Numerical - Categorical Relationship

- Tests
  - T- test
  - Z- test

- Constraint on Num - Categories
  - num_categories = 2

Questions What test would you use for following Variable pairs

1. Product vs Gender
   Chi - square

2. Income vs Gender
   T- test / z - test

3. Product vs Income?
   (>2 Categories) (Numerical)
   - nC_2 T- Tests (n → num_categories)
   - One Way ANOVA

One-Way ANOVA Test

* One → A single categorical Variable (Ex: Product)
* Way → Dependent Variable (Ex. Income)
* ANOVA → Analysis of Variance
* Uses **F-Distribution** to generate **F-statistic / F-ratio**
* This test is suitable when dealing with

Numerical Variable

vs

Categorical Variable
(num_categories > 2)

* Aerofit: Is there a significant Difference between Income of Different product Buyers

H_0 : Means across all groups are Same

H_a : Atleast mean of One Group is Different

In Anova

① Analys Variance of Data using F Distribution

② Two types
- Variance Between the Groups
- Variance within the Groups

F-ratio

$$\frac{\text{Variance Between the Groups}}{\text{Variance within the Groups}}$$

F-ratio
F statistic

F-ratio $\propto \frac{1}{p}$

* Interpretation

① F-score is 1 (ie) Both within and Between Variances are close to each other

② Population is probably Common for all Group/Samples

② F-score >> 1

① Samples might be from Population with Different means

Assumptions of ANOVA

① Normality of Data (Residual)

② Homogeneous Variances (Residual)
(Variances across groups should be approximately Equal)

③ Independent Observations

Questions

① Do we Have Alternative when Data is Not Gaussian?

② How do we check if Data is Gaussian?

Kruskal - Wallis Test

H_0 : All groups have same population median

H_a : There is a significant difference in medians of Atleast two group

Advantages

1. No assumption of Normality

2. Robust to Outliers

Limitations

1. Less powerful compared to ANOVA when assumption are met.

② How do we check if Data is Gaussian?

Ans ① Plot Histogram

② Plot QQ-plot

③ Shapiro Wilkins Test

H_0 ⇒ Data is Gaussian

H_a ⇒ Data is Not Gaussian

α ⇒ 0.05

test_stat, pvalue ⇒ Shapiro(data)

Levene – Test

Used for checking if variances in 2 samples are equal or Not

H_0 : Variances are Equal i.e. $\sigma_1^2 = \sigma_2^2$

H_a : Variance are not Equal

- Returns a p-value and a Test-statistic
- P-Value can be compare with α to reject or fail to Reject: $H_0 (\sigma_1^2 = \sigma_2^2)$