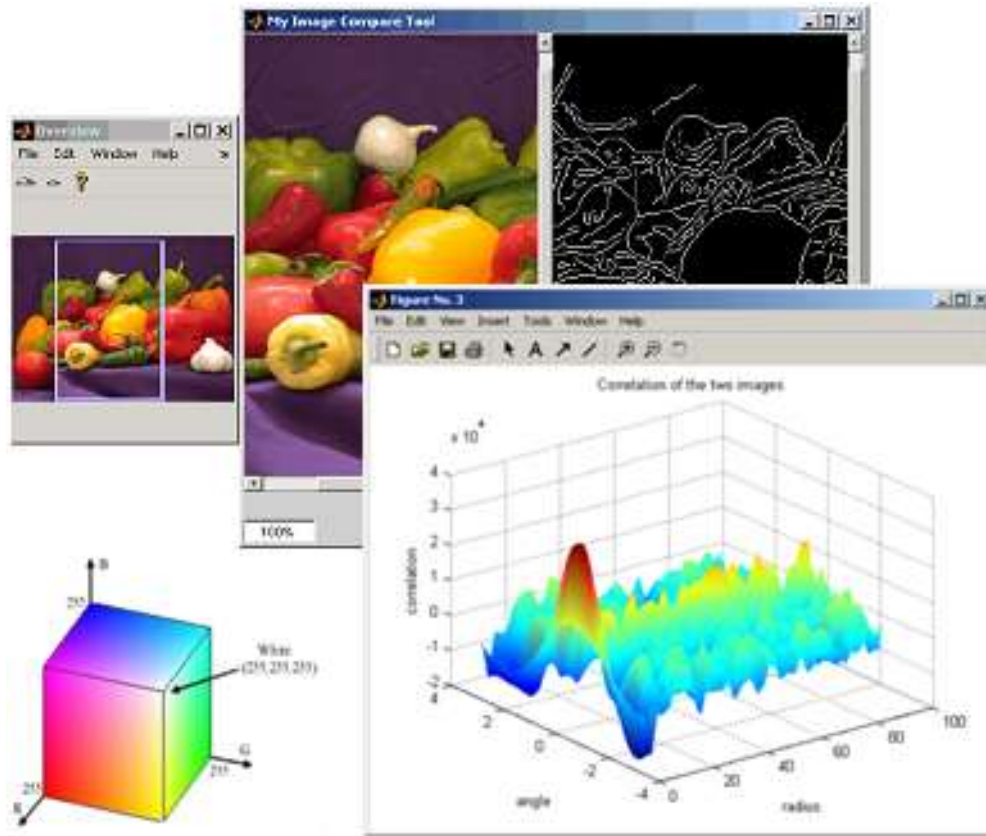


# Digital Image Processing



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ECE Department  
Gla University Mathura

**DIGITAL IMAGE  
PROCESSING**

**LECTURE -15**

# Morphological Operations (Mathematical Equations)

# Morphological Operations

- Dilation

$$I \oplus S = \{z \mid (\hat{S})_z \cap I \neq \phi\}$$

- Erosion

$$I \ominus S = \{z \mid (S)_z \cap I^c = \phi\}$$

- Opening

$$I \circ S = (I \ominus S) \oplus S$$

- Closing

$$I \bullet S = (I \oplus S) \ominus S$$

- Hit or Miss

$$I \odot S = (I \ominus S) \cap (I^c \ominus (W - S))$$

- Boundary (Internal)

$$\beta(I) = I - (I \ominus S)$$

- Boundary (External)

$$\beta(I) = (I \oplus S) - I$$

# Morphological Operations

- Region Filling

$$X_k = (X_{k-1} \oplus S) \cap I^c$$

- Connected Components

$$X_k = (X_{k-1} \oplus S) \cap I$$

- Convex Hull

$$X_k = (X_{k-1} \otimes S_i) \cup I$$

- Thinning

$$I \otimes \{S\} = (((((I \otimes S_0) \otimes S_1) \otimes S_2) \dots \otimes S_7)$$

- Thickening

$$I \odot \{S\} = | (I^c \otimes S) \text{ isolated pixel removal} |^c$$

# Morphological Operations (Previous Year Question)

# University End Sem Questions

**Ques1:** An image of size 5 x 4 and structuring element of size 1 x 2 are given below. Apply erosion, dilation operation to find the result.

**GLA University Mathura End Term Examination, Even Semester, 2023-24**

**GLA University Mathura End Term Examination, Odd Semester, 2023-24**

|   |   |   |   |
|---|---|---|---|
| 1 |   |   |   |
| 1 |   |   |   |
|   | 1 | 1 | 1 |
|   | 1 |   |   |
|   | 1 |   |   |

|          |   |
|----------|---|
| <u>1</u> | 1 |
|----------|---|

# University End Sem Questions

**Ques 2:** Perform Erosion and Dilation on the image shown in Figure. Use 0 value for padding.

**GLA University Mathura, Carry Examination, Even Semester, 2023-24**

|   |   |   |   |   |
|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 |

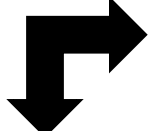










|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
| 1 | 1 | 1 |
| 0 | 1 | 0 |

# University End Sem Questions


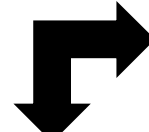

**Ques 3: Find  $A \ominus B$**

**GLA University Mathura End Term Examination, Even Semester, 2022-23**

**$X$**

|   |   |   |   |
|---|---|---|---|
|  |    |   |   |
|  |    |  |   |
|   |  |   |  |
|   |  |   |  |
|   |  |   |  |

**$B$**

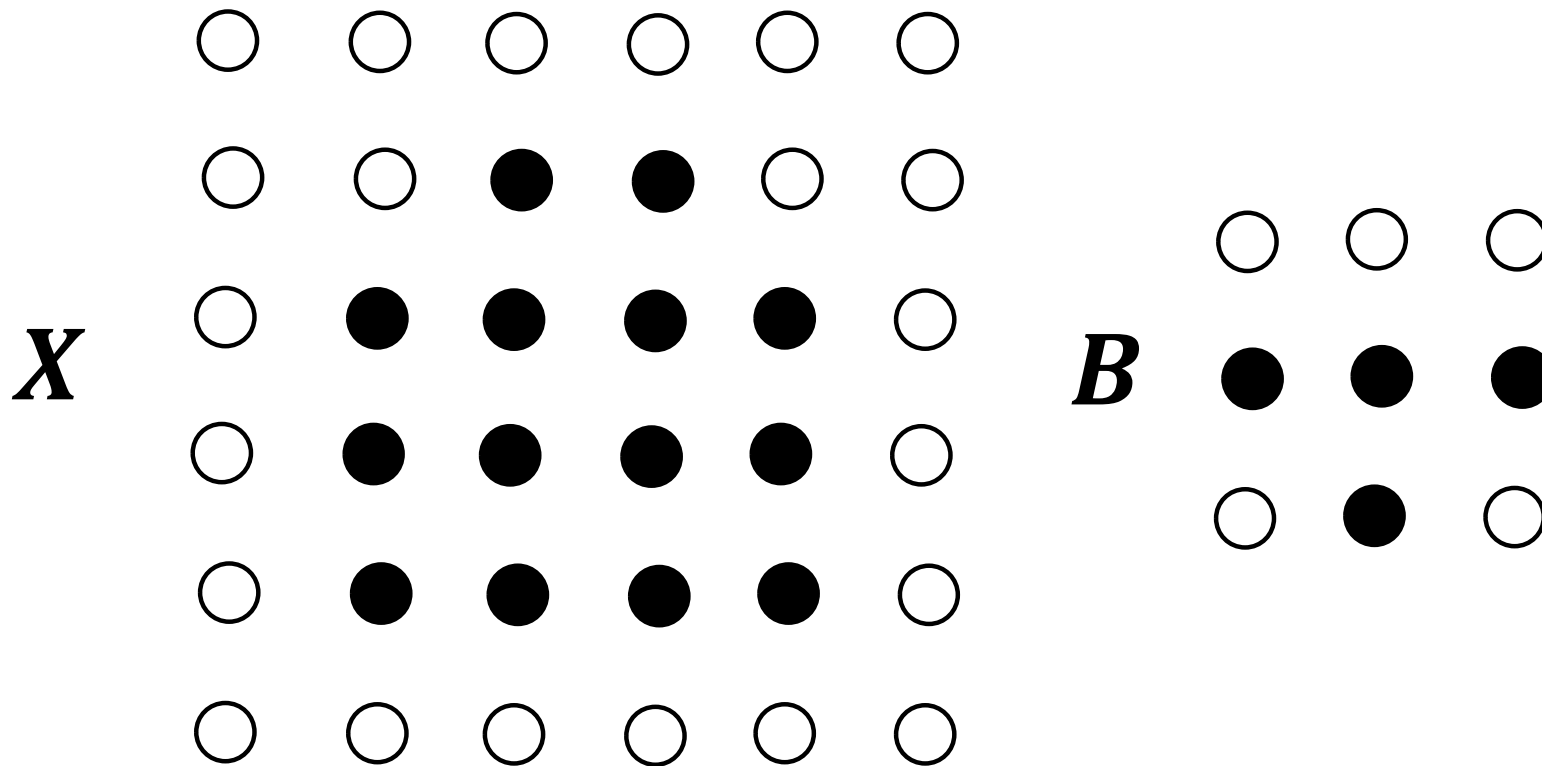
|  |  |  |
|--|--|--|
|  |  |  |
|--|--|--|



# University End Sem Questions

**Ques 4:** Binary image  $X$  and structuring element  $B$ , are given in Figure 1

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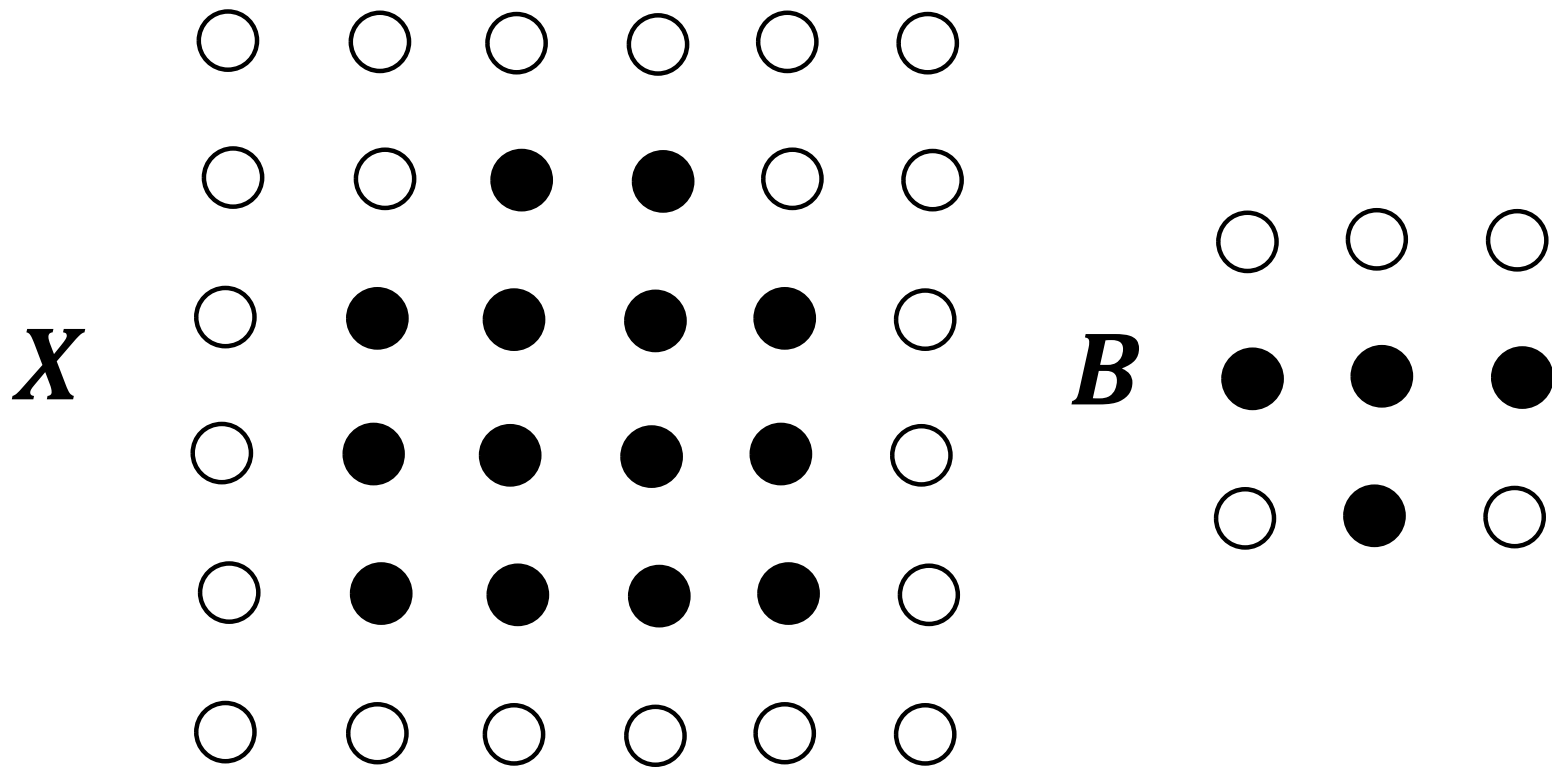


Calculate  $Y1 = X \ominus B$  where  $\ominus$  denotes the morphological erosion operator, and  $Y2 = X \oplus B$  where  $\oplus$  denotes the morphological dilation operator.

# University End Sem Questions

**Ques 5:** Binary image  $X$  and structuring element  $B$ , are given in Figure 1

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Perform the Hit or Miss transformation. Show all the steps.

# University End Sem Questions

**Ques 6:** Apply the opening operation on the image shown on the left using the structuring element on the right. Show all steps in  $8 \times 8$  grids.

**GLA University Mathura End Term Examination, Even Semester, 2022-23**

|  |   |   |   |   |   |   |  |
|--|---|---|---|---|---|---|--|
|  |   |   |   |   |   |   |  |
|  |   | 1 | 1 | 1 | 1 | 1 |  |
|  |   | 1 | 1 | 1 |   |   |  |
|  | 1 | 1 | 1 |   |   |   |  |
|  |   | 1 | 1 |   |   |   |  |
|  |   |   |   |   |   |   |  |

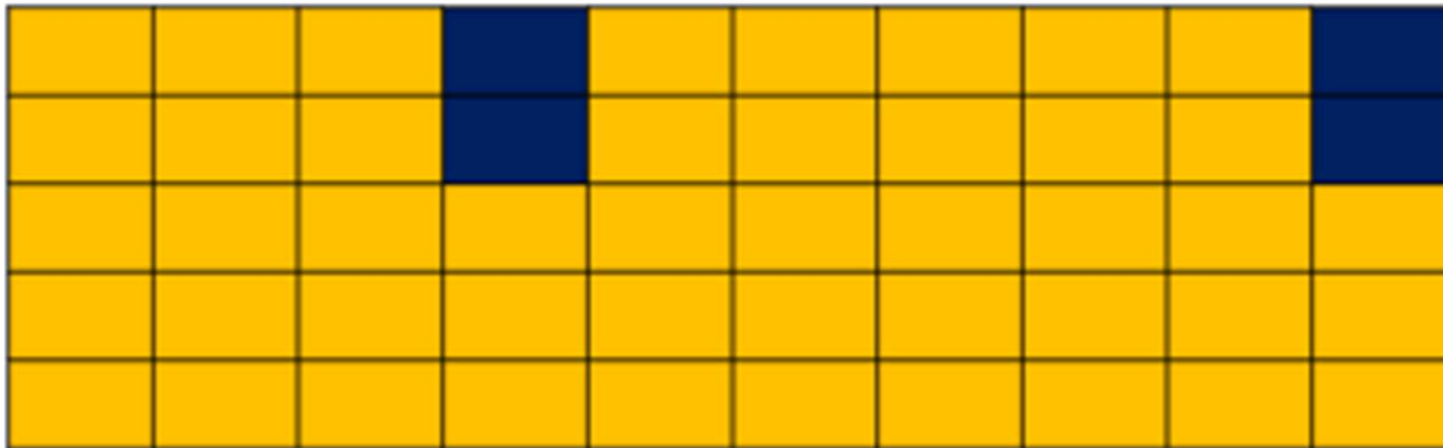
|   |          |   |
|---|----------|---|
|   | 1        |   |
| 1 | <u>1</u> | 1 |
|   | 1        |   |

# University Question

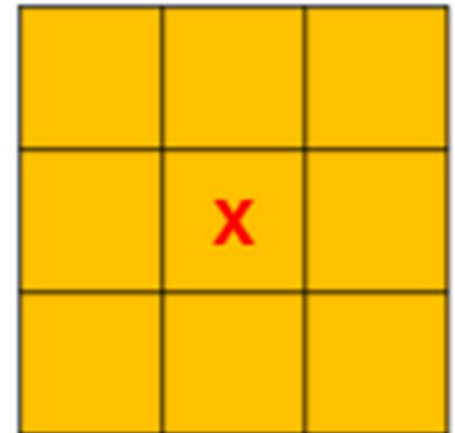
**Ques 7:** There is an image A and structuring element B. Write an apply an algorithm over the given image and structuring element to extract the boundary of the image A. (Gray color represents Logic 1 and white color represents Logic 0)

**GLA University, End Sem, Odd Sem, 2023-24**

*I*



*S*



# University End Sem Questions

**Ques 8:** When do we say the shape is convex? What do you mean by convex hull? Give the basic  $3 \times 3$  structuring elements used to find the convex hull.

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**Ques 9:** Boundary is considered as a sequence of connected points. Explain the boundary following algorithm in detail.

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**Ques 10:** Explain convex hull with the help of an Example.

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Thank You