

Statistical Inference Project Part 1

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Overview

This project investigates the exponential distribution of R and applies The Central Limit Theorem to a thousand mean simulations.

Exponential distribution is simulated in R using `rexp(n, lambda)`. Lambda is the rate parameter. The mean of exponential distribution is $1/\lambda$. The standard deviation is $1/\lambda$.

Instructions provided are as follows.

$\lambda = .2$ for all simulations Investigate the distribution of averages of 40 exponentials Do 1,000 simulations

Simulations Explanation

This code sets the parameters as an outline

```
# set seed for reproducibility
set.seed(123)

# set sampling values as mandated in the instructions

#lambda
lambda <- 0.2

# number of exponentials
n <- 40

# number of simulations
run_sim <- 1000

# Run simulations

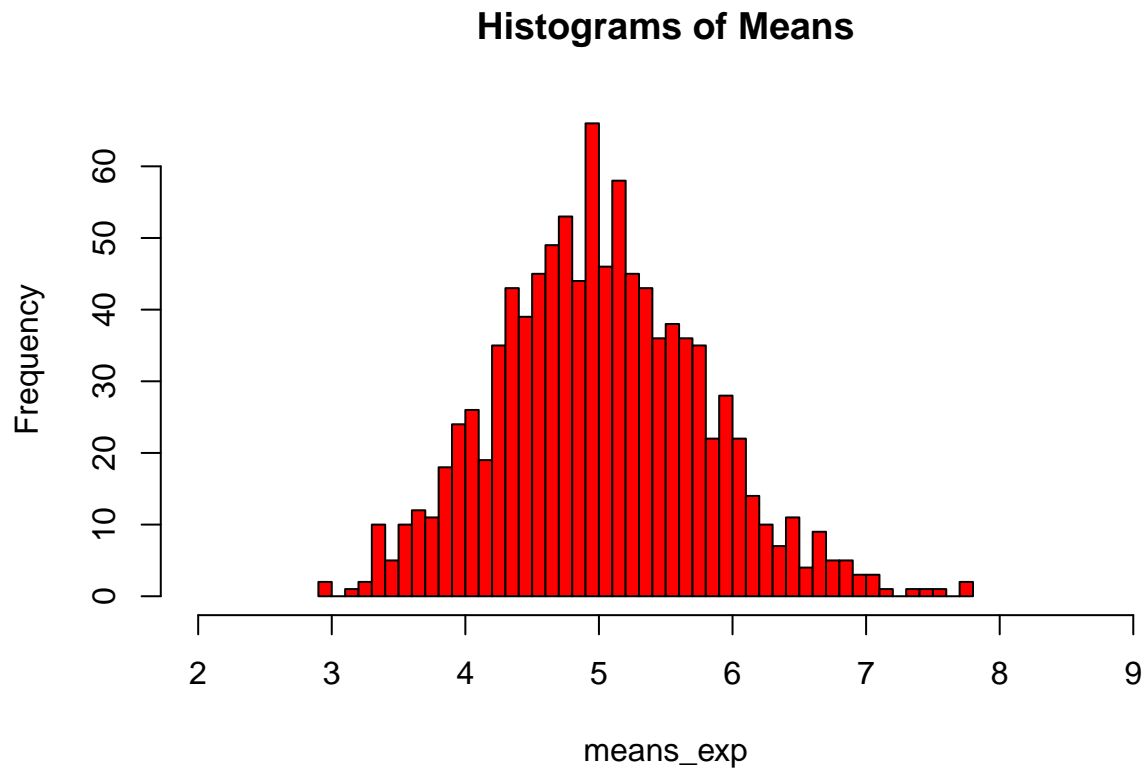
run_sim<- replicate(run_sim,rexp(n,lambda))

# Calculate the mean of the exponential simulations

means_exp<- apply(run_sim,2,mean)

#Histogram of the means

hist(means_exp, breaks=40, xlim = c(2,9), main="Histograms of Means", col = "red")
```



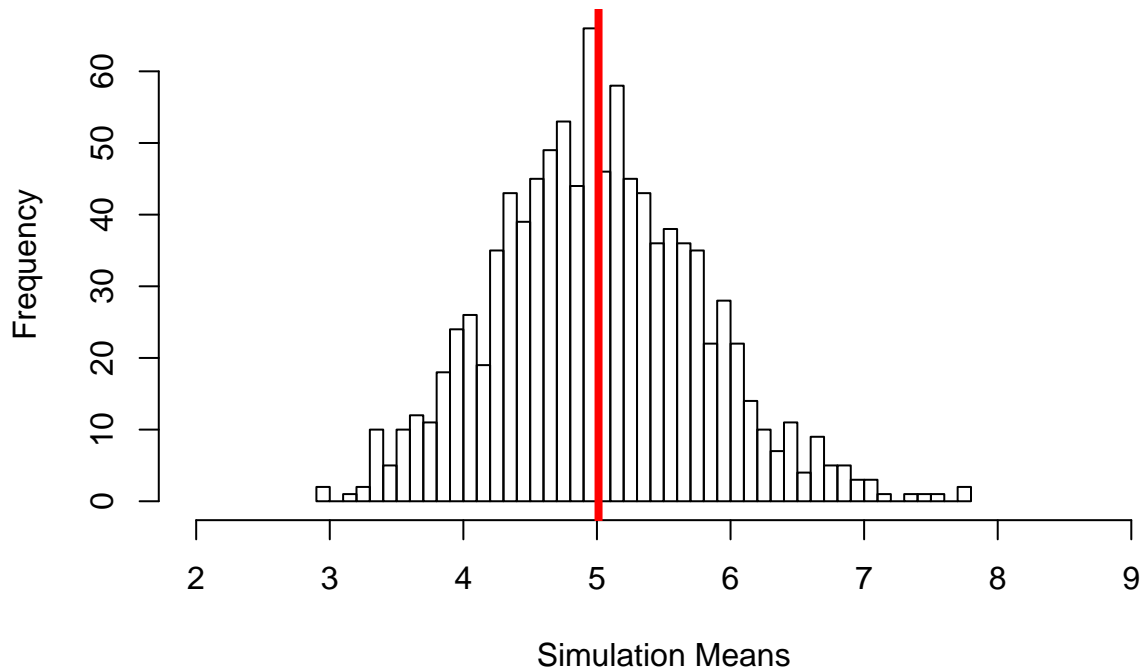
Sample Mean vs Theoretical Mean

The exponential distribution mean is equal to $1/\lambda$. For this simulation, λ is 0.2. The theoretical mean is 5.

```
# plot histogram of the sample means
hist(means_exp, main = "Sample Mean vs Theoretical Mean", xlim = c(2,9), breaks = 40, xlab = "Simulation", col = "red", lwd = 2)

# plot vertical blue line at mean of samples
abline(v = mean(means_exp), lwd = "4", col = "red")
```

Sample Mean vs Theoretical Mean



```
# calculate the sample mean  
mean(means_exp)
```

```
## [1] 5.011911
```

```
## [1] 5.011911
```

The sample mean of 5.011911 is close to the theoretical mean of 5

Sample Variance vs Theoretical Variance

The standard deviation of the exponential distribution is $(1/\lambda) / \sqrt{n}$.

```
# theoretical variance vs simulated variance  
print(paste("Theoretical variance is: ", round((1/lambda)^2/n, 3)))
```

```
## [1] "Theoretical variance is: 0.625"
```

```
print(paste("Actual variance is: ", round(var(means_exp), 3)))
```

```
## [1] "Actual variance is: 0.6"
```

The actual variance is slightly lower than the theoretical variance.

Distribution

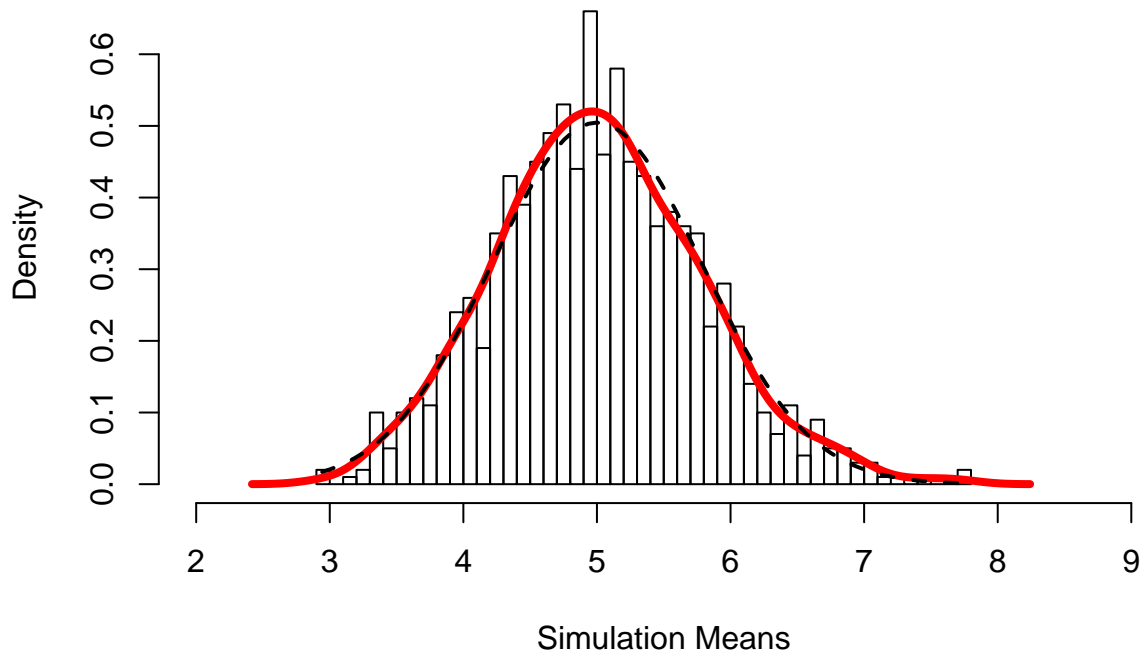
The histogram below shows whether the exponential distribution is approximately normal. Due to the Central Limit Theorem, the means of the sample simulations should follow a normal distribution.

```
# Histogram with distribution curve  
hist(means_exp, prob=TRUE, main = "Mean of Exponential Function Sim", breaks = 40, xlim = c(2,9), xlab = "Simulation Means", ylab = "Density")
```

```
lines(density(means_exp), lwd=4, col="red")

# Normal distribution line
x <- seq(min(means_exp), max(means_exp), length = 2*n)
y <- dnorm(x, mean = 1/lambda, sd = sqrt(((1/lambda)/sqrt(n))^2))
lines(x,y, pch = 20, lwd = 2, lty = 2)
```

Mean of Exponential Function Sim



The histogram above shows the calculated distribution of means of the simulated exponential distributions. The distribution is approximately normal because of the Central Limit Theorem. If the number of samples increases, the distribution would be closer to the standard normal distribution.