \cdot (-12) + 1 \cdot 17 = -400$$

$$C_{23} = A_{21}B_{13} + A_{22}B_{23} + A_{23}B_{33} + A_{24}B_{43}$$

$$C_{23} = 15 \cdot 3 + 3 \cdot 11 + 28 \cdot (-20) + 1 \cdot 3 = -749$$

$$C_{31} = A_{31}B_{11} + A_{32}B_{21} + A_{33}B_{31} + A_{34}B_{41}$$

$$C_{31} = 10 \cdot 7 + (-12) \cdot (-6) + (-20) \cdot 10 + (-24) \cdot 6 = -202$$

$$C_{32} = A_{31}B_{12} + A_{32}B_{22} + A_{33}B_{32} + A_{34}B_{42}$$

$$C_{32} = 10 \cdot (-6) + (-12) \cdot 2 + (-20) \cdot (-12) + (-24) \cdot 17 = -764$$

$$C_{33} = A_{31}B_{13} + A_{32}B_{23} + A_{33}B_{33} + A_{34}B_{43}$$

$$C_{33} = 10 \cdot 3 + (-12) \cdot 11 + (-20) \cdot (-20) + (-24) \cdot 3 = 236$$

$$C_{33} = B_{31}A_{13} + B_{32}A_{23} + B_{33}A_{33}$$

$$C_{33} = 10 \cdot 10 + (-12) \cdot 28 + (-20) \cdot (-70) = 164$$

$$C_{34} = B_{31}A_{14} + B_{32}A_{24} + B_{33}A_{34}$$

$$C_{34} = 10 \cdot 12 + (-12) \cdot 1 + (-20) \cdot (-74) = 581$$

$$C_{41} = B_{41}A_{11} + B_{42}A_{21} + B_{43}A_{31}$$

$$C_{41} = 6 \cdot (-5) + 17 \cdot 15 + 3 \cdot 10 = 255$$

$$C_{42} = B_{41}A_{12} + B_{42}A_{22} + B_{43}A_{32}$$

$$C_{42} = 6 \cdot 6 + 17 \cdot 3 + 3 \cdot (-12) = 61$$

$$C_{43} = B_{41}A_{13} + B_{42}A_{23} + B_{43}A_{33}$$

$$C_{43} = 6 \cdot 10 + 17 \cdot 28 + 3 \cdot (-20) = 476$$

$$C_{44} = B_{41}A_{14} + B_{42}A_{24} + B_{43}A_{34}$$

$$C_{44} = 6 \cdot 12 + 17 \cdot 1 + 3 \cdot (-74) = 17$$

$$BA = \begin{bmatrix} -95 & -12 & -158 & -6 \\ 170 & -162 & -224 & -334 \\ -430 & 264 & 164 & -528 \\ 255 & 61 & 476 & 17 \end{bmatrix}$$

c) $CA = 3 \times 4$ $C = 3 \times 3$ $A = 3 \times 4$

$$D_{11} = C_{11}A_{11} + C_{12}A_{21} + C_{13}A_{31}$$

$$D_{11} = 14 \cdot (-5) + 8 \cdot 15 + 1 \cdot 10 = 60$$

$$D_{12} = C_{11}A_{12} + C_{12}A_{22} + C_{13}A_{32}$$

$$D_{12} = 14 \cdot 6 + 8 \cdot 3 + 1 \cdot (-12) = 76$$

$$D_{13} = C_{11}A_{13} + C_{12}A_{23} + C_{13}A_{33}$$

$$D_{13} = 14 \cdot 10 + 8 \cdot 28 + 1 \cdot (-20) = 344$$

$$D_{14} = C_{11}A_{14} + C_{12}A_{24} + C_{13}A_{34}$$

$$D_{14} = 14 \cdot 12 + 8 \cdot 1 + 1 \cdot (-74) = 152$$

$$D_{21} = C_{21}A_{11} + C_{22}A_{21} + C_{23}A_{31}$$

$$D_{21} = 5 \cdot (-5) + 4 \cdot 15 + 1 \cdot 10 = 45$$

$$D_{22} = C_{21}A_{12} + C_{22}A_{22} + C_{23}A_{32}$$

$$D_{22} = 5 \cdot 6 + 4 \cdot 3 + 1 \cdot (-12) = 30$$

$$D_{23} = C_{21}A_{13} + C_{22}A_{23} + C_{23}A_{33}$$

$$D_{23} = 5 \cdot 10 + 4 \cdot 28 + 1 \cdot 10 = 142$$

$$D_{24} = C_{21}A_{14} + C_{22}A_{24} + C_{23}A_{34}$$

$$D_{24} = 5 \cdot 12 + 4 \cdot 1 + 1 \cdot 12 = 60$$

$$D_{31} = C_{31}A_{11} + C_{32}A_{21} + C_{33}A_{31}$$

$$D_{31} = 2 \cdot -5 + 25 \cdot 15 + 6 \cdot 10 = 425$$

$$D_{32} = C_{31}A_{12} + C_{32}A_{22} + C_{33}A_{32}$$

$$D_{32} = 2 \cdot 6 + 25 \cdot 3 + 6 \cdot -12 = 15$$

$$D_{33} = C_{31}A_{13} + C_{32}A_{23} + C_{33}A_{33}$$

$$D_{33} = 2 \cdot 10 + 25 \cdot 28 + 6 \cdot -70 = 600$$

$$D_{34} = C_{31}A_{14} + C_{32}A_{24} + C_{33}A_{34}$$

$$D_{34} = 2 \cdot 12 + 25 \cdot 1 + 6 \cdot -24 = -95$$

$$CA = \begin{bmatrix} 60 & 96 & 344 & 152 \\ 45 & 30 & 142 & 40 \\ 425 & 15 & 600 & -95 \end{bmatrix}$$

c) Tanto A como B no cumplen que m y n sean iguales por lo tanto no es posible hallar determinante.

Determinante de C

$$C = \begin{bmatrix} 14 & 8 & 1 \\ 5 & 4 & 1 \\ 2 & 25 & 6 \end{bmatrix}$$

$$14 \det \begin{bmatrix} 4 & 1 \\ 25 & 6 \end{bmatrix} - 8 \det \begin{bmatrix} 5 & 1 \\ 2 & 6 \end{bmatrix} + 1 \det \begin{bmatrix} 5 & 4 \\ 2 & 25 \end{bmatrix}$$

$$14(4 \cdot 6 - 25 \cdot 1) - 8(5 \cdot 6 - 2) + (5 \cdot 25 - 2 \cdot 4) = -121$$