

Matrix Multiplication using MapReduce

Aim:

To perform Matrix Multiplication using MapReduce in Hadoop framework.

Theory:

Matrix multiplication is a common operation in scientific and data analysis applications. Given two matrices A ($m \times n$) and B ($n \times p$), their product $C = A \times B$ is a matrix of size ($m \times p$), where: $C[i][j] = \sum (A[i][k] \times B[k][j])$. In MapReduce, this multiplication is distributed across multiple mappers and reducers:

- **Mapper Phase:** Each mapper takes input elements of matrices A and B, and emits key-value pairs in the form (i, j) as key and partial multiplication results as values.
- **Shuffle & Sort Phase:** Framework groups all values with the same key (i, j).
- **Reducer Phase:** The reducer aggregates the partial results for each (i, j) and computes the final sum for $C[i][j]$.

Algorithm / Steps:

1. Input: Two matrices A and B stored as text files in HDFS. Each line format: A,i,j,value B,i,j,value
2. Mapper: Emits key-value pairs for all columns (for A) or rows (for B).
3. Reducer: Collects all values with same key (i,j), multiplies and sums them.
4. Output: Resulting matrix C written to HDFS.

Sample Input:

Matrix A:

```
A 0 0 1
A 0 1 2
A 1 0 3
A 1 1 4
```

Matrix B:

```
B 0 0 5
B 0 1 6
B 1 0 7
B 1 1 8
```

Reducer Output (Final Result):

Matrix C = A × B

```
C 0 0 19
C 0 1 22
C 1 0 43
C 1 1 50
```

Result:

Matrix multiplication was successfully performed using the MapReduce model. The output matrix C is obtained as expected and stored in HDFS.

Viva Questions:

1. What is the main advantage of using MapReduce for matrix multiplication?
→ It distributes computation across multiple nodes for parallel processing.
2. What are the inputs and outputs of Mapper and Reducer?
→ Mapper outputs key-value pairs; Reducer outputs the final matrix elements.
3. Why is Hadoop suitable for this operation?
→ Because it handles large datasets efficiently using distributed computing.
4. What are the real-world applications?
→ Machine Learning, Data Mining, Image Processing, and Scientific Computation.