

15-10-24
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AI lab

Misplaced tiles

class Puzzle:

```
def __init__(self, initial_state, goal_state):  
    self.board = initial_state  
    self.goal = goal_state  
    self.n = len(initial_state)
```

To find the index of '0' (blank tile)

```
def find_blank(self, board):  
    for i in range(self.n):  
        for j in range(self.n):  
            if board[i][j] == 0:  
                return (i, j)
```

Heuristic function: $h(n)$ - number of misplaced tiles

```
def misplaced_tiles(self, board):  
    misplaced = 0  
    for i in range(self.n):  
        for j in range(self.n):  
            if board[i][j] != 0 and board[i][j] != self.goal[i][j]:  
                misplaced += 1  
    return misplaced
```

Generate possible moves (neighbors) from the current state

```
def get_neighbors(self, board):  
    neighbors = []  
    blank_pos = self.find_blank(board)  
    x, y = blank_pos  
    # Possible moves (up, down, left, right)  
    moves = [(x-1, y), (x+1, y), (x, y-1), (x, y+1)]  
    for move in moves:  
        new_x, new_y = move  
        if 0 <= new_x < self.n and 0 <= new_y < self.n:  
            new_board = [row[:] for row in board] # Copy the board  
            # Swap the blank with the adjacent tile  
            new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y],  
new_board[x][y]  
            neighbors.append(new_board)  
    return neighbors
```

```

# A* Search Algorithm
def a_star(self):
    start = self.board
    goal = self.goal
    open_list = [(start, 0)] # List of tuples (board, g(n))
    closed_list = set()
    iteration = 0

    while open_list:
        # Sort open list by f(n) = g(n) + h(n)
        open_list.sort(key=lambda x: x[1] + self.misplaced_tiles(x[0])) # Sort by f(n)
        current_board, g = open_list.pop(0) # Get the board with the lowest f(n)

        iteration += 1
        print(f"\nIteration {iteration}:")
        self.print_board(current_board)
        print(f"g(n): {g}, h(n): {self.misplaced_tiles(current_board)}, f(n): {g + self.misplaced_tiles(current_board)}")

        # If we reach the goal, return the solution
        if current_board == goal:
            print("\nGoal reached!")
            return g

        # Add the current state to the closed list
        closed_list.add(tuple(map(tuple, current_board)))

        # Get all possible moves (neighbors)
        for neighbor in self.get_neighbors(current_board):
            if tuple(map(tuple, neighbor)) in closed_list:
                continue
            # g(n) is the depth (number of moves from the start)
            g_new = g + 1
            # Add neighbor to the open list
            open_list.append((neighbor, g_new))

    return -1 # If no solution is found

# Print the 3x3 board
def print_board(self, board):
    for row in board:
        print(" ".join(str(tile) if tile != 0 else "_" for tile in row))

```

```

# Helper function to take input from the user
def take_input():
    print("Enter the initial state (3x3 grid) row by row, use '0' for the blank tile:")
    initial_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        initial_state.append(row)

    print("Enter the goal state (3x3 grid) row by row, use '0' for the blank tile:")
    goal_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        goal_state.append(row)

    return initial_state, goal_state

# Main
if __name__ == "__main__":
    initial_state, goal_state = take_input()

    puzzle = Puzzle(initial_state, goal_state)
    moves = puzzle.a_star()

    if moves != -1:
        print(f"\nNumber of moves to solve: {moves}")
    else:
        print("\nNo solution found.")

```

Output

Enter the initial state (3x3 grid) row by row, use '0' for the blank tile:

5 4 0
6 1 8
7 3 2

Enter the goal state (3x3 grid) row by row, use '0' for the blank tile:

0 1 2
3 4 5
6 7 8

Iteration 1:

5 4 _
6 1 8
7 3 2
g(n): 0, h(n): 12, f(n): 12

Iteration 2:

5 4 8
6 1 _
7 3 2
g(n): 1, h(n): 13, f(n): 14

Iteration 3:

5 _ 4
6 1 8
7 3 2
g(n): 1, h(n): 13, f(n): 14

Iteration 4:

5 4 8
6 1 2
7 3 _
g(n): 2, h(n): 12, f(n): 14

Iteration 5:

```
Iteration 2587:
_ 4 2
5 3 8
6 7 1
g(n): 16, h(n): 8, f(n): 24
```

```
Iteration 2588:
_ 1 2
3 4 5
6 7 8
g(n): 24, h(n): 0, f(n): 24
```

Goal reached!

Number of moves to solve: 24

Manhattan Distance

class Puzzle:

```
def __init__(self, initial_state, goal_state):
    self.board = initial_state
    self.goal = goal_state
    self.n = len(initial_state)
```

To find the index of '0' (blank tile)

```
def find_blank(self, board):
    for i in range(self.n):
        for j in range(self.n):
            if board[i][j] == 0:
                return (i, j)
```

Heuristic function: h(n) - Manhattan distance

```
def manhattan_distance(self, board):
    distance = 0
    for i in range(self.n):
        for j in range(self.n):
            if board[i][j] != 0: # Don't calculate for the blank tile (0)
                goal_x, goal_y = self.find_position(self.goal, board[i][j])
                distance += abs(i - goal_x) + abs(j - goal_y)
    return distance
```

Find the position of a tile in the goal state

```
def find_position(self, board, value):
    for i in range(self.n):
        for j in range(self.n):
```

```

        if board[i][j] == value:
            return (i, j)

# Generate possible moves (neighbors) from the current state
def get_neighbors(self, board):
    neighbors = []
    blank_pos = self.find_blank(board)
    x, y = blank_pos
    # Possible moves (up, down, left, right)
    moves = [(x-1, y), (x+1, y), (x, y-1), (x, y+1)]
    for move in moves:
        new_x, new_y = move
        if 0 <= new_x < self.n and 0 <= new_y < self.n:
            new_board = [row[:] for row in board] # Copy the board
            # Swap the blank with the adjacent tile
            new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y],
new_board[x][y]
            neighbors.append(new_board)
    return neighbors

# A* Search Algorithm
def a_star(self):
    start = self.board
    goal = self.goal
    open_list = [(start, 0)] # List of tuples (board, g(n))
    closed_list = set()
    iteration = 0

    while open_list:
        # Sort open list by f(n) = g(n) + h(n)
        open_list.sort(key=lambda x: x[1] + self.manhattan_distance(x[0])) # Sort by f(n)
        current_board, g = open_list.pop(0) # Get the board with the lowest f(n)

        iteration += 1
        print(f"\nIteration {iteration}:")
        self.print_board(current_board)
        print(f"g(n): {g}, h(n): {self.manhattan_distance(current_board)}, f(n): {g +
self.manhattan_distance(current_board)}")

        # If we reach the goal, return the solution
        if current_board == goal:
            print("\nGoal reached!")
            return g

```

```

        # Add the current state to the closed list
        closed_list.add(tuple(map(tuple, current_board)))

        # Get all possible moves (neighbors)
        for neighbor in self.get_neighbors(current_board):
            if tuple(map(tuple, neighbor)) in closed_list:
                continue
            # g(n) is the depth (number of moves from the start)
            g_new = g + 1
            # Add neighbor to the open list
            open_list.append((neighbor, g_new))

    return -1 # If no solution is found

# Print the 3x3 board
def print_board(self, board):
    for row in board:
        print(" ".join(str(tile) if tile != 0 else "_" for tile in row))

# Helper function to take input from the user
def take_input():
    print("Enter the initial state (3x3 grid) row by row, use '0' for the blank tile:")
    initial_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        initial_state.append(row)

    print("Enter the goal state (3x3 grid) row by row, use '0' for the blank tile:")
    goal_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        goal_state.append(row)

    return initial_state, goal_state

# Main
if __name__ == "__main__":
    initial_state, goal_state = take_input()

    puzzle = Puzzle(initial_state, goal_state)
    moves = puzzle.a_star()

    if moves != -1:
        print(f"\nNumber of moves to solve: {moves}")

```

```
else:  
    print("\nNo solution found")
```

Output

Enter the initial state (3x3 grid) row by row, use '0' for the blank tile:

```
5 4 0  
6 1 8  
7 3 2
```

Enter the goal state (3x3 grid) row by row, use '0' for the blank tile:

```
0 1 2  
3 4 5  
6 7 8
```

Iteration 1:

```
5 4 _  
6 1 8  
7 3 2  
g(n): 0, h(n): 12, f(n): 12
```

Iteration 2:

```
5 4 8  
6 1 _  
7 3 2  
g(n): 1, h(n): 13, f(n): 14
```

Iteration 3:

```
5 _ 4  
6 1 8  
7 3 2  
g(n): 1, h(n): 13, f(n): 14
```

Iteration 4:

```
5 4 8  
6 1 2  
7 3 _  
g(n): 2, h(n): 12, f(n): 14
```

Iteration 5:

```
5 1 4  
6 _ 8  
7 3 2  
g(n): 2, h(n): 12, f(n): 14
```

Iteration 6:

```
_ 5 4  
6 1 8  
7 3 2  
g(n): 2, h(n): 12, f(n): 14
```


6 3 8
g(n): 20, h(n): 4, f(n): 24

Iteration 2587:

_ 4 2
5 3 8
6 7 1
g(n): 16, h(n): 8, f(n): 24

Iteration 2588:

_ 1 2
3 4 5
6 7 8
g(n): 24, h(n): 0, f(n): 24

Goal reached!

Number of moves to solve: 24
