

R(ABCD)

AB \rightarrow CD ✓

~~D~~ \rightarrow B

Key: AB, AD

AD⁺ = ADABC

Normal form

BCNF: No.

3NF: Yes

D⁺ = DB

R1(DB) \longleftrightarrow R2(ACD)

F1

D \rightarrow B

D⁺ DB

F2

~~AB~~

AB \rightarrow C

AB \Rightarrow D

①

$R \cap R_2 \Rightarrow D$

$\rightarrow R_1 - R_2$

$\rightarrow R_2 - R_1$

$R(ABCDE)$

$\left\{ \begin{array}{l} \underline{AB} \rightarrow C \checkmark \\ \underline{C} \rightarrow \underline{DE} \checkmark \end{array} \right.$

NF: 2NF \checkmark

3

$AB^+ = R_1(ABC)$

$C^+ = R_2(CDE)$

BCNF

~~3NF~~
~~1~~

$\underline{C^+} = CDE$

$R_1(\underline{CDE})$

F1 $C \rightarrow DE$
BCNF \checkmark

$R_2(ABC)$

F2 $AB \rightarrow C$

BCNF: \checkmark

R(AB CDEF)

Key: AF

~~A~~ → B ~~6~~
A → C
→ C → D ~~6~~
C → E

BCNF: NO

3NF: NO

2NF: NO.

$C^+ = CDE$

R1(CDE) F1

Key: C

BCNF: ✓

C → D

C → E

~~R2(ABDEF C)~~ F2

Key: AF

R21(ABC)

Key: A

BCNF

F21

(A → B
A → C

A → B

A → C

$A^+ = ABCE$

R22(FA)

F22 BCNF

✓ ① loss less ness

R , F

$$(\cancel{x_1}) \underline{R_1} \times \overset{x_2}{(\cancel{R_2})} = R$$

R1

R2

✓ ② Attribute preserving

R1 \cup R2

③ FD preserving

F₁ \cup F₂
 \equiv F

1. R(ABCDEF), and FDs

$A \rightarrow B$

$B \rightarrow CDE$

$E \rightarrow F$

Key: $\underline{A}^+ = ABCDEF$

BCNF: NO
3NF: NO
2NF: Yes

$\underline{A} \rightarrow B$
 $B \rightarrow C$
 $B \rightarrow D$
 $B \rightarrow E$
 $E \rightarrow F$

$A^+ = AB$

$B^+ = BCDE$

$E^+ = EF$

$R_1(\underline{A}B)$ BCNF
 $R_2(\underline{B}CDE)$ BCNF
 $R_3(\underline{E}F)$ BCNF
3NF

F1

$A \rightarrow B$

F2

$B \rightarrow C$
 $B \rightarrow D$
 $B \rightarrow E$

F3

$E \rightarrow F$

1. R(ABCDEF), and FDs

$A \rightarrow B$

$B \rightarrow CDE$

$E \rightarrow F$

Key: A

$C \rightarrow D$

$A \rightarrow B$

$B \rightarrow C$

~~$B \rightarrow D$~~

$B \rightarrow E$

$E \rightarrow F$

$C \rightarrow D$

$R_1(\underline{A}B)$

$R_2(\underline{B}CE)$

$R_3(\underline{E}F)$

$R_4(\underline{C}D)$

$F_1 \quad A \rightarrow B$

$F_2 \quad B \rightarrow C$

$B \rightarrow E$

F_3

$E \rightarrow F$

F_4

$C \rightarrow D$

\uparrow $R(ABCDEF)$

$AB \rightarrow C$

$C \rightarrow DEFA$

\Downarrow

$AB \rightarrow C$

$C \rightarrow D$

$C \rightarrow E$

$C \rightarrow F$

$C \rightarrow A$

$R1(\underline{ABC})$

Key: AB. BCNF: NO
3NF: Yes

$R2(\underline{C}DEFA)$

C

BCNF: Yes

F1

$AB \rightarrow C$

$C \rightarrow A$

$C \rightarrow D$

$C \rightarrow E$

$C \rightarrow F$

$C \rightarrow A$

F2

$R(AB C D E F)$

$AB \rightarrow C$

$C \rightarrow D E F A$

H

$AB \rightarrow C$

$C \rightarrow D$

$C \rightarrow E$

$C \rightarrow F$

$C \rightarrow A$

Key: AB

$C^+ C D E F A$ F1

$R1(C D E F A)$

C BCNF

$C \rightarrow D$

$C \rightarrow E$

$C \rightarrow F$

$C \rightarrow A$

$R2(BC)$

Key: BC

BCNF

F2: Null
 \emptyset

~~$AB \rightarrow C$~~

3. $R(\text{CourseNo}, \text{Sem}, \text{AcadYear}, \text{InstructorID}, \text{StudentID}, \text{Grade})$
 $\{\text{CourseNo}, \text{Sem}, \text{AcadYear}\} \rightarrow \text{InstructorID}$
 $\{\text{CourseNo}, \text{Sem}, \text{AcadYear}, \text{StudentID}\} \rightarrow \text{Grade}$