# **Priority Queues**

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- Eager Priority Queue.
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# **Abstract Priority Queue**

Source: AbstractPriorityQueue.java

```
public abstract class AbstractPriorityQueue<T extends Comparable<T>> {
    protected Comparator<T> comparator;

public AbstractPriorityQueue(Comparator<T> comparator) {
    this.comparator = comparator;
}
```

- Class types: class vs. abstract class vs. interface.
- Generics: <T extends Comparable<T>>.
- Interface in generics: Comparable.
- Member types: private VS. package VS. protected VS. public.
- Constructor: this.

```
/**
 * Adds a comparable key to this queue.
 * @param key the comparable key.
abstract public void add(T key);
/**
 * Removes the key with the highest priority if exists.
 * @return the key with the highest priority if exists; otherwise, {@code null}.
abstract public T remove();
/** @return the size of this queue. */
abstract public int size();
/** @return {@code true} if the queue is empty; otherwise, {@code false}. */
public boolean isEmpty() {
    return size() == 0;
```

- Abstract methods: add(), remove(), size().
- Regular method in abstract class: isEmpty().
- Javadoc.

# **Lazy Priority Queue**

Source: LazyPriorityQueue.java

```
public class LazyPriorityQueue<T extends Comparable<T>> extends AbstractPriorityQueue<T> {
    private List<T> keys;

    public LazyPriorityQueue(Comparator<T> comparator) {
        super(comparator);
        keys = new ArrayList<>();
    }

    public LazyPriorityQueue() {
        this(Comparator.naturalOrder());
    }
}
```

- Class inheritance: extends AbstractPriorityQueue<T>.
- Constructors: default vs. parameters, this vs. super.

```
/**
 * Adds a key to the back of the list.
 * @param key the comparable key.
@Override
public void add(T key) { keys.add(key); }
/**
 * Finds the key with the highest priority, and removes it from the list.
 * @return the key with the highest priority if exists; otherwise, {@code null}.
@Override
public T remove() {
    if (isEmpty()) return null;
    T max = Collections.max(keys, comparator);
    keys.remove(max);
    return max;
@Override
public int size() { return keys.size(); }
```

- Annotation: @Override.
- Edge case handling: remove().
- Base API: Collections.max().
- Complexity: add(), remove().

# **Eager Priority Queue**

Source: EagerPriorityQueue.java

```
/**
 * Adds a key to the list according to the priority.
 * @param key the comparable key.
@Override
public void add(T key) {
    int index = Collections.binarySearch(keys, key, comparator);
    if (index < 0) index = -(index + 1);
    keys.add(index, key);
 * Remove the last kev in the list.
 * @return the key with the highest priority if exists; otherwise, {@code null}.
@Override
public T remove() {
    return isEmpty() ? null : keys.remove(keys.size() - 1);
```

- Base API: Collections.binarySearch().
- Ternary conditional operator: condition ? : .
- Complexity: add(), remove().

# **Binary Heap**

### What is a heap?

- A tree where each node has a higher (or equal) priority than its children.
- The tree must be balanced at all time.
- What is a binary heap?

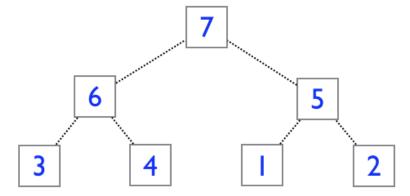
## **Operations**

- Add: swim.
- Remove: sink.
- Both operations can be done in  $O(\log n)$ .

# Representation

- Binary heap can be represented by a list.
- Index of the parent: k/2.
- ullet Index of the children: k\*2 and (k\*2)+1.





#### Source: BinaryHeap.java

```
public class BinaryHeap<T extends Comparable<T>> extends AbstractPriorityQueue<T> {
    private List<T> keys;

    public BinaryHeap(Comparator<T> comparator) {
        super(comparator);
        keys = new ArrayList<>();
        keys.add(null); // initialize the first item as null
    }

    public BinaryHeap() {
        this(Comparator.naturalOrder());
    }

    @Override
    public int size() {
        return keys.size() - 1;
    }
}
```

Handle the null key at the front.

```
@Override
public void add(T key) {
    keys.add(key);
    swim(size());
}

private void swim(int k) {
    while (1 < k && comparator.compare(keys.get(k / 2), keys.get(k)) < 0) {
        Collections.swap(keys, k / 2, k);
        k /= 2;
    }
}</pre>
```

- Add each key to the end of the list and swim.
- comparator.compare(): compare itself to its parent.
- Base API: Collections.swap().

```
@Override
public T remove() {
    if (isEmpty()) return null;
    Collections.swap(keys, 1, size());
    T max = keys.remove(size());
    sink(1);
    return max;
}

private void sink(int k) {
    for (int i = k * 2; i <= size(); k = i, i *= 2) {
        if (i < size() && comparator.compare(keys.get(i), keys.get(i + 1)) < 0) i++;
        if (comparator.compare(keys.get(k), keys.get(i)) >= 0) break;
        Collections.swap(keys, k, i);
    }
}
```

- Replace the root with the last key in the list and sink.
- Compare two children.
- Compare itself to the greater child.

# **Unit Tests**

Source: PriorityQueueTest.java

### Accuracy

```
* @param q a priority queue.
* @param c a comparator used for sorting.
* @param keys a list of comparable keys.
private <T extends Comparable<T>>void testAccuracy(AbstractPriorityQueue<T> q, Comparator<T> c, List<T> keys) {
    keys.forEach(q::add);
    keys.sort(c);
    keys.forEach(key -> assertEquals(key, g.remove()));
}
@Test
public void testAccuracy() {
   testAccuracy(new LazyPriorityQueue<>(), Comparator.reverseOrder());
   testAccuracy(new EagerPriorityQueue<>(), Comparator.reverseOrder());
   testAccuracy(new BinaryHeap<>(), Comparator.reverseOrder());
   testAccuracy(new LazyPriorityQueue<Integer>(Comparator.reverseOrder()), Comparator.naturalOrder());
   testAccuracy(new EagerPriorityQueue<Integer>(Comparator.reverseOrder()), Comparator.naturalOrder());
   testAccuracy(new BinaryHeap<Integer>(Comparator.reverseOrder()), Comparator.naturalOrder());
}
```

- Generics on method.
- Lambda expression: Iterable.forEach().
- Annotation: @Test .

### **Speed**

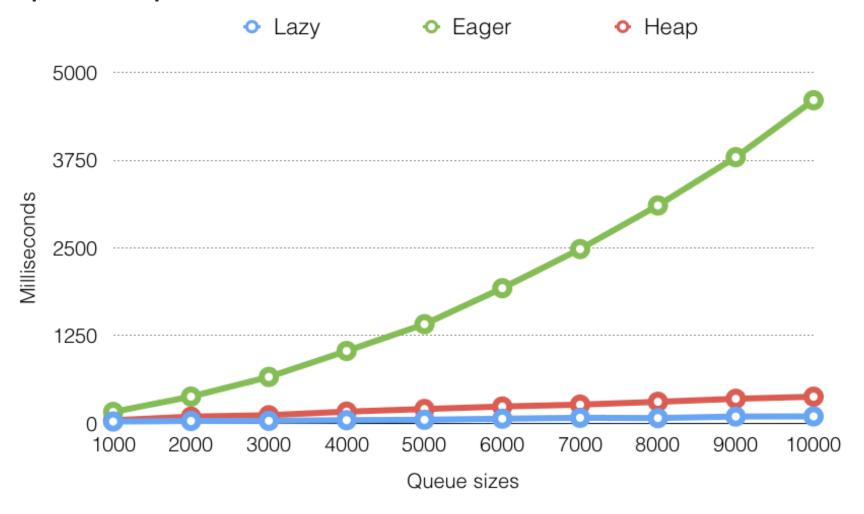
```
private class Time {
   long add;
   long remove;
private void addRuntime(AbstractPriorityQueue<Integer> q, Time t, int[] keys) {
   long st, et;
   // runtime for q.add()
    st = System.currentTimeMillis();
   Arrays.stream(keys).forEach(q::add);
    et = System.currentTimeMillis();
   t.add += et - st;
   // runtime for q.remove()
   st = System.currentTimeMillis();
   while (!q.isEmpty()) q.remove();
    et = System.currentTimeMillis();
   t.remove += et - st;
```

- Class type: private class.
- Constructor type: default constructor.
- Base API: System.currentTimeMillis().
- Lambda expression: Arrays.stream().

```
private Time[] benchmark(AbstractPriorityQueue<Integer>[] qs, int iter, int size) {
    Time[] ts = Stream.generate(Time::new).limit(qs.length).toArray(Time[]::new);
    Random rand = new Random();
    for (int i = 0; i < iter; i++) {
        int[] keys = Utils.getRandomIntArray(rand, size);
        for (int j = 0; j < qs.length; j++)</pre>
            addRuntime(qs[j], ts[j], keys);
    return ts;
private void testSpeed(AbstractPriorityQueue<Integer>... qs) {
    for (int size = 1000; size <= 10000; size += 1000) {</pre>
        // JVM warmup
        benchmark(qs, 10, size);
        // benchmark all priority queues with the same keys
        Time[] times = benchmark(qs, 1000, size);
}
@Test
public void testSpeed() {
    testSpeed(new LazyPriorityQueue<>(), new EagerPriorityQueue<>(), new BinaryHeap<>());
```

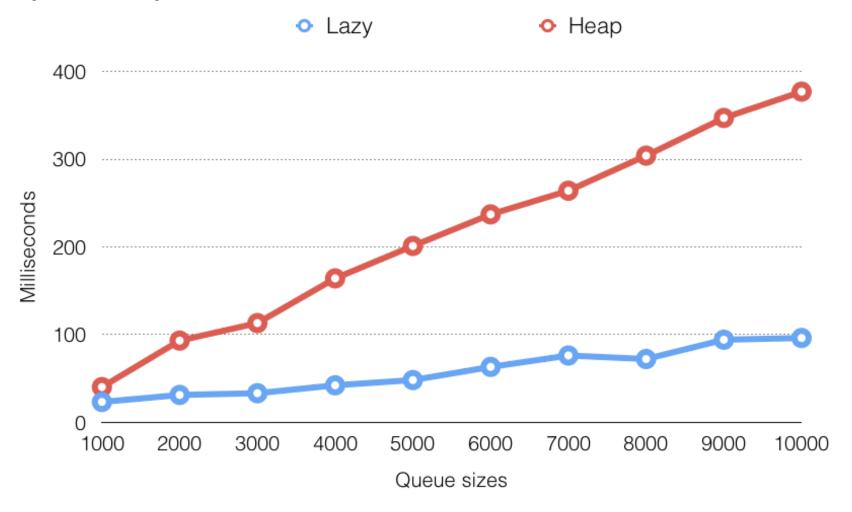
- Variable Arguments: AbstractPriorityQueue<Integer>... qs .
- Lambda expression: Stream.generate().limit().toArray().

# **Speed Comparison - Add**



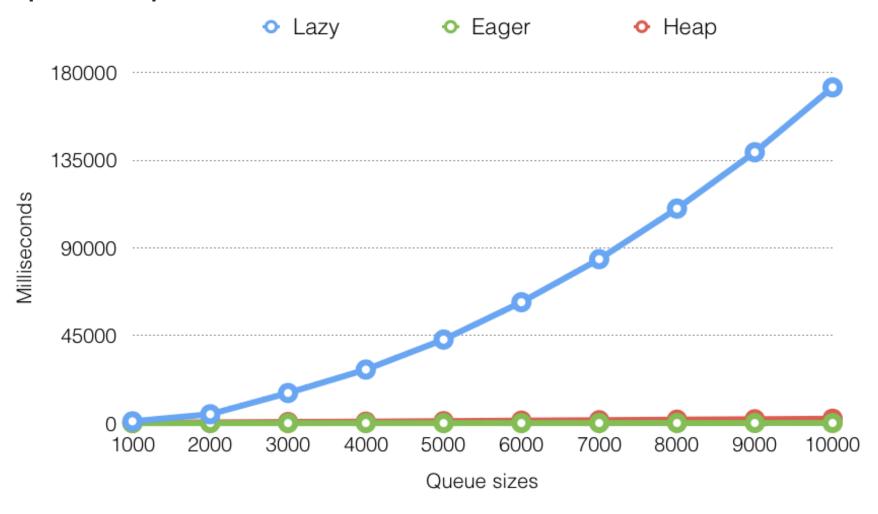
• Lazy: O(1) vs. Eager:  $O(\log n)$ ? vs. Heap:  $O(\log n)$ .

# **Speed Comparison - Add**



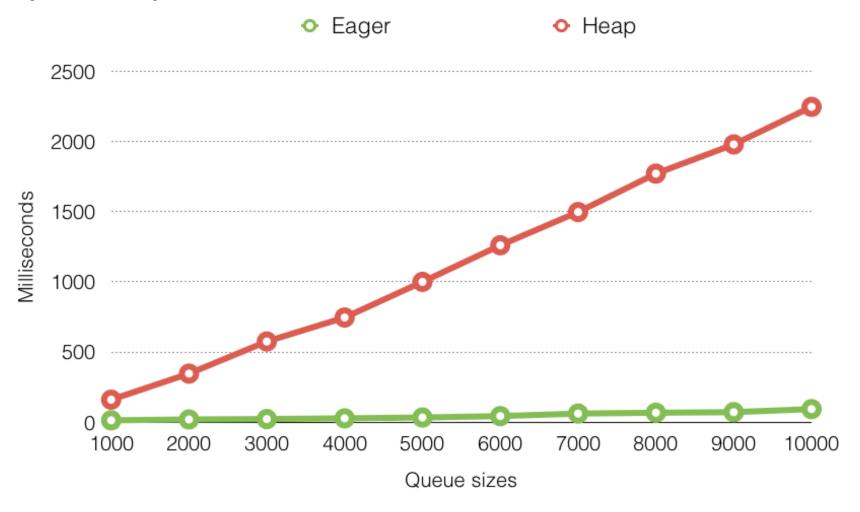
• Lazy: O(1) vs. Heap:  $O(\log n)$ .

# **Speed Comparison - Remove**



• Lazy: O(n), Eager: O(1), Heap:  $O(\log n)$ .

# **Speed Comparison - Remove**



• Eager: O(1), Heap:  $O(\log n)$ .

# References

- Priority queue.
- Binary heap.
- Java Base API:
  - o Comparable.
  - o Collections: max() , swap() , binarySearch() .
  - o Iterable: forEach() .
  - o Arrays: forEach() .
  - o Stream: generate(), limit(), toArray().
- Java Annotation:
  - @Override.
  - o @Test.