

# Tabular Method

# Step 1

- In the 1<sup>st</sup> column, list all the minterms in binary for which the output is a 1 or don't care.

## Step 2

- Arrange the terms present in column 1 and column 2 considering the number of 1's in each term.

## Step 3

- Identify terms that differ from another by only 1 digit and list them in the 3<sup>rd</sup> column.
- Replace the different digit by hyphen (-).

## Step 4

- Repeat step 3 until no more combination can be made.

## Step 5

- The term which are not carried to the next column are called “PRIME IMPLICANTS”.
- Select sufficient prime implicants to cover all the minterms.
- For this purpose, prepare a “table of choice” (prime implicant table).

# Prime Implicant (PI)

- To prepare a table of choice, write PI's in rows and minterms in columns and check the minterms covered by each PI.
- If a Minterm is present only in one PI, that PI is called and "Essential PI"
  - Implicants – Groups of 1's
  - Prime Implicants – Largest groups of 1's
  - Essential Prime implicant – Having at least 1 minterm that cannot group any other way

## Step 6

- Select the optimal set of PI; which covers all the original minterms, and this gives the solution.



# Example

- $Z = f(A, B, C, D)$ 
  - $Z = 1$  for the minterms (0, 3, 5, 11, 13)
  - $Z = \text{don't care}$  for the minterms (1, 4, 12)
  - $Z = 0$  for the remaining minterms
- Simplify  $Z$  using:
  - K – Map method
  - Tabular method

$$Z = f(A, B, C, D)$$

Z = 1 for the minterms (0, 3, 5, 11, 13)

Z = don't care for the minterms (1, 4, 12)

Z = 0 for the remaining minterms

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
<b>0</b>							
<b>3</b>							
<b>5</b>							
<b>11</b>							
<b>13</b>							
<b>1</b>							
<b>4</b>							
<b>12</b>							

# Step 1

A	B	C	D	
0	0	0	0	m0
0	0	0	1	m1
0	0	1	0	m2
0	0	1	1	m3
0	1	0	0	m4
0	1	0	1	m5
0	1	1	0	m6
0	1	1	1	m7
1	0	0	0	m8
1	0	0	1	m9
1	0	1	0	m10
1	0	1	1	m11
1	1	0	0	m12
1	1	0	1	m13
1	1	1	0	m14
1	1	1	1	m15

$$Z = f(A, B, C, D)$$

Z = 1 for the minterms (0, 3, 5, 11, 13)

Z = don't care for the minterms (1, 4, 12)

Z = 0 for the remaining minterms

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
<b>0</b>	<b>0000</b>						
<b>3</b>	<b>0011</b>						
<b>5</b>	<b>0101</b>						
<b>11</b>	<b>1011</b>						
<b>13</b>	<b>1101</b>						
<b>1</b>	<b>0001</b>						
<b>4</b>	<b>0100</b>						
<b>12</b>	<b>1100</b>						

# Step 1

A	B	C	D	
0	0	0	0	m0
0	0	0	1	m1
0	0	1	0	m2
0	0	1	1	m3
0	1	0	0	m4
0	1	0	1	m5
0	1	1	0	m6
0	1	1	1	m7
1	0	0	0	m8
1	0	0	1	m9
1	0	1	0	m10
1	0	1	1	m11
1	1	0	0	m12
1	1	0	1	m13
1	1	1	0	m14
1	1	1	1	m15

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	<b>0</b>	<b>0000</b>				
3	0011						
5	0101						
11	1011						
13	1101						
1	0001						
4	0100						
12	1100						

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000				
3	0011	1	0001				
5	0101	4	0100				
11	1011						
13	1101						
1	0001						
4	0100						
12	1100						

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	<b>0</b>	<b>0000</b>				
3	0011	<b>1</b>	<b>0001</b>				
5	0101	<b>4</b>	<b>0100</b>				
11	1011	<b>3</b>	<b>0011</b>				
13	1101	<b>5</b>	<b>0101</b>				
1	0001	<b>12</b>	<b>1100</b>				
4	0100						
12	1100						

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	<b>0</b>	<b>0000</b>				
3	0011	<b>1</b>	<b>0001</b>				
5	0101	<b>4</b>	<b>0100</b>				
11	1011	<b>3</b>	<b>0011</b>				
13	1101	<b>5</b>	<b>0101</b>				
1	0001	<b>12</b>	<b>1100</b>				
4	0100	<b>11</b>	<b>1011</b>				
12	1100	<b>13</b>	<b>1101</b>				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00		
3	0011	1	0001				
5	0101	4	0100				
11	1011	3	0011				
13	1101	5	0101				
1	0001	12	1100				
4	0100	11	1011				
12	1100	13	1101				



	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00		
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01		
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011				
13	1101	5	0101				
1	0001	12	1100				
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00		
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01		
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01		
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01	(4,5,12,13) (4,12,5,13)	– 10 – – 10 –
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3) (1,5)	00 – 1 0 – 01	(4,5,12,13) (4,12,5,13)	– 10 – – 10 –
5	0101	4	0100	(4,5) (4,12)	010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

	col1		col2		col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
0	0000	0	0000	(0,1) (0,4)	000 – 0 – 00	(0,1,4,5) (0,4,1,5)	0 – 0 – 0 – 0 –
3	0011	1	0001	(1,3)	00 – 1	(4,5,12,13) (4,12,5,13)	– 10 – – 10 –
5	0101	4	0100	(1,5) (4,5) (4,12)	0 – 01 010 – – 100		
11	1011	3	0011	(3,11)	– 011		
13	1101	5	0101	(5,13)	– 101		
1	0001	12	1100	(12,13)	110 –		
4	0100	11	1011				
12	1100	13	1101				

# Prime Implicant Table

	MT \ PI	0	3	5	11	13	1	4	12
$\overline{A}\overline{C}$	P								
$B\overline{C}$	Q								
$\overline{A}\overline{B}D$	R								
$\overline{B}CD$	S								

# Prime Implicant Table

	MT \ PI	0	3	5	11	13	1	4	12
$\overline{A}\overline{C}$	P	✓		✓			✓	✓	
$B\overline{C}$	Q								
$\overline{A}\overline{B}D$	R								
$\overline{B}CD$	S								



# Prime Implicant Table

	MT \ PI	0	3	5	11	13	1	4	12
$\overline{A}\overline{C}$	P	✓		✓			✓	✓	
$B\overline{C}$	Q			✓		✓		✓	✓
$\overline{A}\overline{B}D$	R		✓				✓		
$\overline{B}CD$	S		✓		✓				

$$Z = P + Q + S$$

# Prime Implicant Table

PI \ MT	0	3	5	11	13	1	4	12
	0	3	5	11	13	1	4	12
$\bar{A}\bar{C}$ P	✓		✓			✓	✓	
$B\bar{C}$ Q			✓		✓		✓	✓
$\bar{A}\bar{B}D$ R		✓				✓		
$\bar{B}CD$ S		✓		✓				

$$Z = P + Q + S$$

$$Z = \bar{A}\bar{C} + B\bar{C} + \bar{B}CD$$

$$Z = f(A, B, C, D)$$

$Z = 1$  for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care}$  for the minterms (1, 4, 12)

$Z = 0$  for the remaining minterms

# using K – Maps

$$Z = f(A, B, C, D)$$

$Z = 1$  for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care}$  for the minterms (1, 4, 12)

$Z = 0$  for the remaining minterms

# using K – Maps

**X**

**CD**

**AB**

	<b>00</b>	<b>01</b>	<b>11</b>	<b>10</b>
<b>00</b>	0	1	3	2
<b>01</b>	4	5	7	6
<b>11</b>	12	13	15	14
<b>10</b>	8	9	11	10

$Z = 0$  for the remaining minterms

$$Z = f(A, B, C, D)$$

Z = 1 for the minterms (0, 3, 5, 11, 13)

Z = don't care for the minterms (1, 4, 12)

Z = 0 for the remaining minterms

# using K – Maps

X

CD

AB

00

01

11

10

00

01

11

10

1

X

1

X

1

X

1

1

0

1

3

2

4

5

7

6

12

13

15

14

8

9

11

10

Z = 0 for the remaining minterms

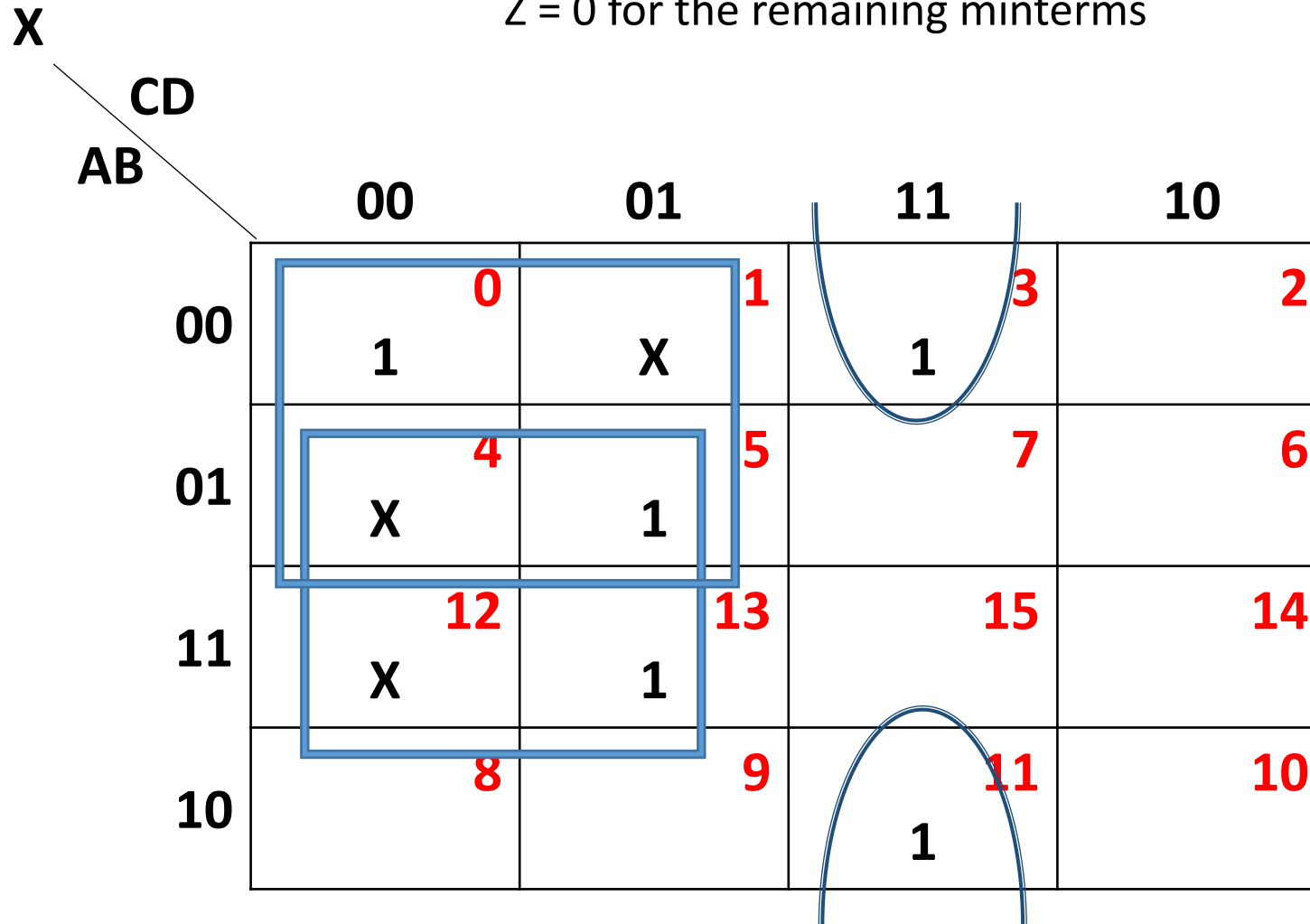
$$Z = f(A, B, C, D)$$

$Z = 1$  for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care}$  for the minterms (1, 4, 12)

$Z = 0$  for the remaining minterms

# using K – Maps

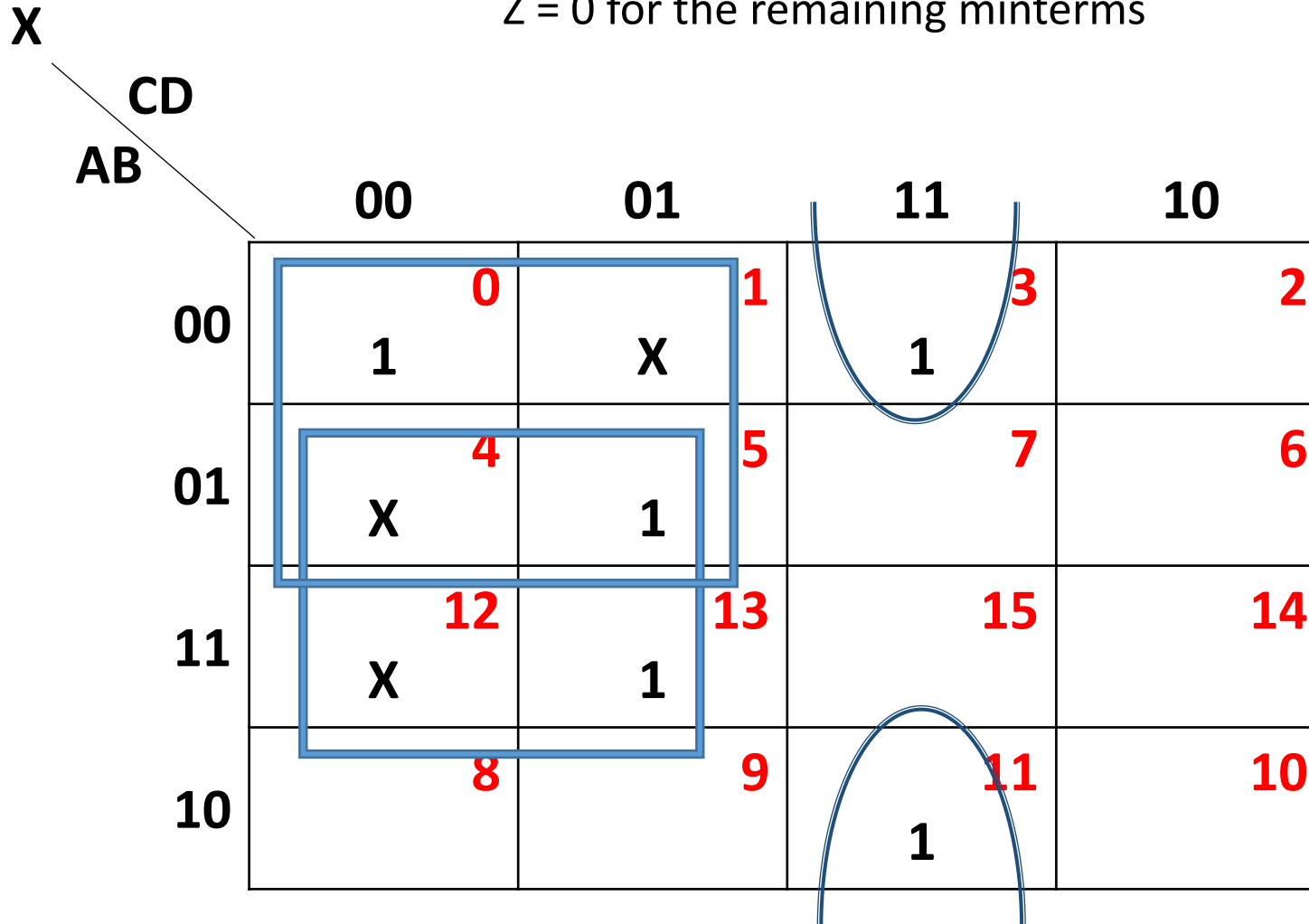


$$Z = f(A, B, C, D)$$

$Z = 1$  for the minterms (0, 3, 5, 11, 13)

$Z = \text{don't care for the minterms (1, 4, 12)}$

$Z = 0$  for the remaining minterms



# using K – Maps

$$Z = \bar{A}\bar{C} + B\bar{C} + \bar{B}CD$$

# Exercise - 01

- $Z = f(A, B, C, D)$ 
  - $Z = 1$  for the minterms (0, 2, 5, 11, 13, 15)
  - $Z = \text{don't care}$  for the minterms (7, 8, 10)
  - $Z = 0$  for the remaining minterms
- Simplify  $Z$  using:
  - K – Map method
  - Tabular method



## Exercise - 02

- $Z = f(A, B, C, D)$ 
  - $Z = 1$  for the minterms (3, 6, 8, 12, 13, 14)
  - $Z = \text{don't care}$  for the minterms (2, 7, 9)
  - $Z = 0$  for the remaining minterms
- Simplify  $Z$  using:
  - K – Map method
  - Tabular method

$$Z = f(A, B, C, D)$$

Z = 1 for the minterms (3, 6, 8, 12, 13, 14)

Z = don't care for the minterms (2, 7, 9)

Z = 0 for the remaining minterms

# Step 1

	col1		col2		Col3		col4
MT	ABCD	MT	ABCD	MT	ABCD	MT	ABCD
<b>3</b>	0011	<b>8</b>	1000	8,12	1_00	8,9,12,13	1_0_
<b>6</b>	0110	<b>2</b>	0010	8,9	100_	2,3,6,7	0_1_
<b>8</b>	1000	<b>3</b>	0011	2,3	001_		
<b>12</b>	1100	<b>6</b>	0110	2,6	0_10		
<b>13</b>	1101	<b>12</b>	1100	3,7	0_11		
<b>14</b>	1110	<b>9</b>	1001	6,14	_110		
<b>2</b>	0010	<b>13</b>	1101	6,7	011_		
<b>7</b>	0111	<b>14</b>	1110	12,13	110_		
<b>9</b>	1001	<b>7</b>	0111	12,14	11_0		
				9,13	1_01		

A	B	C	D	
0	0	0	0	m0
0	0	0	1	m1
0	0	1	0	m2
0	0	1	1	m3
0	1	0	0	m4
0	1	0	1	m5
0	1	1	0	m6
0	1	1	1	m7
1	0	0	0	m8
1	0	0	1	m9
1	0	1	0	m10
1	0	1	1	m11
1	1	0	0	m12
1	1	0	1	m13
1	1	1	0	m14
1	1	1	1	m15

MT PI	3	6	8	12	13	14	2	7	9
P			✓	✓	✓				✓
Q	✓	✓					✓	✓	
R		✓				✓			
S				✓		✓			

$$A'C + AC' + BCD'$$

## Exercise - 03

- $Z = f(A, B, C, D)$ 
  - $Z = 1$  for the minterms (7, 8, 9, 10, 14, 15)
  - $Z = \text{don't care}$  for the minterms (6, 12)
  - $Z = 0$  for the remaining minterms
- Simplify  $Z$  using:
  - K – Map method
  - Tabular method