

Write your answers in the answer blank (or circle them). Show all necessary work for full credit. Answers are to be exact values unless stated otherwise.

1. Determine the following given: $\mathbf{a} = \mathbf{i} + \mathbf{j} - 2\mathbf{k}$, $\mathbf{b} = 3\mathbf{i} - 2\mathbf{j} + \mathbf{k}$, $\mathbf{c} = \mathbf{j} - 5\mathbf{k}$

(a) $-7\mathbf{a} + 5\mathbf{b}$

1a. _____

(b) $-\mathbf{a} \cdot 2\mathbf{b}$

1b. _____

(c) $\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c})$

1c. _____

(d) $\text{comp}_{\mathbf{a}} \mathbf{b}$

1d. _____

(e) The angle between \mathbf{a} and \mathbf{b}

1e. _____

2. Find the values of x such that the vectors $\langle 3, 2, x \rangle$ and $\langle 2x, 4, x \rangle$ are orthogonal.

3. Determine an equation of the plane through $(2,1,0)$ and parallel to $x + 4y - 3z = 1$

4. Determine if the given lines are parallel, skew, or intersecting.

$$L_1 : \quad \frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$$

$$L_2 : \quad \frac{x+1}{6} = \frac{y-3}{-1} = \frac{z+5}{2}$$

5. For the given planes: $x + y - z = 1$ and $2x - 3y + 4z = 5$

- (a) Show that the planes are neither parallel nor orthogonal.
- (b) Find the angle between the planes to the nearest degree.

6. Find the distance between the planes $3x + y - 4z = 2$ and $3x + y - 4z = 24$