

Tabular Method

Step 1

- In the 1st column, list all the minterms in binary for which the output is a 1 or don't care.

Step 2

- Arrange the terms present in column 1 and column 2 considering the number of 1's in each term.

Step 3

- Identify terms that differ from another by only 1 digit and list them in the 3rd column.
- Replace the different digit by hyphen (-).

Step 4

- Repeat step 3 until no more combination can be made.

Step 5

- The term which are not carried to the next column are called “PRIME IMPLICANTS”.
- Select sufficient prime implicants to cover all the minterms.
- For this purpose, prepare a “table of choice” (prime implicant table).

Prime Implicant (PI)

- To prepare a table of choice, write PI's in rows and minterms in columns and check the minterms covered by each PI.
- If a Minterm is present only in one PI, that PI is called and “Essential PI”
 - Implicants – Groups of 1's
 - Prime Implicants – Largest groups of 1's
 - Essential Prime implicant – Having at least 1 minterm that cannot group any other way

Step 6

- Select the optimal set of PI; which covers all the original minterms, and this gives the solution.

Example

- $Z = f(A, B, C, D)$
 - $Z = 1$ for the minterms (0, 3, 5, 11, 13)
 - $Z = \text{don't care}$ for the minterms (1, 4, 12)
 - $Z = 0$ for the remaining minterms
- Simplify Z using:
 - K – Map method
 - Tabular method

$$Z = f(A, B, C, D)$$

$Z = 1$ for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care}$ for the minterms (1, 4, 12)

$Z = 0$ for the remaining minterms

Step 1

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0							
3							
5							
11							
13							
1							
4							
12							

A	B	C	D
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

m0
m1
m2
m3
m4
m5
m6
m7
m8
m9
m10
m11
m12
m13
m14
m15

$$Z = f(A, B, C, D)$$

$Z = 1$ for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care}$ for the minterms (1, 4, 12)

$Z = 0$ for the remaining minterms

Step 1

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000						
3	0011						
5	0101						
11	1011						
13	1101						
1	0001						
4	0100						
12	1100						

A	B	C	D
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

m0
m1
m2
m3
m4
m5
m6
m7
m8
m9
m10
m11
m12
m13
m14
m15

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000				
3	0011						
5	0101						
11	1011						
13	1101						
1	0001						
4	0100						
12	1100						

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000				
3	0011	1	0001				
5	0101	4	0100				
11	1011						
13	1101						
1	0001						
4	0100						
12	1100						

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000				
3	0011	1	0001				
5	0101	4	0100				
11	1011	3	0011				
13	1101	5	0101				
1	0001	12	1100				
4	0100						
12	1100						

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000				
3	0011	1	0001				
5	0101	4	0100				
11	1011	3	0011				
13	1101	5	0101				
1	0001	12	1100				
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00		
3	0011	1	0001				
5	0101	4	0100				
11	1011	3	0011				
13	1101	5	0101				
1	0001	12	1100				
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00		
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01		
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011				
13	1101	5	0101				
1	0001	12	1100				
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00		
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01		
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01		
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01	(4,5,12,13) (4,12,5,13)	– 10 – – 10 –
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3)	00 – 1	(4,5,12,13)	– 10 –
5	0101	4	0100	(1,5) (4,5) (4,12)	0 – 01 010 – – 100	(4,12,5,13)	– 10 –
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD <th>MT</th> <td>ABCD</td>	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3)	00 – 1	(4,5,12,13) (4,12,5,13)	– 10 – – 10 –
5	0101	4	0100	(1,5) (4,5) (4,12)	0 – 01 010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

R
P
S
Q

Prime Implicant Table

PI	MT	0	3	5	11	13	1	4	12
$\bar{A}\bar{C}$	P								
$B\bar{C}$	Q								
$\bar{A}\bar{B}D$	R								
$\bar{B}CD$	S								

Prime Implicant Table

PI \ MT	0	3	5	11	13	1	4	12
$\bar{A}\bar{C}$	P	✓		✓		✓	✓	
$B\bar{C}$	Q							
$\bar{A}\bar{B}D$	R							
$\bar{B}CD$	S							

Prime Implicant Table

PI	MT	0	3	5	11	13	1	4	12
$\bar{A}\bar{C}$	P	✓			✓			✓	
$B\bar{C}$	Q			✓		✓		✓	✓
$\bar{A}\bar{B}D$	R		✓				✓		
$\bar{B}CD$	S		✓			✓			

$$Z = P + Q + S$$

Prime Implicant Table

PI	MT	0	3	5	11	13	1	4	12
$\bar{A}\bar{C}$	P	✓			✓		✓	✓	
$B\bar{C}$	Q			✓		✓		✓	✓
$\bar{A}\bar{B}D$	R		✓				✓		
$\bar{B}CD$	S		✓			✓			

$$Z = P + Q + S$$

$$Z = \bar{A}\bar{C} + B\bar{C} + \bar{B}CD$$

$$Z = f(A, B, C, D)$$

Z= 1 for the minterms (0, 3, 5, 11, 13)

Z = don't care for the minterms (1, 4, 12)

Z = 0 for the remaining minterms

using K – Maps

$$Z = f(A, B, C, D)$$

Z= 1 for the minterms (0, 3, 5, 11, 13)

Z = don't care for the minterms (1, 4, 12)

Z = 0 for the remaining minterms

X

CD \ AB

		00	01	11	10
		00	1	3	2
		01	4	5	7
		11	12	13	15
		10	8	9	11

using K – Maps

$$Z = f(A, B, C, D)$$

$Z = 1$ for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care}$ for the minterms (1, 4, 12)

$Z = 0$ for the remaining minterms

X

CD

AB

	00	01	11	10
00	0 1	1 X	3 1	2
01	4 X	5 1	7	6
11	12 X	13 1	15	14
10	8	9	11 1	10

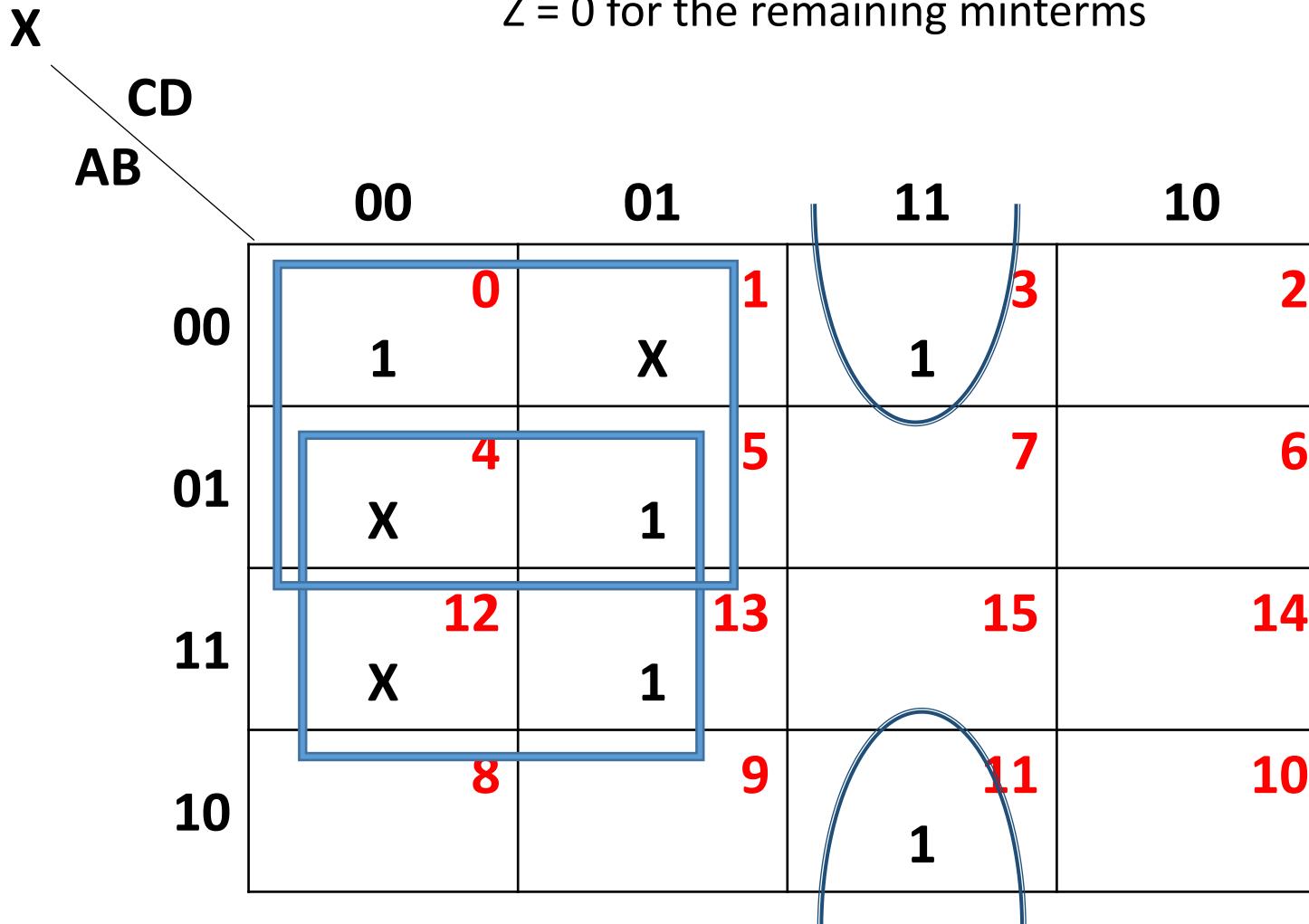
using K – Maps

$$Z = f(A, B, C, D)$$

$Z = 1$ for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care for the minterms}$ (1, 4, 12)

$Z = 0$ for the remaining minterms



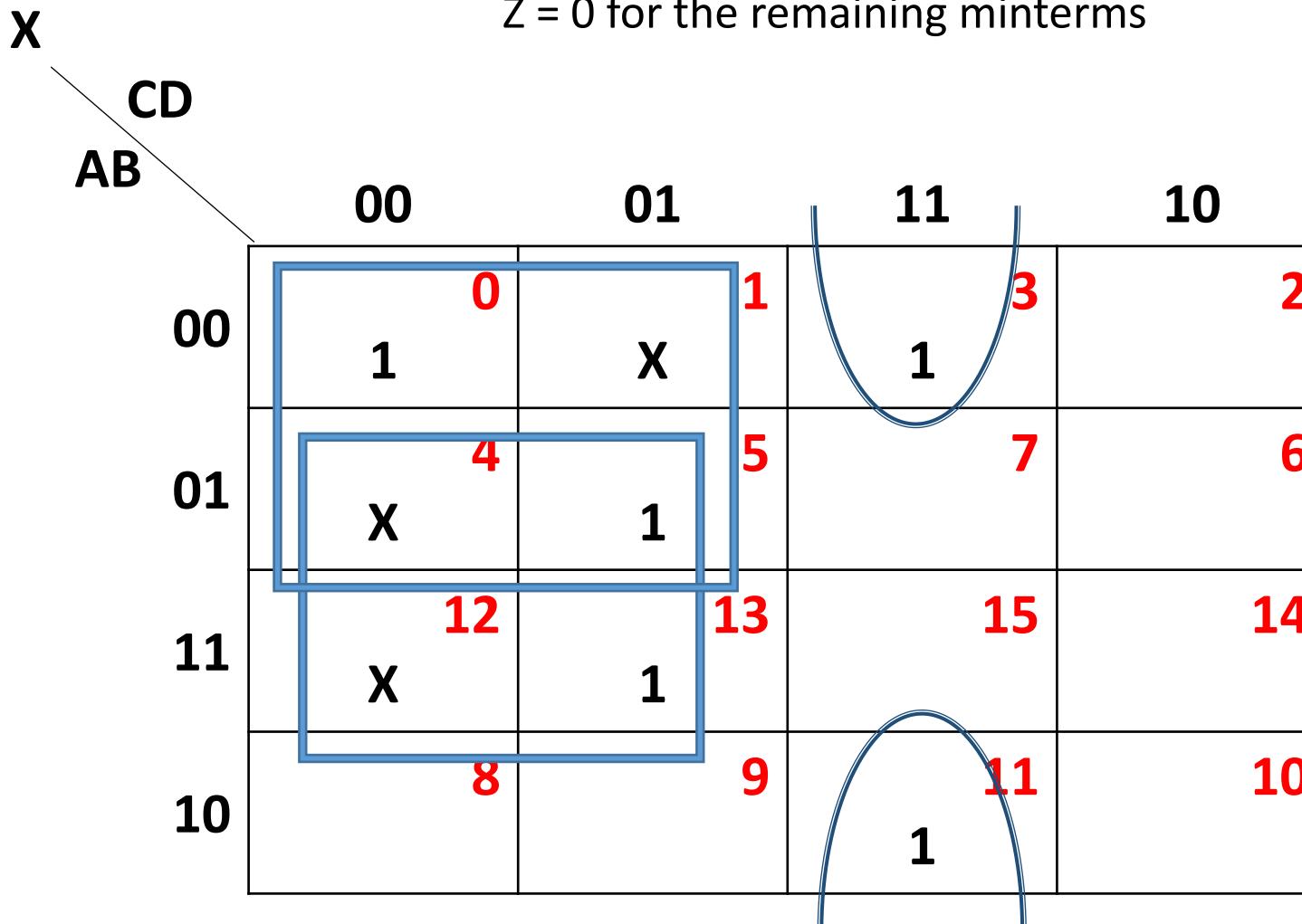
using K – Maps

$$Z = f(A, B, C, D)$$

$Z = 1$ for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care for the minterms}$ (1, 4, 12)

$Z = 0$ for the remaining minterms



using K – Maps

$$Z = \bar{A}\bar{C} + B\bar{C} + \bar{B}CD$$

Exercise - 01

- $Z = f(A, B, C, D)$
 - $Z = 1$ for the minterms (0, 2, 5, 11, 13, 15)
 - $Z = \text{don't care}$ for the minterms (7, 8, 10)
 - $Z = 0$ for the remaining minterms
- Simplify Z using:
 - K – Map method
 - Tabular method

Exercise - 02

- $Z = f(A, B, C, D)$
 - $Z = 1$ for the minterms (3, 6, 8, 12, 13, 14)
 - $Z = \text{don't care}$ for the minterms (2, 7, 9)
 - $Z = 0$ for the remaining minterms
- Simplify Z using:
 - K – Map method
 - Tabular method

$$Z = f(A, B, C, D)$$

$Z = 1$ for the minterms (3, 6, 8, 12, 13, 14)

$Z = \text{don't care}$ for the minterms (2, 7, 9)

$Z = 0$ for the remaining minterms

Step 1

	col1		col2		Col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
3	0011	8	1000	8,12	1_00	8,9,12,13	1_0_
6	0110	2	0010	8,9	100_	2,3,6,7	0_1_
8	1000	3	0011	2,3	001_		
12	1100	6	0110	2,6	0_10		
13	1101	12	1100	3,7	0_11		
14	1110	9	1001	6,14	_110		
2	0010	13	1101	6,7	011_		
7	0111	14	1110	12,13	110_		
9	1001	7	0111	12,14	11_0		
				9,13	1_01		

A	B	C	D
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

m0
m1
m2
m3
m4
m5
m6
m7
m8
m9
m10
m11
m12
m13
m14
m15

PI	MT	3	6	8	12	13	14	2	7	9
P				✓	✓	✓				✓
Q		✓	✓					✓	✓	
R			✓				✓			
S					✓		✓			

A'C+AC'+BCD'

Exercise - 03

- $Z = f(A, B, C, D)$
 - $Z = 1$ for the minterms (7, 8, 9, 10, 14, 15)
 - $Z = \text{don't care}$ for the minterms (6, 12)
 - $Z = 0$ for the remaining minterms
- Simplify Z using:
 - K – Map method
 - Tabular method