

- Key words:
- STFT - Short-term Fourier Transform
 - Piecewise Linear Transformation
- NLP) Speaker - Diarization.
input: multiple voice signal
output: transcript
solution: framing → frame by frame feature comparison
-
- Signal
- fragmentation
- clustering
- Sampling
 - zero-crossing rate
-
- Low rate High rate
- MFCC - Mel Frequency Cepstral Coefficients
 - Letters → sentences → paragraphs → documents → corpus
- * NLTK - natural language toolkit (Python library)



→ Processing Text Data

D1 I read a book daily

D2 I bought ticket

D3 Read and wrote daily

- ① Tokenization - word level or character level
- ② Stop word removal - domain specific
- ③ Stemming - transform word to root form

eg: crying }
 Cries }
 Cried } cry
 | remove
 | suffix

machines → machine

Note: butterflies → butterfly
solution Lemmatization: preserves meaning

(4) Lower case conversion

(5) Extract vocabulary: list of terms

V = {book, daily, read, ticket, write}

Note: Not necessarily in alphabetic order.

→ Document - term matrix

	book	daily	read	ticket	work
D ₁	1		1	1	0 0
D ₂	1		0 0	1	0
D ₃	0		1 1	0 1	0 1

Also known as boolean representation of corpus or bag-of-words (BoW)

→ TF = Term - frequency representation
TFIDF = alternative to doc-term matrix

> Problems with document-term matrix

- Assume 1 billion docs \times 50 billion terms
- And sparse matrix - most values are zeros.

Drawbacks - frequency of word count
- order of words



Inverted Indexing Term - Frequency Representat.

D ₁	D ₂	Relevance
t ₁ = 180	t ₁ = 134	2
t ₂ = 180	t ₂ = 5	-
t ₃ = 5	t ₃ = 8	3

t₁ A term is present in most of the documents in the corpus.

t₂ A term is present in a single document several times and rarely found in others.

t₃ A term is present in very few documents of the corpus.

Drawbacks - TF cannot separate between t₂ and t₁.

→ TF-IDF approach.

DF = document frequency.

Number of documents in which this term front

IDF(t_i) = kind of weight - such that it captures difference of t_i, t_j

$$= \log \left(\frac{N}{df_i} \right)$$

The intuition behind this is that if a term appears in a large number of documents in a corpus it is probably not important or discriminative.



► Vector-space model. (TF-IDF)

book daily read ticket write

D_1 $\log \frac{3}{2}$ $\log \frac{3}{2}$ $\log \frac{3}{2}$ 0 0

D_2 0 $\log \frac{3}{2}$ 0 0 $\log \frac{3}{2}$ 0

D_3 0 0 $\log \frac{3}{2}$ $\log \frac{3}{2}$ 0 $\log \frac{3}{2}$

Consider D_1, D_2, \dots, D_n as vectors of dimension 5.

This allows us to perform vector operation on these and perform document classification, document similarity, document clustering etc.

► There are more advanced representations. word2vec, doc2vec, Wav2vec, GloVe -....

* App of the week - SCIgen.



Innovative Assignment (30 marks)

- Research article / Review Paper
- Implementation of GUI based project

Topic	Team of 1- 3 people	Prepare Report
Founding Areas		- Survey
		- Existing soln
		- Implementation
- Image Captioning (image to text)		
- Reverse of image captioning		
- Text-based question - answering system		
- Visual question - answer system		
- Text - to - speech synthesis		
- Speech - to - text (speech recognition)		
- Document classification		
- Information retrieval from PDF / Documents		
- Voice Biometrics		
- Speaker Digitization		
- Singer Identification		
- Sentiment Analysis from text data		
- Music composer recognition		
- ChatBot / Voice Assistant		
- Text or Audio Summerization		
- Generating speech or music (GAN)		
- Intent detection from audio		
- Speech data collection and some experiments		
- Bird species classification (BirdClap)		
- Text detection and conversion to speech		
- Speech corpus development for gujarati language		
- Voice transformation		
- Audio signal classification		- Tagging Audio data
- Sound calculator		- Talking Calculator



→ Artificial Neural Networks

Dendrites

(Receive signals)

Nucleus

Axon

Processing
element

Biological Neuron

Input lines

 x_4 w_1 w_2

$$\sum f$$

$$\hat{y} = f(\sum(w_i x_i))$$

Output line

Processing
elementwe have to
learn these
parameterssigmoid
relulinear
tanh
elu

hardlimit

$$w_i' = w_i + \Delta w$$



Keywords -

- Vanishing Gradient Problem,

MNIST Dataset - 70,000 images of B&W digits
i.e. classes

Flattening 28×28 700c image / class

Word Embeddings

App of the week -

Wednesday Text Representation:

Text - Bag of words.

- One hot encoding

Labels = {book, daily, read, ticket, write}

$$= \{ [1, 0, 0, 0, 0], [0, 1, 0, 0, 0], [0, 0, 1, 0, 0], [0, 0, 0, 1, 0], [0, 0, 0, 0, 1] \}$$

Problem = sparsity \Rightarrow meaning

- Embeddings



Dimensionality reduction
Attribute subset selection / feature ranking

Principal Component analysis

Linear Discriminant analysis

Auto encoder.

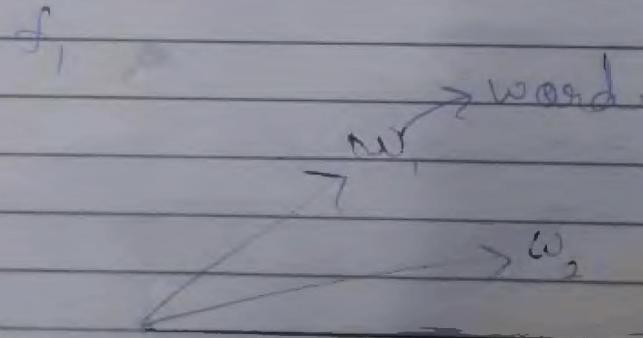
Singular value decomposition

Ref 24/02/2023

→ Embeddings

Embeddings aim to represent the word in a dense vector form.

Making sure that similar words are close to each other in the embedding space.



$f_2 = \text{feature}$

Latent Semantic Indexing

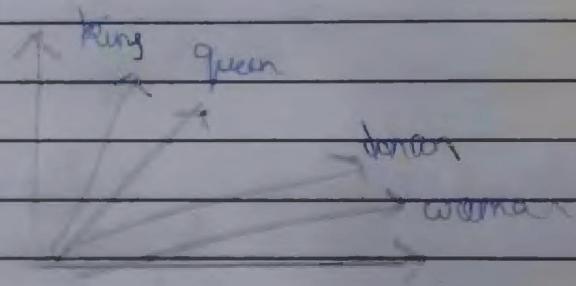
hidden
Implicit

Captures
meaning
content



- Topic modeling - similar words come closer in embedding space
- Cosine similarity is preferred as compared to euclidean distance.
- Vector arithmetic operations on words-

King - man + woman = queen



i) Word 2 Vec - Word To vector
ii) GLoVe - global vectors



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RJ

6/29/23
3/2023

→ Language models

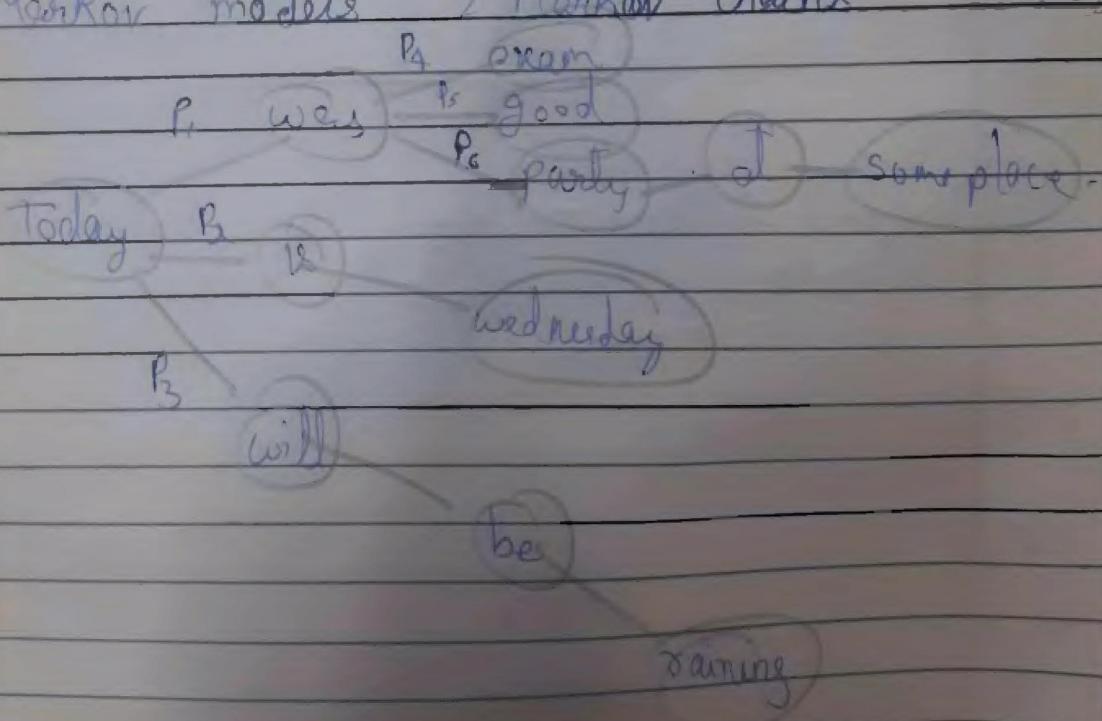
Unigrams = {book, road, ticket, ...}

Bigrams = {book daily, daily road, ...}

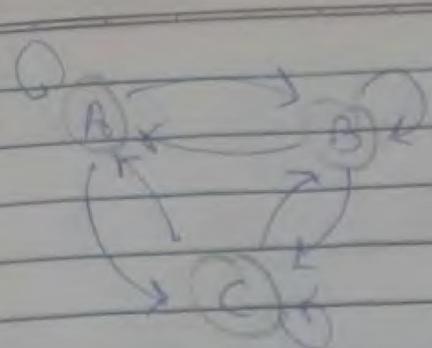
Order is important.

In general N-gram is a representation of language model.

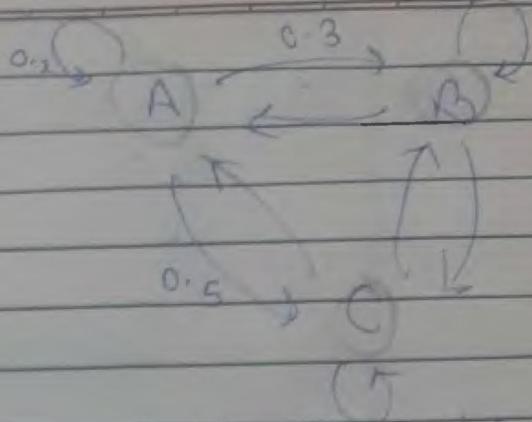
→ Markov models / Markov chains



Markov models are state-transition diagrams with probabilities.



State transition diagram



Markov model

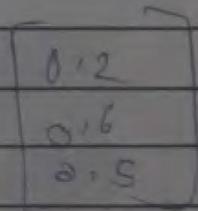
If there are n states, maximum n^2 transition possible.

Summation of probability for each outgoing transition is equal to 1.

Can be represented as $N \times N$ matrix
Diagonals represent probability self loops.
Known as state transition probability matrix.

Deterministic
state

Non deterministic
state



$$P = \begin{bmatrix} 0.5 & 0.1 & 0.4 \\ 0.1 & 0.7 & 0.2 \\ 0.3 & 0.3 & 0.4 \end{bmatrix}$$

16/02/2023
Friday



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	A	B	C	
T	A	0.3	0.1	0.4
	B	0.1	0.7	0.2
	C	0.3	0.3	0.4

$$P = [0 \ 1 \ 0]_{n \times 3}$$

$$I = [0.1 \ 0.7 \ 0.2]_{3 \times 3}$$

$$P_1 = [0.18 \ 0.56 \ 0.26]_{3 \times 3}$$

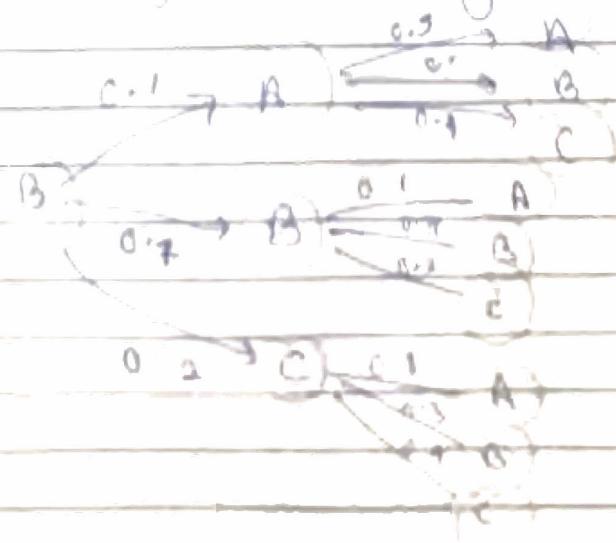
↑

$$P(S-A) = P(BAA) + P(BBA) + P(BCA)$$

$$P_2 = P_1 \cdot T = [0.224, 0.488, 0.288]$$

$$P_n = P_{n-1} \cdot T = P_0 T^n$$

→ Probability Tree Diagram



P_0

P_1

P_2

.....



Q) Calculate probability of following state sequence

$$A \xrightarrow{0.3} B \xrightarrow{0.4} A \xrightarrow{0.3} C =$$

Q) Calculate probability of achieving state C
assuming you start with same state

$$P(C \dots C)$$

$$P_1 A = [1 \ 0 \ 0]$$

$$P_2 AC = [0.3 \ 0.3 \ 0.4]$$

$$P_3 ACB = [0.34 \ 0.34 \ 0.26]$$

$$P_4 ACBA = [0.262 \ 0.346 \ 0.292]$$

$$P_5 ACBAB = [0.2532 \ 0.356 \ 0.2908]$$

$$P_6 ACBABAC = [0.25 \ 0.35 \ 0.3]$$

A → C → B → A → C → B

$$= 0.00144$$

$$\times \quad \times \quad \times \quad \times$$

$$P_7 = [0.2472 \ 0.4504 \ 0.3024]$$

$$P_8 = [0.25936]$$



$$A \Rightarrow P(C \mid A) = P_0 = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}$$

$$P_1 = \begin{bmatrix} 0.3 & 0.3 & 0.4 \end{bmatrix}$$

$$P_2 = \begin{bmatrix} 0.3 & 0.31 & 0.34 \end{bmatrix}$$

$$P_3 = \begin{bmatrix} 0.288 & 0.374 & 0.328 \end{bmatrix}$$

$$\alpha \quad \alpha \quad \alpha \quad \alpha$$

$$T = \begin{matrix} & A & B & C \end{matrix}$$

$$\begin{matrix} A & \begin{bmatrix} 0.5 & 0.1 & 0.4 \end{bmatrix} \\ B & \begin{bmatrix} 0.1 & 0.7 & 0.2 \end{bmatrix} \\ C & \begin{bmatrix} 0.3 & 0.3 & 0.4 \end{bmatrix} \end{matrix}$$

$$P_0 = \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}$$

$$P_1 = \begin{bmatrix} 0.1 & 0.7 & 0.2 \end{bmatrix}$$

$$P_2 = \begin{bmatrix} 0.18 & 0.56 & 0.26 \end{bmatrix}$$

$$P_3 = \begin{bmatrix} 0.224 & 0.488 & 0.288 \end{bmatrix}$$

$$P_4 = \begin{bmatrix} 0.2472 & 0.4504 & 0.3024 \end{bmatrix}$$

$$P_5 = \begin{bmatrix} 0.25936 & 0.43072 & 0.30992 \end{bmatrix}$$

$$P_6 = \begin{bmatrix} 0.265728 & 0.420416 & 0.319856 \end{bmatrix}$$

$$P_7 = \begin{bmatrix} 0.2690624 & 0.4150208 & 0.3159168 \end{bmatrix}$$

$$P_8 = \begin{bmatrix} 0.27080832 & 0.41219594 & 0.31699584 \end{bmatrix}$$

$$P_9 = \begin{bmatrix} 0.271722496 & 0.410716672 & 0.317560912 \end{bmatrix}$$



2) A markov chain is used to model the status of equipment and having following possible states:

idle and awaiting work I
working on a task W
broken B
in repair R

The machine is monitored at regular intervals to determine its status,

assume that status is monitored every hour

	I	W	B	R	
T =	I	0.05	0.93	0.02	0
	W	0.10	0.86	0.04	0
	B	0	0	0.8	0.2
	R	0.5	0.1	0	0.4

i) find that machine is working after 1 hour if it is idle now.

$$P(W|I) = P(IW) = 0.93$$

$$(ii) P(IIW) = 0.1$$

$$(iii) P(B-R) = 0.24$$

$$\begin{aligned} P_0 &= [0 \ 0 \ 1 \ 0] \\ P_0 &= [0 \ 0.93 \ 0.04 \ 0] \end{aligned}$$

$$P_1 = [0.1 \ 0.02 \ 0.64 \ 0.24]$$

(iv) In next five hours, states is

IWNIB

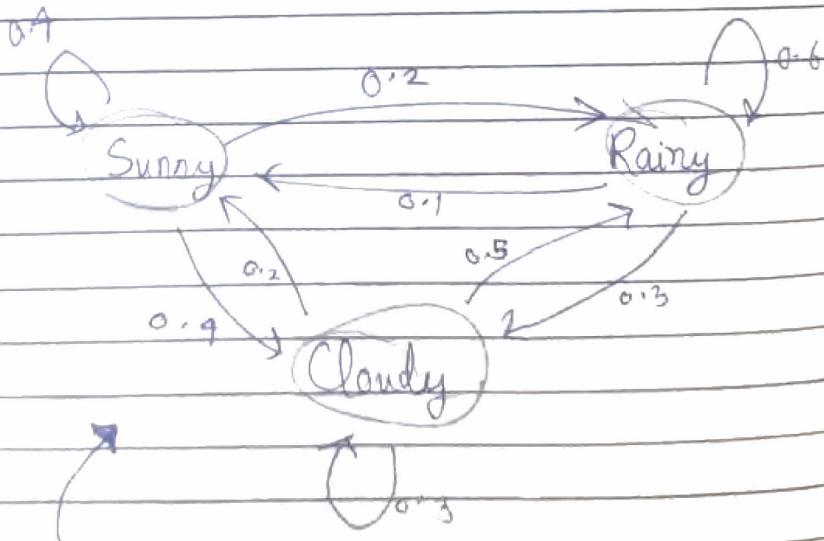
$$= (0.93)(0.86)(0.1)(0.02)$$

$$= 0.0015$$

→ Hidden Markov Models (HMM)

- Applications - Next word prediction.
- Any data which has sequence of states can be modeled as HMM.

→ Weather Example.



Nothing is hidden (observable markov model)



In hidden markov models - state is not given. Only probability is available.

Example : Tomorrow is cloudy - 0.3

↳ what is current state?

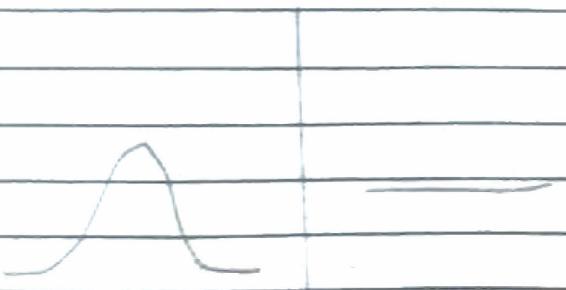
Related to Bayes Theorem / Probability distribution

Condition of evidence

Posterior = $\frac{\text{likelihood} \times \text{prior}}{\text{evidence}}$

$$P(A|B) = \frac{P(B|A) \times P(A)}{P(B)}$$

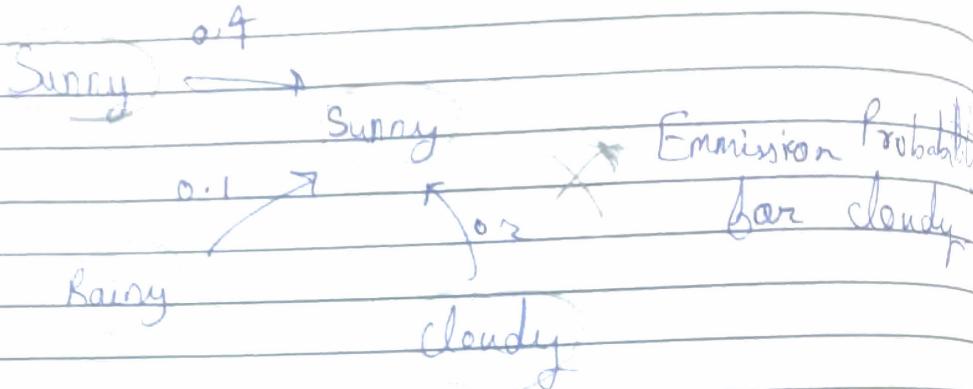
Types of distribution.



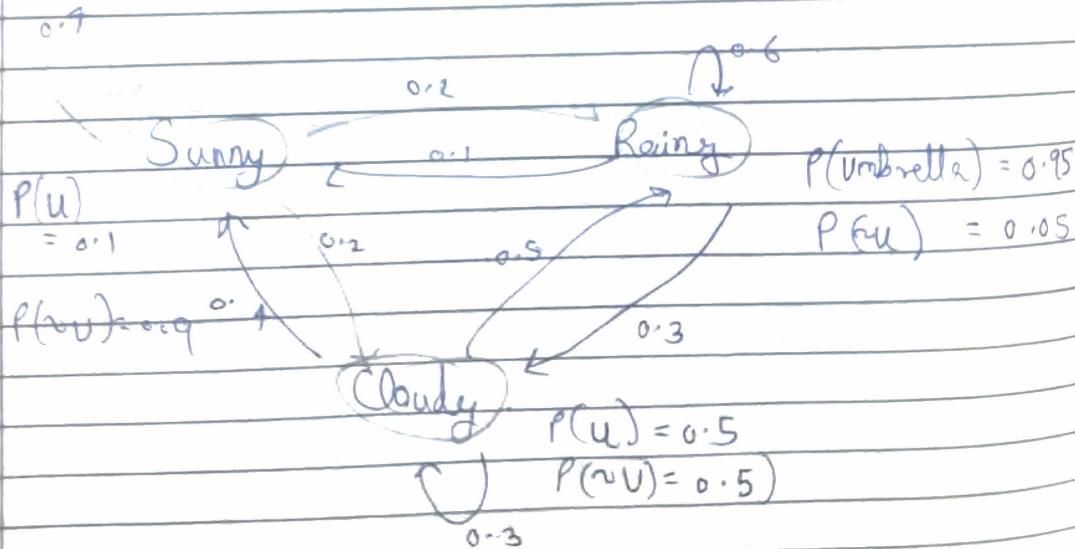
Types of ML models

- Discriminative
- Generative

HMM is useful for



- HMM : If today is sunny, which state could have resulted to today





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HMM has 3 parameters:

- B) i) Emission probability matrix (can be more than 1)
- π) ii) Initial probability vector.
- A) iii) Transition probability matrix.

$$\lambda = \{A, B, \pi\}$$

Hidden Markov Models (Continued)

- State sequence notation.

q_1, q_2, \dots where $q_i \in \{\text{Sunny, Rainy, Cloudy}\}$

- In order to compute prob. for tomorrow's state we can use markov property.

$$P(q_1, \dots, q_n) = \prod_{i=1}^n P(q_i | q_{i-1})$$

* Not dependent on all previous state

But only on immediate previous state:

$$P(q_3 | q_2, q_1) = P(q_3 | q_2)$$

- It is stochastic model which models temporal or sequential data.
- A way to model dependencies of current information with previous information.
- Stochastic = Non-deterministic process.
- Example:

- o_i is observation on i th day
- We have observation sequence $o_1, o_2 \dots o_t$
- we need to find probability that corresponding state sequence is $q_1, q_2 \dots q_t$
- $P(q_1, q_2 \dots q_t | o_1, o_2 \dots o_t) = P(o_1, o_2 \dots o_t | q_1, q_2 \dots q_t) P(q_1, q_2 \dots q_t)$

(i.e.) $P(q_i | o_i) = \frac{P(o_i | q_i) P(q_i)}{P(o_i)}$

$P(q_i | o_i) \propto \prod_{l=1}^t P(o_l | q_i) \prod_{l=1}^{t-1} P(q_l | q_{l-1})$

HMM Parameters

transition Probabilities

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Red Coin

$$P(H) = 0.9$$

$$P(T) = 0.1$$

Green Coin

$$P(H) = 0.95$$

$$P(T) = 0.05$$

missions

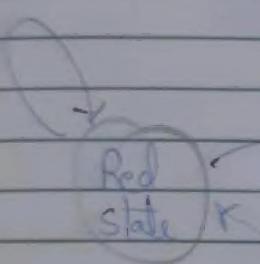
Red dice

$$\{1, 2, 3, 4, 5, 6\}$$

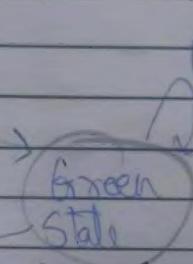
Green Dice

$$\begin{cases} \{1, 1, 1, 1, 1, 1\} \\ 2, 3, 4, 5, 6 \end{cases}$$

$P(H | \text{Red Coin})$



$P(T | \text{Red coin})$



$P(H | \text{Green coin})$

$P(T | \text{Green coin})$

$$A = \begin{bmatrix} 0.9 & 0.1 \\ 0.05 & 0.95 \end{bmatrix}_{2 \times 2}$$

$N = \max \text{ no. of emissions}$

$$N = 6$$

$$\pi = \begin{bmatrix} 1 \\ 0 \end{bmatrix}_{2 \times 1}$$

$N = \text{no. of states}$

$$N = 2$$

$$B = \begin{bmatrix} \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} \\ \frac{7}{12} & \frac{1}{12} & \frac{1}{12} & \frac{1}{12} & \frac{1}{12} & \frac{1}{12} \end{bmatrix}_{2 \times 6}$$

- In forward, we cannot determine exact value of parameters.
- Hence, we need to estimate the parameters.
- Parameter Estimation
 - Viterbi algorithm
 - Forward algorithm (Ref # 15/03/2023)
 - Baum - Welch Algorithm. (")



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$\vec{u} = \vec{u}_1 + \vec{u}_2 + \vec{u}_3 + \vec{u}_4$

$$\begin{bmatrix} 2 \\ 3 \\ 2 \end{bmatrix} + \begin{bmatrix} 1 \\ 4 \\ 8 \end{bmatrix} + \begin{bmatrix} 0 \\ 5 \\ -3 \end{bmatrix} + \begin{bmatrix} 7 \\ 4 \\ 6 \end{bmatrix}$$

3x4

$$\|\vec{u}\| = \sqrt{2^2 + 3^2 + 2^2} = \sqrt{17}$$

\rightarrow The Euclidean norm of vector

2nd Norm

Orthogonal matrix \rightarrow Each ^{column} vector is perpendicular to each other.

$$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

Unit vector.

Normalization $[2, 4, 1] \rightarrow \left[\frac{2}{\sqrt{21}}, \frac{4}{\sqrt{21}}, \frac{1}{\sqrt{21}} \right]$

Ortho Normalization
(Ortho + normal)

$$\begin{bmatrix} \frac{1}{\sqrt{2}} & 0 & 0 \\ 0 & \frac{1}{\sqrt{2}} & 0 \\ 0 & 0 & 1 \end{bmatrix} \Rightarrow$$



→ Matrix factorization

$24 \rightarrow 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$

* LU Decomposition

- (Lower - upper) Decomposition:

$$A = \begin{matrix} L \\ U \end{matrix} \xrightarrow{\text{LUD}} \begin{matrix} \text{Lower} \\ \text{triangular matrix} \end{matrix} \quad \begin{matrix} \text{Upper} \\ \text{triangular matrix} \end{matrix}$$

LUD

Ref: 08/02/2023

* Singular value decomposition

$$A = \underline{U} \underline{S} \underline{V}^T \quad \begin{matrix} \text{Diagonal matrix (square)} \\ \text{Orthonormal matrix} \end{matrix}$$

- Used for Dimensionality reduction
- Used for latent semantic indexing

$$A = \underline{U} \underline{S} \underline{V}^T$$

$\frac{500 \times 4000}{\text{documents vocabulary}} \xrightarrow{\quad} \frac{500 \times 1000}{\quad} \xrightarrow{\quad} \frac{1000 \times 1000}{\quad} \xrightarrow{\quad} \frac{4000 \times 1000}{\text{feature matrix}}$



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Hyperparameters

$K = 1000, 1001 \dots \uparrow \downarrow$, reconstruct A ,

find score, rank of SVD:

- $S = \begin{pmatrix} s_1 & 0 & 0 & 0 \\ 0 & s_2 & 0 & 0 \\ 0 & 0 & s_3 & 0 \\ 0 & 0 & 0 & s_n \end{pmatrix}$

← most colinear
↓ least colinear
↓ singular values

- Lower rank approximation.

- Eigen value (prerequisite)

- $A \vec{v} = \lambda \vec{v}$

Eigen value Eigen vector

- $\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = \begin{bmatrix} 2v_1 \\ 2v_2 \end{bmatrix}$

- $v_1 + v_2 = 2v_1 \quad \left. \begin{array}{l} (1-2)v_1 + v_2 = 0 \\ v_1 + (1-2)v_2 = 0 \end{array} \right\}$

- $1 - 2 + 1 = 0 \quad \left. \begin{array}{l} 1 - 2 + 1 = 0 \\ 1 - 2 = 0 \end{array} \right\} = 0$

~~$\lambda =$~~ $\lambda = 0, 12$



- For $\lambda = 12$,

$$\begin{array}{l|l} (11 - \lambda) v_1 + v_2 = 0 & \\ -v_1 + v_2 = 0 & | \quad v_1 - v_2 = 0 \end{array} ?$$

$$v_1 = v_2 \quad \text{Infinite } [1, 1], [2, 2], \dots$$

- For $\lambda = 10$,

$$\begin{array}{l|l} v_1 + v_2 = 0 & | \quad v_1 + v_2 = 0 \end{array} ?$$

$$v_1 = -v_2 \quad \infty [1, -1], [2, -2], \dots$$

- Process of SVD

• The columns of \tilde{U} are orthonormal eigenvectors of $A \cdot A^T$

$$A \cdot A^T$$

• Columns of \tilde{V} are orthonormal eigenvectors of $A^T \cdot A$

$$A^T \cdot A$$

• S is a diagonal matrix which contains square roots of Eigen values from U or V in descending order.



$$\textcircled{Q} \quad A = \begin{bmatrix} 3 & 1 & 1 \\ -1 & 3 & 1 \end{bmatrix}_{2 \times 3}$$

$$A^T = \begin{bmatrix} 3 & 1 & 1 \\ 1 & 3 & 1 \end{bmatrix}_{3 \times 2}$$

$$\blacktriangleright A \cdot A^T = \begin{bmatrix} 9+1+1 & -3+3+1 \\ -3+3+1 & 1+9+1 \end{bmatrix}_{2 \times 2} = \begin{bmatrix} 11 & 1 \\ 1 & 11 \end{bmatrix}_{2 \times 2}$$

$$\textcircled{U} \quad \lambda = 10, 12 \quad \boxed{12, 10}$$

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \xrightarrow{\text{norm}} \begin{bmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{bmatrix}$$

$$\blacktriangleright A^T \cdot A = \begin{bmatrix} 9+1 & 3-3 & 3-1 \\ 3-3 & 1+9 & 1+3 \\ 3-1 & 1+3 & 1+1 \end{bmatrix}_{3 \times 3}$$

$$= \begin{bmatrix} 10 & 0 & 2 \\ 0 & 10 & 4 \\ 2 & 4 & 2 \end{bmatrix}_{3 \times 3}$$

$$10V_1 + 2V_2 = 2V_1 \\ 10V_1 + 4V_3 = 3V_2 \\ 2V_2 + 4V_3 = 2V_3$$

$$\textcircled{V} \quad \lambda = 12, 10, 0$$

$$\begin{bmatrix} 1 & -2 & 0 \\ 2 & 1 & 2 \\ 1 & 0 & -5 \end{bmatrix} \xrightarrow{\text{norm}} \begin{bmatrix} \frac{1}{\sqrt{5}} & 0 & \frac{1}{\sqrt{5}} \\ \frac{2}{\sqrt{5}} & \frac{1}{\sqrt{5}} & \frac{2}{\sqrt{5}} \\ \frac{1}{\sqrt{5}} & 0 & -\frac{1}{\sqrt{5}} \end{bmatrix}_{3 \times 3}$$



$$S = \begin{bmatrix} \sqrt{12} & 0 \\ 0 & \sqrt{10} \end{bmatrix}_{2 \times 2}$$

$$S = \begin{bmatrix} \sqrt{12} & 0 & 0 \\ 0 & \sqrt{10} & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Calculation
for V

$$10V_1 + 0V_2 + 2V_3 = 2V_1$$

$$0V_1 + 10V_2 + 4V_3 = 2V_2$$

$$2V_1 + 4V_2 + 2V_3 = 2V_3$$

$$\begin{vmatrix} 10-2 & 0 & 2 \\ 0 & 10-2 & 4 \\ 2 & 4 & 2-2 \end{vmatrix} = 0$$

$$(10-2)(20+2^2-12\lambda - 16) + \\ -2(20-2\lambda) = 0$$

$$(10-2)[(2^2-12\lambda+4) + 4] = 0$$

$$(10-2)(2^2-12\lambda+8) = 0$$

$$2(10-2)(2-12) = 0$$

$$\lambda = \frac{12 \pm \sqrt{144-16}}{2}$$

$$\lambda = 0, 10, 12$$

$$\lambda = 12 \pm \sqrt{16}$$

$$\lambda = 12, 10, 0$$



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→ $U_{2 \times 1} \cdot S_{1 \times 2} \cdot K_{3 \times 3}^T$ = should give $A_{2 \times 3}$

↓ → ↓

Not compatible.

∴ Change S →

$$\begin{bmatrix} J_{12} & 0 & 0 \\ 0 & J_{10} & 0 \\ 0 & 0 & 0 \end{bmatrix}_{2 \times 3}$$

10/03/2023
Friday



documents

D

rank

k

D

k

K

Terms

$$T = T \cdot \circ$$

$$A_k = U_k \cdot S_k \cdot V_k^T$$



Dynamic Programming

Reuse values from previous calculations

Ref # 24/02/2023

Parameter estimation for HMM

- 1 Viterbi Algorithm (Ref # 15/03/2023)
- 2 Forward Algorithm (Ref # 15/03/2023)
- 3 Baum Welch Algorithm (Ref # 15/03/2023)



Expectation Maximization (EM Algorithm)

~~Note~~

K Means is hard - clustering algo.

Hard clustering - One point belongs to only one cluster.

Soft clustering - Overlapping clusters.

→ fuzzy clustering } probabilistic

→ EM Algorithm is soft clustering algorithm.

X Hidden Markov Models.

π 1 Initial probability vector

q 2 # states

A 3 state transition prob - matrix } Also in Observable markov models.

B 4 Emission probability matrix

V + 5 Observation from each state

Notation: $q_1, q_2 \dots q_n$

$Q_1, Q_2 \dots Q_n$

} states

- q_{ij} = transition probability from q_i to q_j

- $O = o_1, o_2, o_3 \dots o_n$ } observation

- $B = [b_i(v_1) \dots]$

- probability that observation v_i is emitted by state q_i