



Examination : Block - Repeater      Seat No. :  
Date : 19/11/2018      Day :  
Time : 11:00 to 12:15 pm      Max. Marks : 36

INSTRUCTIONS:

1. Figures to the right indicate maximum marks for that question.
2. The symbols used carry their usual meanings.
3. Assume suitable data, if required & mention them clearly.
4. Draw neat sketches wherever necessary.

Q.1 Do as directed.

- (a) Prove that if  $L_1$  and  $L_2$  are CFL but  $L_1'$  and  $L_1 \cap L_2$  are not CFL. [03]
- (b) Prove that product of two odd integer is Odd using direct constructive method. [03]
- (c) If  $A$  is set of real numbers so  $2^A$  is countable / uncountable and infinite / finite. Justify your answer with proper reason. [03]
- (d) Give Context free grammar for  $L = \{ a^i b^j c^k \mid i, j, k \geq 0, \text{ and } i = j \text{ or } i = k \}$  [03]

Q.2 Attempt following questions.(any two)

- (a) Design PDA for  $L = \{ a^{2n} b^{3n} \mid n \geq 0 \}$  [06]
- (b) Draw DFA for given two language. [06]  
 $L_1 = \{ w \in \Sigma^* \mid w = saba \text{ for some string } s \in \Sigma^* \}$   
 $L_2 = \{ w \in \Sigma^* \mid na(w) \geq 2, nb(w) \leq 1 \}$
- (c) State and explain Kleene's theorem part 1. [03]  
[03]

- Q.3 (a) Design TM for reverse of string. For example i/p aabb | - o/p bbaa. [05]  
Trace for given above example. [03]
- (b) Define Chomsky Hierarchy and relation between grammar. [04]

OR

- Q.3 (a) Design TM for  $L = \{ a^n b^n c^n \mid n \geq 0 \}$ . Trace for string aabbcc and aabc. [05]  
[03]
- (b) Describe unrestricted grammar using one example and differentiate between unrestricted grammar and CSL. [04]