

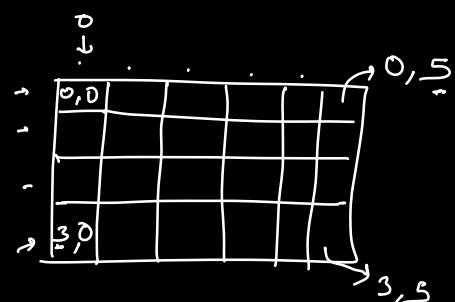
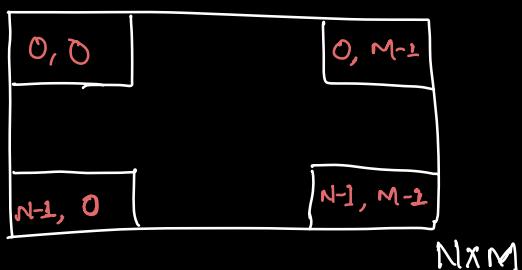
- Arrays
- Subarrays
- Prefix sum
- Carry forward
- Sliding window
- Contribution Tech.

↑  
0 1 2 3 4 5 6 7 ←

$$\Rightarrow \begin{array}{|c|c|c|c|c|c|c|c|} \hline & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \hline 0 & | & | & | & | & | & | & | & | \\ \hline 1 & | & | & | & | & | & | & | & | \\ \hline 2 & | & | & | & | & | & | & | & | \\ \hline 3 & | & | & | & | & | & | & | & | \\ \hline 4 & | & | & | & | & | & | & | & | \\ \hline \end{array} \Rightarrow \underline{\text{2D Matrix}}$$

$$\begin{aligned} \text{No. of cells} &= 5 \times 8 \\ &= 40 \end{aligned}$$

int mat [4][6]  
 ↓      ↓  
 No. Rows    No. of Col  
 [0 - 3]      [0 - 5]



Q Given a 2-D array of size  $N \times M$ .

Print all the values row-by-row.

```
for (i=0; i<N ; i++) {  
    for (j=0; j<M; j++) {  
        print (A[i][j]),  
    }  
}
```

TC:  $O(NM)$

Q Given a matrix. Print sums of all the cols.

$$\begin{array}{rccc} 3 & 1 & 6 & \\ 8 & 2 & 5 & \\ 0 & -1 & 3 & \\ 11 & 4 & 4 & \\ \hline 11 & 2 & 14 & \end{array}$$

```
for (j=0; j<M; j++) {
```

$$S = 0;$$

```
for (i=0; i<N ; i++) {
```

$$S = S + A[i][j],$$

}

```
print (S),
```

}

Q Given two 2-D matrices. Return the sum.

$$A : \begin{matrix} 3 & 2 & 8 \\ 1 & 6 & 9 \\ 7 & 5 & 4 \end{matrix}$$

$$B : \begin{matrix} -1 & 2 & 2 \\ -2 & 6 & 1 \\ 3 & 4 & 8 \end{matrix}$$

$$A + B \Rightarrow \begin{matrix} (3-1) & (2+2) & (8+2) \\ (1-2) & (6+6) & (9+1) \\ (7+3) & (5+4) & (4+8) \end{matrix}$$

Dimensions of the two matrices have to be  
the same for addition / subtraction

Sum [N][M] ← New space

for ( $i = 0$ ;  $i < N$ ;  $i + 1$ ) {

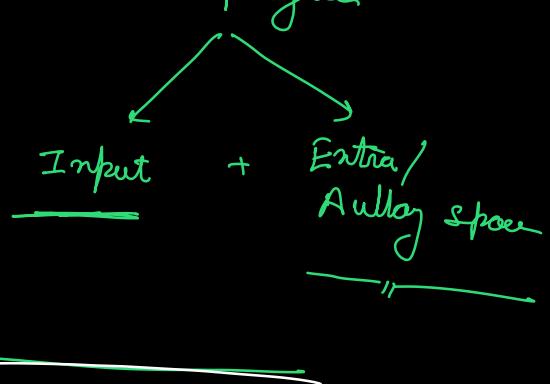
    for ( $j = 0$ ;  $j < M$ ;  $j + 1$ ) {

$$\text{Sum}[i][j] = A[i][j] + B[i][j],$$

TC :  $O(N \times M)$

SC :  $O(N \times M)$

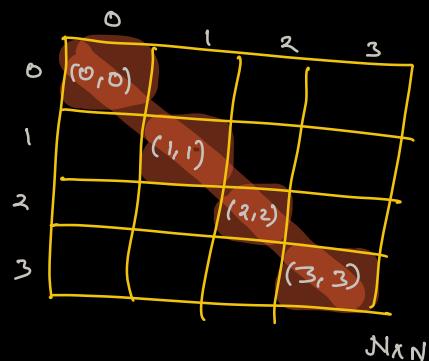
Space Complexity  $\Rightarrow$  Total space used in the program



Q Given a square matrix. Print all the diagonal elements. (L to R)

```
for(i=0; i<N; i+1){
    print(a[i][i]),
}
```

TC:  $O(N)$



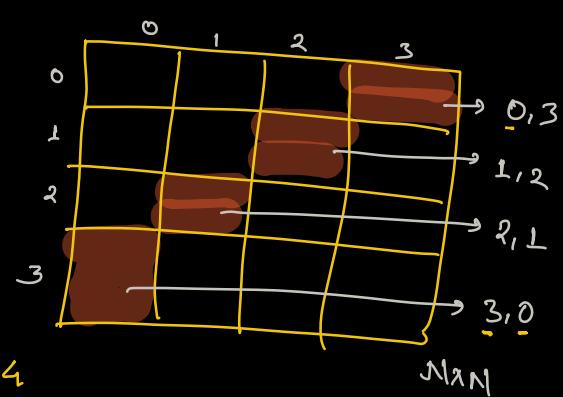
Diagonal (R-to-L)

Row 0  $\rightarrow$  (N-1)

Col N-1  $\rightarrow$  0

$$i+j = N-1$$

$$\Rightarrow \boxed{j = N-i-1}$$



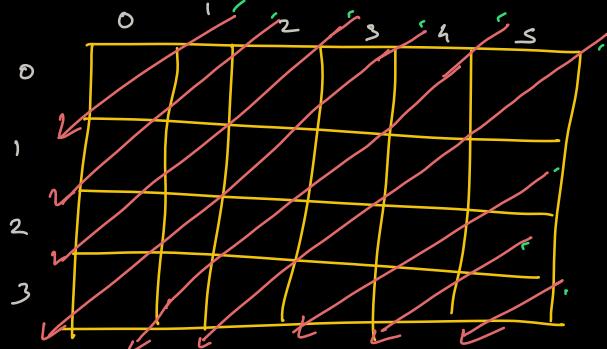
```

i = 0 ; j = N-1;
while ( i < N && j >= 0 ) {
    Print ( arr[i][j] );
    i++;
    j--;
}

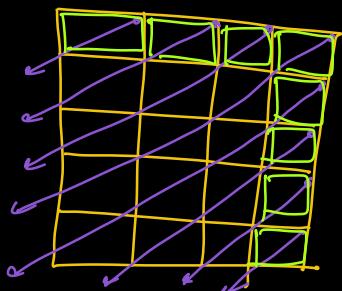
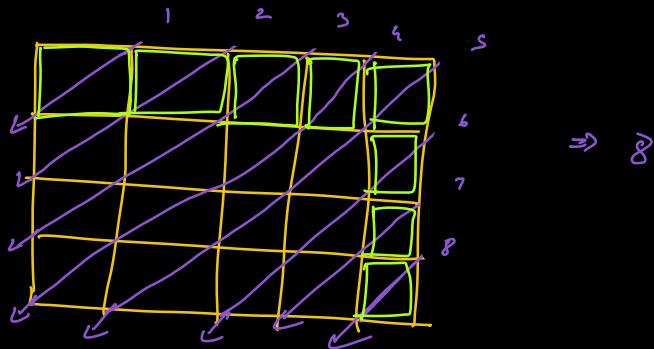
```

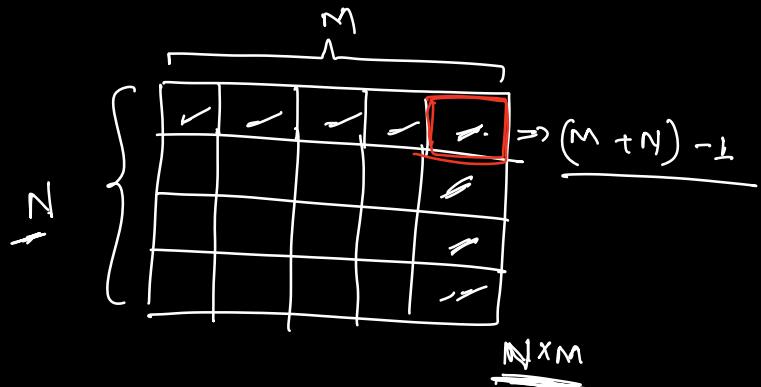
Q Diagonals in a

rect. matrix



Quiz

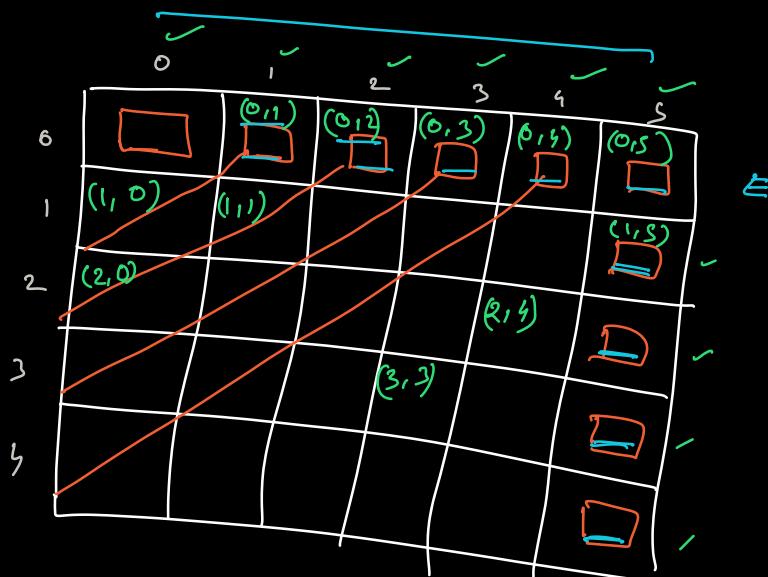




$$\boxed{\text{No of diagonals} = N + M - 1}$$

(R to L)

OR  
(L to R)



Print Diagonal ( $s_i, s_j, N, M$ ) {

$i = s_i; j = s_j;$

while ( $i < N \text{ } \&\& \text{ } j \geq 0$ ) {

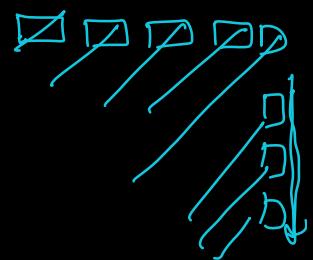
Print( $a[i][j]$ );

$i++; j--;$

```

// for the first row
for (j=0 ; j < m ; j++) {
    PrintDiagonal(0, j, n, m),
}

```

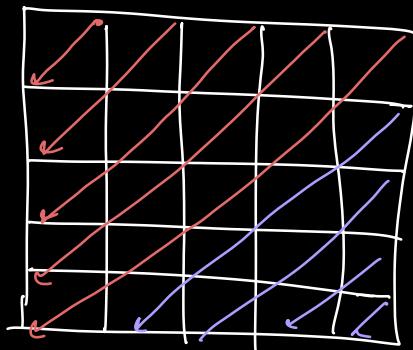
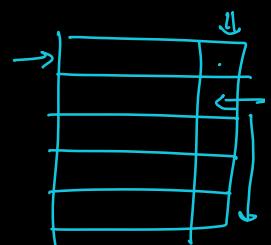


// for the last col.

```

for (i=1; i < n; i++) {
    PrintDiagonal(i, m-1, n, m),
}

```



Total No of Cells =  $N \times M$

$$TC = O(N \times M)$$

Break till 10:35 p

Q  
=

Given a square matrix. Convert it to transpose.  
Without using any extra space.

1	2	3
4	5	6
7	8	9

→ 1 4 7  
2 5 8  
3 6 9

1, 4, 6

1 5 8

2, 7, 2 →

4 7 9

3, 6, 5

6 2 5

0<sup>th</sup> row → 0<sup>th</sup> col  
1<sup>st</sup> row → 1<sup>st</sup> col  
⋮

(N-1) row → (N-1) col

	0	1	2	3	4
0	3	2	1	4	5
1	8	7	9	10	11
2	1	2	3	4	5
3	0	1	8	10	12
4	7	9	13	17	21

	0	1	2	3	4
0	3	8	1	0	7
1	2	7	2	1	9
2	1	9	3	8	13
3	4	10	9	10	17
4	5	11	5	12	21

$$(0,0) \longrightarrow (0,0)$$

$$(0,1) \longrightarrow (1,0)$$

$$(0,2) \longrightarrow (2,0)$$

①  $i, j \longrightarrow j, i$

② Diagonal elements remain in original position.

for ( $i=0; i < N; i++$ ) {

$i$   
0      j  
      3

  for ( $j=i+1; j < N; j++$ ) {

j  
3      0

    // Swap  $A[i][j]$  with  $A[j][i]$

    ↓

    ↓

TC :  $O(N^2)$   
SC :  $O(1)$

HW : Create transpose by iterating over the lower triangle.

Q

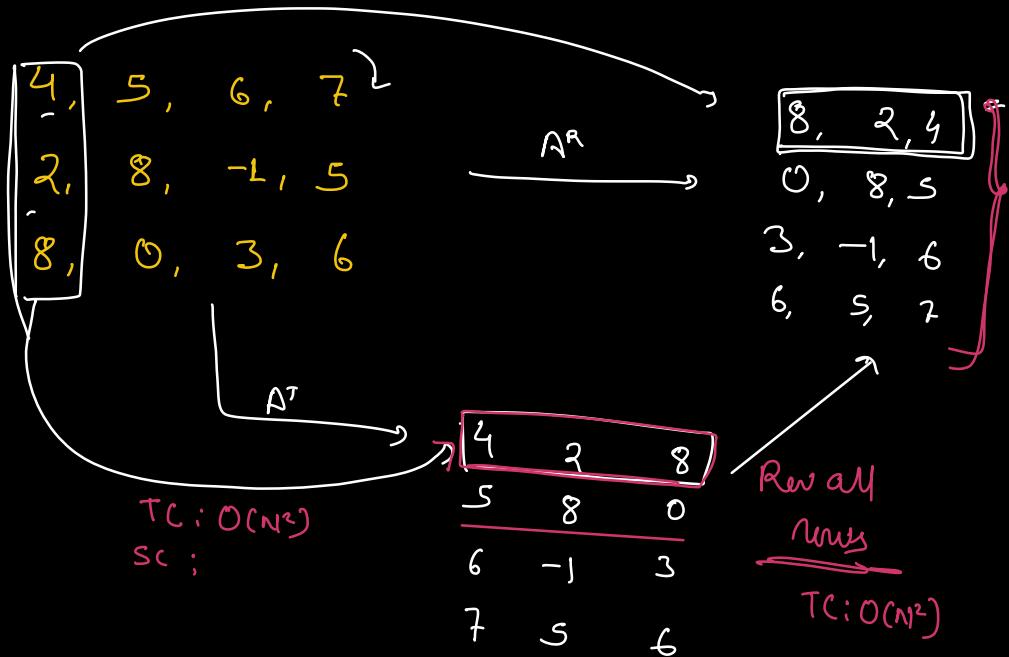
Amazon  
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Given a square matrix. ( $N \times N$ )

Rotate it by  $90^\circ$  in clockwise direction.  
[Without extra space]

$$\begin{array}{cccc}
 1, & 2, & 3, & 4 \\
 5, & 6, & 7, & 8 \\
 9, & 10, & 11, & 12 \\
 13, & 14, & 15, & 16
 \end{array} \xrightarrow{90^\circ} \Rightarrow \begin{array}{cccc}
 13, & 9, & 5, & 1 \\
 14, & 10, & 6, & 2 \\
 15, & 11, & 7, & 3 \\
 16, & 12, & 8, & 4
 \end{array}$$

A :



- Write matrix on a paper
- Rotate the paper by  $90^\circ$  clockwise.

$$\text{TC} : \underbrace{O(N^2)}_{A^T} + \underbrace{O(N^2)}_{\text{Rev of rows}} \Rightarrow O(N^2) \quad \begin{cases} \text{SC: } \underbrace{O(1)}_{(\text{Extra})} \\ \text{OSC = } O(N^2) \end{cases}$$

$$\textcircled{1} \quad A \rightarrow A^T \Rightarrow O(N^2) \mid O(1)$$

$$\textcircled{2} \quad \text{Rev all rows of } A^T \Rightarrow O(N^2) \mid O(1)$$

↓

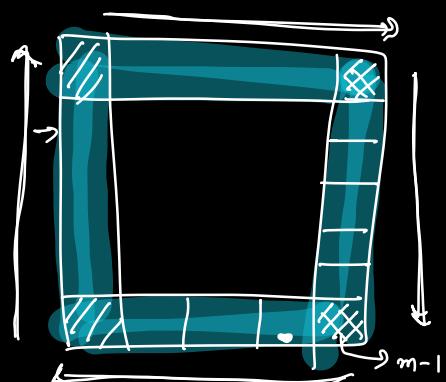
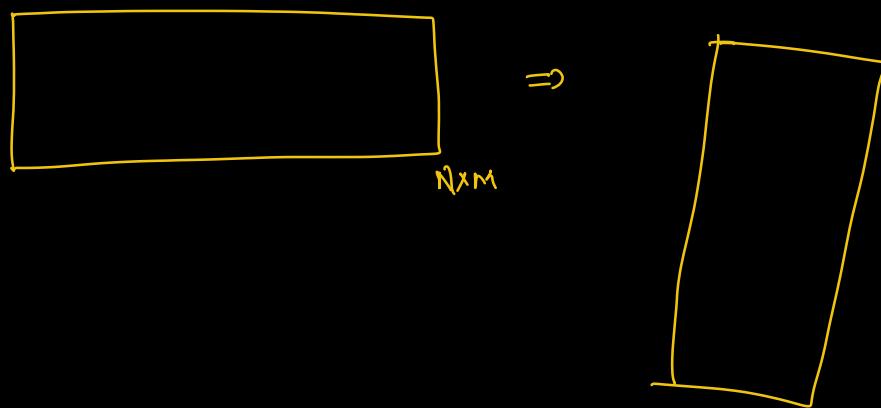
$$T() : O(N^2)$$

—————

$$\text{Mat} \rightarrow N \times M$$

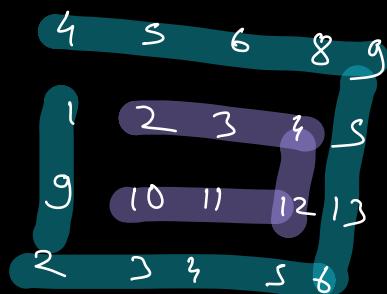
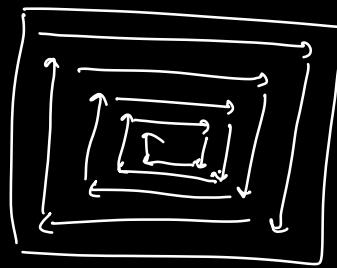
$$\underline{\underline{A_i : N \times M}}$$

$$A^T \Rightarrow \underline{\underline{M \times N}}$$

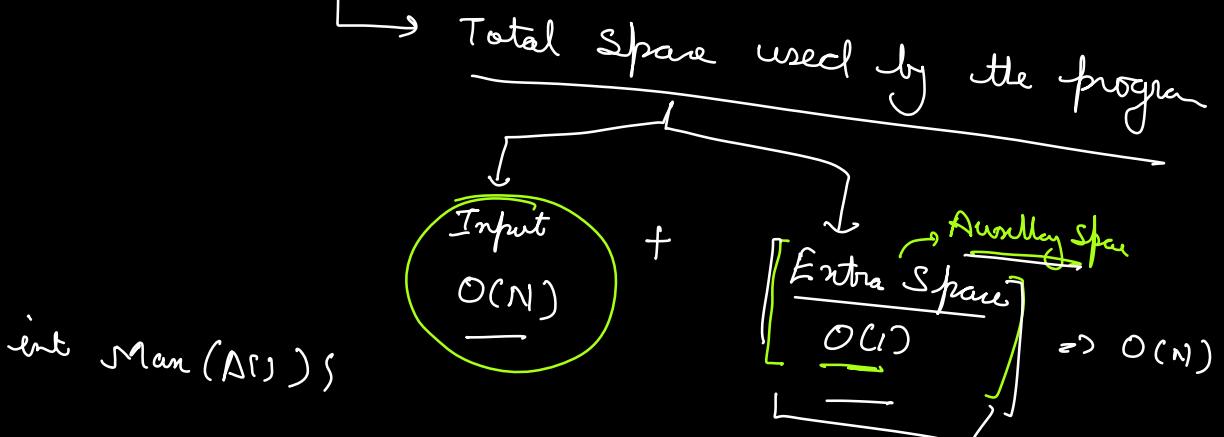


- ①  $i \rightarrow 0, \quad \begin{matrix} & M \times N \\ \nearrow & \searrow \end{matrix}$   
for ( $j = 0 \rightarrow M$ )
- ②  $C \rightarrow M-1$   
for ( $i = 1 \rightarrow N$ )
- ③  $i \rightarrow N-1$   
for ( $j = m-2 \rightarrow 0$ )
- ④  $C \rightarrow 0$   
for ( $i = N-2 \rightarrow 1$ )

HW: Print Matrix in Spiral order



Space Complexity



int Max(A[]){}

SC of Binary Search :  $\frac{O(1)}{\text{Extra Space}}$