Homework 6: Algorithms and Data Structures

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Problem 6.1

Sorting in Linear Time

- (a) It is implemented in countingsort.py
 - \$: make countingsort.
- (b) It is implemented in bucketsort.py
 - \$: make bucketsort.
- (c) The pseudo code for **COUNT_IN_INTERVAL** is given below:

Algorithm 1 Pseudo code

```
1: procedure COUNT_IN_INTERVAL(A,a,b)
        Temp[max]
 2:
 3:
        for a=0 to max do
            \text{Temp}[a] \leftarrow 0
 4:
        for i = 0 to A.length do
 5:
            temp[A[i]] \leftarrow temp[A[i]] + 1
 6:
 7:
        for j = 1 to max do
            temp[j] \leftarrow temp[j] + temp[j-1]
 8:
        count \leftarrow Temp[b]\text{-}Temp[a\text{-}1]
 9:
        return count
10:
```

- (d) It is implemented in implement_word.py
 - \$:make wordsort
- (e) Here for the bucket sort the worst case complexity is when there are all the points in a single bucket and the third party sorting algorithm has to do all the work. The worst case depends on the sorting algorithm used for sorting the buckets. So at its worst case it has the time complexity of $O(n^2)$ if the sorting algorithm for the sorting the bucket is insertion sort.

Example:

Let the points be:

0.196	0.152	0.143	0.134	0.125	0.116

So we have the buckets as:

0	\rightarrow	/					
1	\rightarrow	0.196	0.152	0.143	0.134	0.125	0.116
2	\rightarrow	/					
3	\rightarrow	/					
4	\rightarrow	/					
5	\rightarrow	/					
6	\rightarrow	/					
7	\rightarrow	/					
8	\rightarrow	/					
9	\rightarrow	/					

(f) The pseudo code for Sorting Points is given below:

```
Algorithm 2 Pseudo code for Sorting Points
```

```
ightharpoonup Euclidean Distance from Origin
 1: procedure E_Dis(A)
        distance \leftarrow \sqrt{A_x^2 + A_y^2}
                                                               \triangleright A_x and A_y are x and y coordinates of point A
        return distance
 3:
 4:
 5: procedure Points_Distance(A,B)
6: distance\leftarrow \sqrt{(A_x - B_x)^2 + (A_y - B_y)^2}
                                                                          ▶ Euclidean Distance between 2 points
                                                                          \triangleright A_x, A_y, B_x, B_y are x & y coordinates
 7:
 8:
    procedure BucketSort(A)
 9:
10:
        n = A.length
        Let B[0, \ldots, n \ 1] be a new array
11:
        for i=0 to n do
12:
             A[i].distance=E_Dis(A[i])
13:
        for i = 0 to n - 1 do
14:
             B[i] \leftarrow 0
15:
        for i = 1 to n do
16:
             B[nA[i].distance] \leftarrow A[i].distance
17:
        for i = 0 to n-1 do
18:
             sort list B[i] using insertion sort
19:
        concatenate the lists B[0], B[1], . . . , B[n 1]
20:
        return B
21:
22:
23: This is an alternative method:
24:
    procedure Bubblesort(A)
                                                                          ▷ Procedure Declaration for Point Sort
25:
                                                                                          \triangleright A is the array of Points
26:
        for i = 0 to A.length do
27:
            swapflag=False
28:
             \mathbf{for} \ \mathbf{j} \mathbf{=} \ 0 \ \mathbf{to} \ A.length\text{-}\mathbf{i}\text{-}1 \ \mathbf{do}
29:
                 if E_Dis(A[j]) > E_Dis(A[j+1]) then
30:
                     Swap (A[j] \text{ with } A[j+1])
31:
                     swapflag=True
32:
                 if swapflag==False then
33:
                     break
34:
35:
```

Problem 6.2

Radix Sort

!! NOTE !!

Run file named radixsort.py

- (a) It is implemented in radixsort.py.
 - \$: make radixsort
- (b) Here, we have a radix sort (MSD to LSD):

In this algorithm we start from the most significant bit in the number and carry on towards to the least significant bit in the number. The general algorithm makes buckets for the various digits in the first significant bit and then moves to the second making another bucket for the second most significant bit towards the LSB.

Asymptotic Time Complexity

Initially when we start with the loop of the number of the character/digits in the outer loop that is σ we have σ number of loops for the inner n numbers of numbers. Given that the input data is uniformly random distributed, then the expected running time of the MSD radix sort is $O(n \log(n)/\log(d))$. So in general we have for the asymptotic time complexity:

$$O(\sigma^*n) \implies O(n)$$

Asymptotic Storage Space

Here the storage space complexity is also O(n) this is because when there is formation of buckets for the elements in the array the number of buckets remain n.Although going recursively the number of buckets may increase by σ factor we have $O(n^*\sigma)$ given σ is constant then we have the space complexity as O(n+wr) where w is length of word and r is the size of radix.

(c) Here the implementation for the pseudo code of the algorithm which sorts n integers in the range 0 to n^31 in O(n) time.

Here the base of the numbers going inside the counting sort is n. This is done in order to have the O(n) time. If the base is 10 then if the n is large then we have large n cube so even though we use the radix sort we don't have the time complexity of O(n). Thus changing the base for the counting sort will do the trick.

So now we have 0 to (n-1) for the auxiliary array in the counting sort algorithm.I haven't implemented counting sort for that particular base number as it is similar with few changes.

Algorithm 3 Pseudo code for the Algorithm

elements

1: **procedure** RadixSort(A) \triangleright Procedure Declaration 2: $d=floor(\lg_n(n^3-1))+1$ \triangleright \lg has base n ,also d=33: RSort(A,d)4: **procedure** RSORT(A,d) 5: **for** i=d to 1 **do** 6: \triangleright Implementation for counting sort should be different and with the base for numbers n7: CountingSort_Variant(A,i) \triangleright Perform counting sort for i'th digit to sort the array