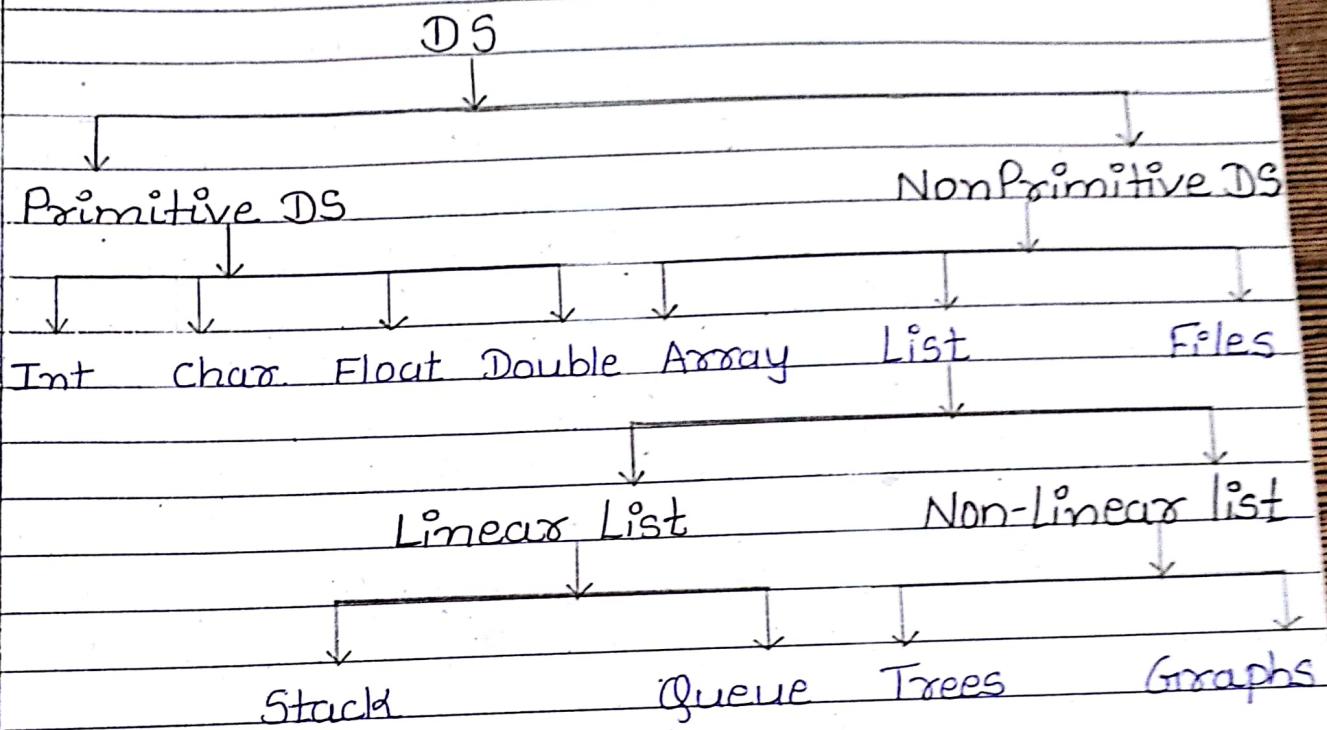


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## Introduction

Data Structure is a particular way of organizing a data in a computer. So it can be used efficiently.



### Primitive Data Structure

Primitive Data Structure are provided by a programming language as a basic building block. This are also known as building types or basic type or primary data structure.

Ex: int, ch, float, double, etc

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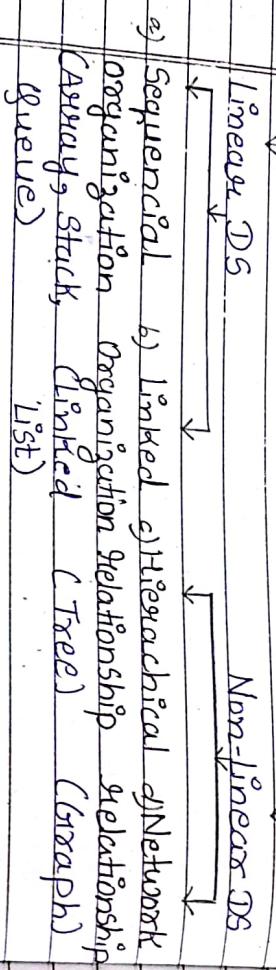
## Non-Primitive Data Structure (Abstract DS)

The data structure which is derived from primitive data structure are known as Non-Primitive Data structure.

Ex: Array, Stack, Queue, Union, structure, Link List, Tree, Graph, etc.

**NOTE** > This all data structure allows to perform different operation on data. We select this DS based on which type of operation is required.

### Types of Data Structure



In Linear Data Structure the elements are stored in sequential order. It means if we know the address of first data item then we can get the second one & so on.

- 1) **Linear DS**
  - 2) **Non-linear DS**
    - a) **Sequential**
    - b) **Linked** (Hierarchical Network Organization, Relationship, C)
- POP :** This Operation delete the element from the Stack
- PEEP :** Peep Operation returns the value of top most element of the Stack.
- Application**
- Reverse the String
  - Expression Conversion
- $\xrightarrow{\text{Infix}} \text{Postfix} \xrightarrow{\text{Postfix}}$
- Paring

In sequential organization elements occupy continuous or consecutive memory location.

In this data structure components are accessed in certain sequence but they are not necessarily stored in consecutive memory location. It uses a pointer which shows the relationship between the elements with the help of links.

### STACK (LIFO)

**Overflow Condition** =  $\text{TOP} \geq \text{Max}$   
**Underflow Condition** =  $\text{TOP} = 0$



**PUSH** : To insert or add the element into the Stack

→ Disadvantage  
Slow access to other element

Interrups are handle in the same order as  
Linked List . they come

## Linked List

they come.

Queue (FIFO)

	1	2	3	4	5
F = D	1	20	30	40	50
R = D					
F					

Enqueue → means insertion or addition.

dequeue  $\rightarrow$  deletion or removal of an element in a queue

## Simple Queue

卷之三

Overflow       $R \geq \max$

**Underflow**     $E=R=0$       }  $F \neq 0$   
**overflow**    If  $R > \max F, R = 1$  }  $C$ ircular  
                  queue

## Application

## → CPU task Scheduling

$\rightarrow$  Keyboard buffer

#### Queue of request at Web Server.

- Interrupts are handled in the same order as they come.

  1. Singly Linked List
  2. Doubly Linked List
  3. Circular Linked List

(Dynamic memory allocation) links of next

**Singly Linked List**

10	2000	→	50	30	→	30	1
100	2000		100	50	200	200	30

**Doubly Linked List**

10	300	→	20	500	→	30	100
100	300		200	500		300	100

**Circular Linked List**

Linked List is a collection of item in which each item is linked with other and order is given by means of links from one item to another. Each item is denoted by node which consist of two field.

**Advantages**

  - It is a dynamic data structure in which the element can be added or deleted from anywhere on the list.
  - In linked list ~~not~~ need not to worry about how many element will be stored in the linked list.
  - In linked list each element is allocated

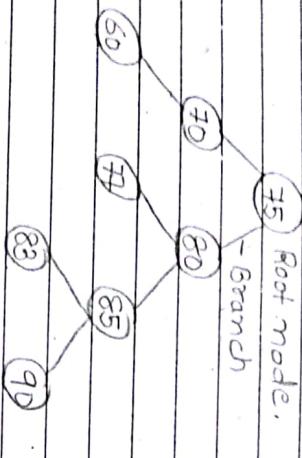
### Disadvantage

- It requires more memory and slow
- Search operations.
- Reverse traversing is difficult

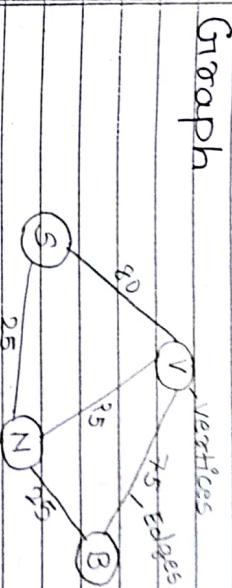
Application  
- It is used to implement Stack,  
Queue, Graph, Trees.

### Tree

It is a Non-linear DS in which data items called nodes are arranged in same sequence.



75 Root node.  
- Branch



### Graph

Application  
Telephone directory assistance information stored in a tree so name & no. can be quickly find out.

TREE CONTAIN PURELY PARENT - CHILD RELATIONSHIP.

It is basically a collection of vertices and edges that connect this vertices. It is a generalization of tree structure i.e. instead of having purely parent & child relationship b/w tree node, any kind of complex relationship b/w the vertices can be representative.

Element can be located very quickly in tree.

Insertion is fast.

Disadvantage  
Deletion algorithm is complex.

### Application

- Node can represent city & edges can represent road since it can be used in GPS.
- A Graph can also used to represent Computer memory where nodes are called station & edges are memory connection. So it can be used in work station.

### Disadvantage

- Some algorithm are slow & very complex.

### Performance analysis & Asymptotic notation

Performance Analysis of an algorithm is a process of calculating Space required by that algorithm and time required by that algorithm. Part of an algorithm is concerned by using the following measures:

- Space complexity
- Time Complexity

⇒ Total amount of computer memory required by an algorithm to complete its execution is called as Space complexity of that algm.

For any algorithm memories required by foll. purpose

- i) Memory required to store program, instruction or structure.
- ii) Memory required to store constant values.
- iii) Memory required to store variable.

Ex: void add (int n)

{

return n+n;

}

size n → 2 bytes  
for returning, 2 bytes  
Stack.

Total → 4 bytes.

If algorithm requires a fixed amount of space for all input values then that space complexity said to be Constant Space Complexity.

int sum (int A[], int n)

{

int sum=0;  
for (i=0; i<n; i++)  
sum = sum + A[i];  
return sum;

}

$n$  Space = 2 byte  
 $A[1]$  Space =  $2 \times n$  byte  
 Sum Space = 2 byte  
 $i$  Space = 2 byte  
 return Space = 2 byte  
 Total =  $2n + 8$  byte

If the amount of Space required by an algorithm is increase with increase of input value then the Space complexity is said to be linear Space Complexity.

ii)  $\Rightarrow$  Total amount of time required by an algorithm to complete its execution is called as Time Complexity.

To calculate the time complexity we check only how our program is behaving further diff. Input Values to perform all the operation like arithmetic, logical, assignment, any return Value operation, etc.

If any program require fixed amount of time for all input Values then its time complexity is said to be Constant time complexity. and th if amount

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of time required by an algorithm is increase with the increase in value then that type of complexity is said to be linear time complexity.

Three types of asymptotic notation

1. Big Oh ( $O$ )  $\rightarrow$  max. amount of time reqd. by alg. defines upperbound of alg.
2. Big Omega ( $\Omega$ )  $\rightarrow$  min. amount
3. Big Theta ( $\Theta$ )  $\rightarrow$  avg.

i. It describes the worst case of an algo.

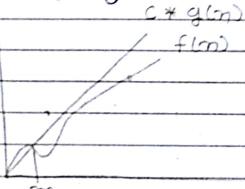
$$f(n) = O(g(n))$$

$f(n) \leq C * g(n)$  for every  $(n > n_0)$

$C = \text{some real constant}$

$f(n) = \text{algo runtime}$

$g(n) = \text{arbitrary time complexity you are trying to relate to your algo.}$

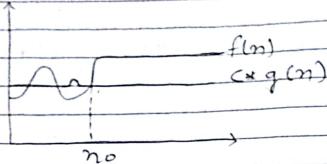


ii. It describes the best case of an algo.

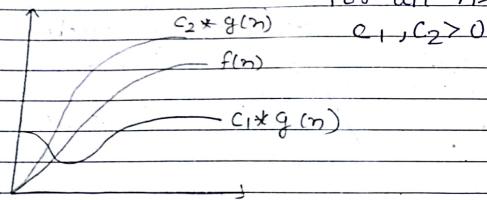
$$f(n) = \Omega(g(n))$$

$f(n) \geq c * g(n)$  for every input size  $n$  ( $n > n_0$ )

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3.  $0 \leq c_1 * g(n) \leq f(n) \leq c_2 * g(n)$   
 for all  $n \geq n_0$



Calculate the time Complexity

fun(n)

{  
 for (i=1; i <= n; i++)

{  
 printf ("Hello"); n

}

$3n + 2$   
 $O(n)$

fun(n)

{  
 for (i=1; i <= n; i = i+2)

{  
 printf ("Hi"); n/2

}

$\frac{3n+2}{2}$        $n=1$

{  
 for (i=1; i < n; i++)

{  
 for (j=1; j < n; j++)

{  
 printf ((i\*j) - j\*(n-1) != n

}

$14n^2 + n - 1 + n - 1 + n^2 - n$   
 $n^2 - 2n + 1 + n^2 - n$

$3n^2 - n$   
 $O(n^2)$

$i=1$

$j=1$   
 $j=2$   
 $j=3$   
 $j=4$

$i=4$   
 $= n-1$

$i=2$

$n-1$

$i=3$

|

)

Date:

Write an Algorithm to insert an element in simple Queue.

Procedure QINSERT (Q, F, R, N, Y)

F & R = It is a pointer which points to front of rear elements of the Queue.  
 $Q = \text{queue}$ .

N = Number of element in queue.  
 Y = element which is to be inserted  
 initially F & R set to zero

1. [Overflow?]

if  $R \geq N$

then write ('overflow')

Return

2. [Increment rear Pointer]  
 $R \leftarrow R + 1$

3. [Insert Element]

$Q[R] \leftarrow Y$

4. [Is front Pointer Property Set?]

1)  $F = 0$  then  $F \leftarrow 1$   
 Return

1 2 3 4 5

FR.

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(i)  $R = 0, Y = 5, N = 5, F = 0$

1. [Overflow?]

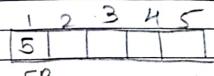
$0 \neq 5$   
 False

2.  $R = 1$

3.  $Q[1] = 5$

4.  $F = 0$

$F = 1$



FR.

(ii)  $R = 1, Y = 10, N = 5, F = 1$

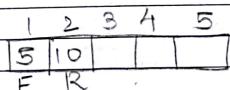
1.  $1 \geq 5$   
 False

2.  $R = 2$

3.  $Q[2] = 10$

4.  $F = 0$

False



(iii)  $R = 2, Y = 15, N = 5, F = 1$

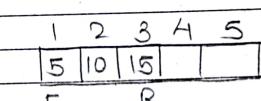
1.  $2 \geq 5$   
 False

2.  $R = 3$

3.  $Q[3] = 15$

4.  $F = 0$

False



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(iv)  $R = 3, Y = 20, N = 5, F = 1$

1.  $3 > 5$

False

2.  $R = 4$

3.  $Q[4] = 20$

4.  $F == 0$ 

1	2	3	4
5	10	15	20
F            R			

False

(v)  $R = 4, Y = 25, N = 5, F = 1$

1.  $4 > 5$

False

2.  $R = 5$

3.  $Q[5] = 25$

4.  $F == 0$ 

1	2	3	4	5
5	10	15	20	25
F            R				

False

(vi)  $R = 5, Y = 30, N = 5, F = 1$

1.  $5 > 5$

True

Overflow

Date:

Draw a simple queue with 6 memory shell which has Front & Rear at zero position. Draw the simple queue structure & represent the position of front & rear pointer for each of the foll. operation.

Insert a, b, c, d, e, f, g

1 2 3 4 5 6

F R

1.  $R = 0, N = 6, Y = a, F = 0$

(i) if  $R \geq N$

$\rightarrow 0 \geq 6$

False.

(ii)  $R = 1$

(iii)  $Q[1] = a$

(iv)  $F == 0$

$\rightarrow F = 1$

1 2 3 4 5 6  
a . . . . .

F R

2.  $R = 1, N = 6, Y = b, F = 1$

(i) if  $R \geq N$

$\rightarrow 1 \geq 6$

False.

(ii)  $R = 2$

(iii)  $Q[2] = b$

(iv)  $F == 0$

False.

1 2 3 4 5 6  
a b . . . .

F R

3.  $R=2, N=6, Y=c, F=1$

(i) if  $R \geq N$   
 $2 \geq 6$ .  
False

L(i)	$R=3$	1 2 3 4 5 6
(ii)	$Q[3]=c$	$ a b c  \quad   \quad  $
(iv)	$F=0$	F R

4.  $R=3, N=6, Y=d, F=1$

(i) if  $R \geq N$   
 $3 \geq 6$   
False

(ii)	$R=4$	1 2 3 4 5 6
(iii)	$Q[4]=d$	$ a b c d  \quad  $
(iv)	$F=0$	F R

5.  $R=4, N=6, Y=e, F=1$

(i) if  $R \geq N$   
 $4 \geq 6$   
False

(ii)	$R=5$	1 2 3 4 5 6
(iii)	$Q[5]=e$	$ a b c d e  \quad  $
(iv)	$F=0$	F R

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6.  $R=5, N=6, Y=f, F=1$

(i) if  $R \geq N$   
 $5 \geq 6$   
False

(ii)	$R=6$	1 2 3 4 5 6
(iii)	$Q[6]=f$	$ a b c d e f $
(iv)	$F=0$	F R

7.  $R=6, N=6, Y=g, F=1$

(i) if  $R \geq N$   
 $6 \geq 6$   
True

(ii)  
(iii)  
(iv)

### Deletion Algo (DEQUEUE)

Procedure QDELETE(Q, F, R)

Q = Queue

F & R = Pointers which points in front of rear

y = Temporary Variable

[underflow?]

if  $F=0$

then write ('UNDERFLOW')

Return(0)

2. [Delete element]  
 $y \leftarrow Q[F]$

3. [Queue empty?]  
if  $F == R$   
then  $F \leftarrow R \leftarrow 0$   
else  
 $F \leftarrow F+1$

4. [Return element]

Return  $y$

	1	2	3	4	5
	10	20	25	30	40

Deletion

F R

1.  $F=1, R=5$

$1 \neq 0$

False

$y = Q[1]$

$y = 10$

$1 \neq 5$  False

$F = 1+1 = 2$

$y = 10$

	1	2	3	4	5
	20	25	30	40	

F R

2.  $F=2, R=5$

$2 \neq 0$

False

$y = Q[2]$

$y = 20$

$2 \neq 5$  False

$F = 2+1 = 3$

$y = 20$

1 2 3 4 5

F R

3.  $F=3, R=5$

$3 \neq 0$

False

$y = Q[3]$

$y = 25$

$3 \neq 5$  False

$F = 3+1 = 4$

$y = 25$

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1	2	3	4	5
		30	40	

FR

4.  $F=4, R=5$

$4 \neq 0$

False

$y = Q[4]$

$y = 30$

$4 \neq 5$  False

$F = 4+1 = 5$

$y = 30$

1	2	3	4	5
		40		

FR

5.  $F=5, R=5$

$5 \neq 0$

False

$y = Q[5]$

$y = 40$

$5 == 5$

True

$F=0, R=0$

$y = 40$

1	2	3	4	5

FR

Consider the Simple Queue given below with 8 memory shell, which has  $F=2$ ,  $R=3$ . Draw the Simple Queue Structure & represent the position of Front & Rear pointers for each of the foll. operation

- 1) Insert c & d
- 2) Delete one alphabet
- 3) Insert e & f
- 4) Delete one alphabet
- 5) Insert g & h.



a)  $F=2, R=3, N=8, Y=c$   
 $3 \neq 8$   
 False

$$R = 3 + 1 = 4$$

$$Q[4] = Y$$

$$Y = c$$

$$2 \neq 0$$

False

b)  $F=2, R=4, N=8, Y=d$   
 $4 \neq 8$   
 False

$$R = 4 + 1 = 5$$

$$Y = Q[5]$$

$$Y = d$$

$$2 \neq 0$$

False

2.  $F=2, R=5$   
 $2 \neq 0$   
 False  
 $Y = Q[2]$   
 $Y = a$   
 $2 \neq 0$   
 False  
 $F = 2 + 1 = 3$   
 $Y = a$

3. a)  $F=3, R=5, N=8, Y=e$   
 $5 \neq 8$   
 False  
 $R = 5 + 1 = 6$   
 $Y = Q[6]$   
 $Y = e$   
 $3 \neq 0$   
 False

b)  $F=3, R=6, N=8, Y=f$   
 $6 \neq 8$   
 False  
 $R = 6 + 1 = 7$   
 $Y = Q[7]$   
 $Y = f$   
 $3 \neq 0$   
 False

4.  $F=3, R=7$   
 $3 \neq 0$   
 False  
 $y = Q[3]$   
 $y = b$   
 $3 \neq 7$   
 $F = 3 + 1 = 4$   
 $y = b$

5. a)  $F=4, R=7, N=8, y=g$   
 $7 \geq 8$   
 False  
 $R=7+1=8$   
 $y = Q[8]$   
 $y = g$   
 $4 \neq 0$   
 False

b)  $F=4, R=8, N=8, y=h$   
 $8 \geq 8$   
 True  
 Overflow

Procedure ( $\varnothing$ INSERT ( $F, R, Q, N, y$ )  
 $F \neq R \rightarrow$  Front & Rear pointer  
 $\varnothing \rightarrow$  Queue.  
 $N \rightarrow$  No. of element in queue  
 $y \rightarrow$  element to be inserted.

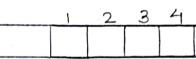
1. [Reset Rear Pointer]  
 if  $R=N$   
 then  $R \leftarrow 1$   
 else  
 $R \leftarrow R+1$

2. [Overflow]  
 if  $F=R$   
 then write ('overflow')  
 Return

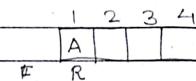
3. [Insert element]  
 $Q[R] \leftarrow y$

4. [Is Front Pointer]  
 $F=0$   
 then  $F \leftarrow 1$   
 Return

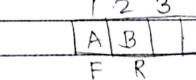
$N=4, y=A, B, C, D$



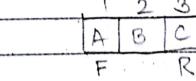
F, R



F, R



F, R



F, R

$0 \neq 4, R=1, Q[1]=A$ .

$1 \neq 4, R=2, Q[2]=B$ ,

$2 \neq 4, R=3, Q[3]=C$ .

$3 \neq 4, R=4, Q[4]=D$

$A = 4, R = 1, I = 1$   
'overflow'

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1	2	3	4
A	B	C	D

1	2	3	4
A	B	C	D

Procedure  $\lceil QDELETE(F, R, Q, N) \rceil$

1. [underflow]

if  $F = 0$   
then write 'UNDERFLOW'.  
Return(0).

2. [Delete element]

$y \leftarrow Q[F]$

3. [Queue empty?]

if  $F = R$

$F \leftarrow R \leftarrow D$

Return(y)

4. [Increment front Pointer]

if  $F = N$

$F \leftarrow 1$

else

$F \leftarrow F + 1$   
return(y)

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### Operation

1. Delete A
2. Insert E
3. Delete B
4. Insert F
5. Delete C, D, E, F

1	2	3	4
A	B	C	D

1)

$I \neq 0$

$y = Q[1]$

$A = y$

$I \neq 4$

$F = F + 1$

$F = 2$

1	2	3	4
	B	C	D

2)

$4 = 4$  True

$R = 1$

$2 \neq 1$  False

$Q[1] = E$

$3 \neq 0$

1	2	3	4
E	B	C	D

3)

$2 \neq 0$

$y = Q[2]$

$y \leftarrow B$

$2 \neq 1$

$F = F + 1$

$F = 3$

1	2	3	4
E	B	C	D

4)  $i \neq 4$   
 $R = R+1$   
 $R = 2$   
 $Q[2] = F$   
 $3 \neq 0$

	1	2	3	4
E	C	D		
	R	F		

5) a)  $3 \neq 0$   
 $Y = Q[3]$   
 $Y = C$   
 $3 \neq 2$   
 $F = F+1$   
 $F = 4$ .

b)  $4 \neq 0$   
 $Y = Q[4]$   
 $Y = D$   
 $4 \neq 2$   
 $F = N$   $4 = 4$  True  
 $F = 1$ .

c)  $1 \neq 0$   
 $Y = Q[1]$   
 $Y = E$   
 $1 \neq 2$   
 $F \neq N$   $1 \neq 4$ .  
 $F = F+1$   
 $F = 2$

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d)  $2 \neq 0$ .  
 $Y = Q[2]$   
 $Y = F$   
 $2 = 2$   
 $F < R < 0$   
 $F = R = 0, F = 1$

1.  $N=6, F=0, R=0$   
2. Insert 5, 10, 15, 20, 25  
3. Delete 5 & 10  
4. Insert 30, 35, 40  
5. Delete 15, 20, 25  
6. Insert 45, 50, 55  
7. Delete 30, 35, 40, 45, 50, 55

1. a)  $F=0, R=0, N=6, Y=5$

$O \neq 6$   
 $R = R+1$   
 $R = 1$   
 $Q[1] = 5$   
 $F = 0, F = 1$

1	2	3	4	5	6
	5				
	R				

b)  $F=1, R=1, N=6, Y=10$

$I \neq 6$   
 $R = R+1$   
 $R = 2$   
 $Q[2] = 10$   
 $F = 1$

1	2	3	4	5	6
5	10				
F	R				

c)  $F=1, R=2, N=6, Y=15$   
 $2 \neq 6$   
 $R = R+1$   
 $= 3$   
 $Q[3] = 15$ ,  
 $F=1$

d)  $F=1, R=3, N=6, Y=20$   
 $3 \neq 6$ .  
 $R = R+1$   
 $= 4$   
 $Q[4] = 20$   
 $F=1$

e)  $F=1, R=4, N=6, Y=25$   
 $4 \neq 6$   
 $R = R+1$   
 $= 5$   
 $Q[5] = 25$   
 $F=1$

2.  
 $1 \neq 0$   
 $Y = Q[1]$   
 $Y = 5$   
 $1 \neq 5$   
 $1 \neq 6$   
 $F = 1+1$   
 $= 2$

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3.  $2 \neq 0$   
 $Y = Q[2]$   
 $Y = 10$   
 $2 \neq 5$   
 $2 \neq 6$   
 $F = 2+1$   
 $= 3$ .

$F = 3, R = 5, N = 6, Y = 30$   
 $5 \neq 6$ .  
 $R = 6$   
 $3 \neq 6$ .  
 $Q[6] = 30$ .  
 $3 \neq 0$ .

$F = 3, R = 6, N = 6, Y = 35$ .  
 $6 = 6$ .  
 $R < 1$   
 $3 \neq 1$   
 $Q[1] = 35$ .  
 $3 \neq 0$ .

$F = 3, R = 1, N = 6, Y = 40$   
 $1 \neq 6$   
 $R = 2$   
 $3 \neq 2$   
 $Q[2] = 40$ .  
 $3 \neq 0$

4.  $E=3, R=2, N=6$   
 $S \neq 0$   
 $Y = Q[3]$   
 $Y = 15$   
 $3 \neq 2$   
 $E = E + 1$   
 $F = 4$

$E=4, R=2, N=6$   
 $4 \neq 0$   
 $Y = Q[4]$   
 $Y = 20$   
 $4 \neq 2$   
 $E = E + 1$   
 $F = 5$

$E=5, R=2, N=6$   
 $5 \neq 0$   
 $Y = Q[5]$   
 $Y = 25$   
 $5 \neq 2$   
 $F = E + 1$   
 $F = 6$

5.  $E=6, R=2, N=6$   
 $2 \neq 6$   
 $R = 3$   
 $6 \neq 0$   
 $Q[3] =$

(task scheduling)

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### Priority Queue

- A priority queue is an abstract data type in which each element is assigned a priority. The priority of the element will be used to determine the order in which this element will proceed. The general rule of processing the element of priority key queue is
1. An element with higher priority is processed before an element with a lower priority.
  2. Two elements with the same priority are processed based on First Come First Served basis.

A queue in which elements are inserted or removed according to some priority is referred to as a priority queue.

Priority queue are widely used in operating system to execute the highest priority process first.

### Implementation of Priority Queue

There are two ways

Sorted list

Unsorted list

### Sorted list

$O(n) \Rightarrow$  Insertion

$O(1) \Rightarrow$  Deletion

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3 | 10 | 15 | 25 | 45  
|

### Unsorted list

$O(1) \Rightarrow$  Insertion

$O(n) \Rightarrow$  Deletion

### Representation of Priority Queue

1. Link Representation of Priority queue
2. Array Representation of Priority queue.

#### 1. Link Representation

R <sub>1</sub>	R <sub>2</sub>	...	R <sub>i-1</sub>	O <sub>1</sub>	O <sub>2</sub>	...	O <sub>j-1</sub>	B <sub>1</sub>	B <sub>2</sub>	...	B <sub>k-1</sub>
1	1	...	1	2	2	...	2	3	3	...	3

Priority 1      R<sub>1</sub> R<sub>2</sub> ... R<sub>i-1</sub>

Priority 2      O<sub>1</sub> O<sub>2</sub> ... O<sub>j-1</sub>

Priority 3      B<sub>1</sub> B<sub>2</sub> ... B<sub>k-1</sub>

If a sequential storage structure is used for the priority queue then insertion of new element must be placed in the middle of the structure.

This can require the moment of several items. It is better to split the priority queue into different different queue, each having its own storage structure.

## 2. Array Representation

Priority Queue		
Priority	Front	rear
1	3	3
2	1	3
3	4	5
4	4	1

Priority	Front & Rear Position				
	1	2	3	4	5
1			A		
2	B	C	D		
3			E	F	
4	I		G	H	

P-1	1	2	3	4	5
	A				

P-2	1	2	3	4	5
	B	C	D		

When an array are used to implement a priority queue then a separate queue for each priority number is maintained. Each of this queue will be implemented using circular queue.

Here two dimensional array is used where each queue will be allocated the same amount of space. To insert a new element with priority 'k' in the priority queue add the new element at the rear end of row 'k'. K = row number as well as priority no. of that element.

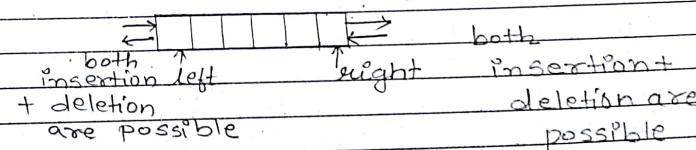
To delete an element we find the first non-empty queue & then process the front element of the non-empty queue.

## Double Ended Queue (Dqueue)

Types.

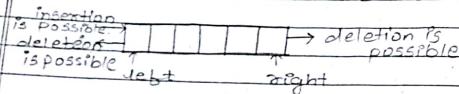
1. Input restricted dqueue
2. Output restricted dqueue.

A dqueue is a linear list of elements in which element may be inserted or deleted from the both end which is called as double ended queue or head-tail link list.

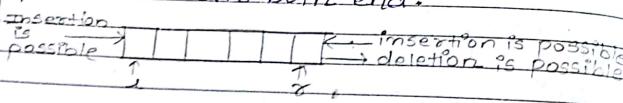


No element can added or deleted from the middle. In Computer memory, queue is implemented as circular array or circular doubly linked list.

1.  $\Rightarrow$  In input restricted queue insertion can be done only at one end, but deletion can be done from both ends.



2.  $\Rightarrow$  In this queue deletion can be possible at only one end, & insertion can be possible from both ends.



Consider a queue given below with 10 memory shells which has  $l=1$  &  $r=5$ .

Draw the queue structure & represent position of left & right pointers for each of the foll. operation

1. Insert F on the left
2. Insert G & H on the right
3. Delete two alphabet from the left.
4. Insert I on the right.
5. Insert J on the left.

6. Delete two alphabet from right

0	1	2	3	4	5	6	7	8	9
A	B	C	D	E					

1. Insert F on left

$$l = - \\ l = 0 \quad dq[l] = F \quad \boxed{\phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0}}$$

2. Insert G & H on right

$$r = + \\ r = 6 \\ dq[r] = G \quad \boxed{\phantom{0} \phantom{0} \phantom{0}} \\ r = + \\ r = 7 \\ dq[r] = H \quad \boxed{\phantom{0} \phantom{0} \phantom{0}}$$

3. Delete 2 alphabet from left.

$$l = 0 \\ F = y = dq[l] \\ l = 1 \\ A = y = dq[l]$$

4. Insert I on right

$$r = + \\ r = 8 \\ dq[r] = I$$

5. Insert J on left

$$l = - \\ l = 1 \\ dq[l] = J$$

6. Delete two alphabet from right

$$T = y = \text{char}[r_1]$$

$$H = y = \text{char}[r_1]$$

0	1	2	3	4	5	6	7	8	9
J	B	C	D	E	G	H			

If there is only one element into  
queue & if deletion operation  
is perform then after deletion  
Set l & r to '0'.

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### Linked List

A link list is a simple term & it is  
a linear collection of data element.

A list is a collection of items in  
which each item is linked with other  
& order is given by means of links  
from one item to another. Each item  
is denoted by node which consist  
of two field

- 1) value of the node
- 2) Address of next node
- 3) and the last node contain the  
null in its address path.

### Advantages of Array

1. Array is very simple to use & easy to create.
2. No memory management is needed.
3. In Array we can access any element  
with the help of index directly.
4. Array are quick to loop.

### Disadvantages of Array

1. Array is static in nature.  
Memory is allocated at compile time.
2. Insertion & deletion of element is more  
complicated in comparison to the  
link list.

## Advantages of Linked List.

1. It is a dynamic data structure therefore the size of the link list can grow & shrink in size during the execution of program.
  2. In link list programmer didn't worry about how many element will be stored in a link list.
  3. In a link list each element is allocated memory as it is added to the list.

## Disadvantages of Linked list

1. Lots of overhead. (lots of malloc call & pointer assignment)
  2. We must traverse the entire list to go to the  $n$ th node.
  3. It consumes extra space to contain the address of next element of string, in the list.

## Application of Linked List.

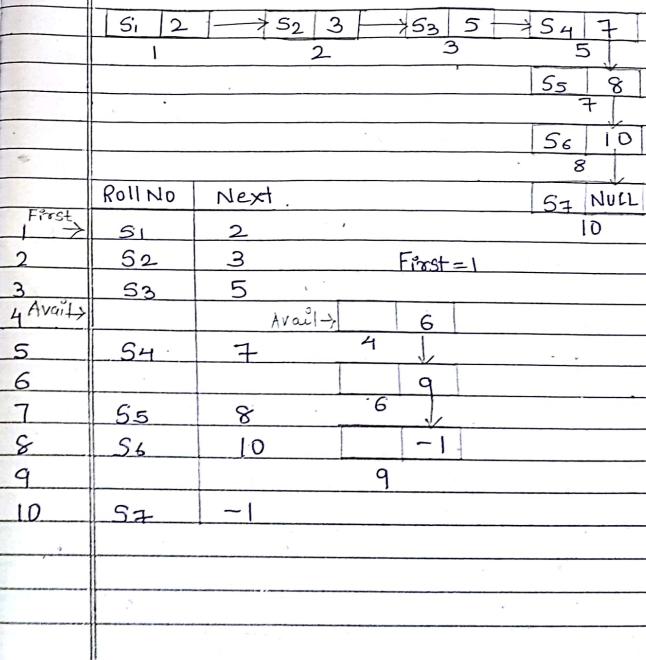
- Appendix D: Linked List.

  1. Stack, Queue, Graph, Tree are implemented using linked list.
  2. Undo functionality, Photoshop or Word.
  3. Consider the history section of web browser where it creates the link list of web pages visited. So when you press the back

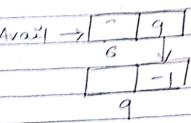
bottom the previous node data is fetched.

"Every node contain a pointer to another node, which is of the same type". It is called as self referential data type."

Representation of link list in memory.



Roll No	Next
1. S1	2
2. S2	3
3. S3	5
4. S4	-1
5. S4	7
Avail → 6	
7. S5	8
8. S6	10
9.	
10. S7	4



When we delete a row from the linked list then operating system changes the status of memory occupied by it from memory available.

The Computer maintain a list of all the free memory shell. The list of available shell is called as free pool. Linked List is a part

#### Link List as Pointer Variable

1) Which Store the address of the first node of the list.

Likewise for the free pool which is the linked list of all free memory shell we have a pointer variable 'Avail' which store the address of the first free space.

2) If we delete node then space occupied by that node must be given.

back to the free pool. So memory can be reused by some other program.

3) The operating System does this task of adding & removing memory from the free pool.

This task is perform when O.S finds the CPU ideal or the program are falling short of memory.

The O.S scan through all the memory shell & marks those cell that are being used by some other program. Then it collect all the cell which are not being used & at their address to free pool. This process is called garbage collection.

#### Singly Linked List

1) Algorithm for Insertion at beginning

FIRST = INSERT(X, FIRST)

X = A new element which is to be inserted.

FIRST = A pointer to the first element to linked list whose typically node contains info & link.

New is a temporary variable.

Avail is a pointer to the top element of the availability stack