



Missing Number

Problem

Given an array `nums` containing `n` distinct numbers in the range `[0, n]`, return the only number in the range that is missing from the array.

Example 1:

Input: `nums = [3,0,1]`

Output: 2

Explanation:

`n = 3` since there are 3 numbers, so all numbers are in the range `[0,3]`.
2 is the missing number in the range since it does not appear in `nums`.

Example 2:

Input: `nums = [0,1]`

Output: 2

Explanation:

`n = 2` since there are 2 numbers, so all numbers are in the range `[0,2]`.
2 is the missing number in the range since it does not appear in `nums`.

Example 3:

Input: `nums = [9,6,4,2,3,5,7,0,1]`

Output: 8

Explanation:

`n = 9` since there are 9 numbers, so all numbers are in the range `[0,9]`.
8 is the missing number in the range since it does not appear in `nums`.

Constraints:

`n == nums.length`

`1 <= n <= 104`

`0 <= nums[i] <= n`

All the numbers of `nums` are unique

Approach 1 (Brute-force with sorting and comparison)

Sort the array.

Loop from index 1 to $n - 1$:

If $\text{nums}[i] \neq \text{nums}[i-1] + 1$, return $\text{nums}[i-1] + 1$ as the missing number.

If no such mismatch is found:

If $\text{nums}[0] \neq 0$, return 0.

Else return n .

Dry Run

Input: `nums = [4, 2, 1, 0, 5]`

After Sorting: `nums = [0, 1, 2, 4, 5]`

Check:

$i = 1 \rightarrow 1 == 0 + 1$

$i = 2 \rightarrow 2 == 1 + 1$

$i = 3 \rightarrow 4 \neq 2 + 1 \rightarrow \text{return } 3$

Output: 3

Time and Space Complexity

Time Complexity: $O(n \log n)$

Due to sorting the array.

Space Complexity: $O(1)$

Sorting is done in-place, and only a few variables are used.

JavaScript

C++

C

Java

Python

```
var missingNumber = function(nums) {  
    nums.sort((a, b) => a - b);  
  
    if (nums[0] !== 0) return 0;  
  
    for (let i = 1; i < nums.length; i++) {  
        if (nums[i] !== nums[i - 1] + 1) {  
            return nums[i - 1] + 1;  
        }  
    }  
  
    return nums.length;  
}
```

```
};
```

Approach (Optimal using Sum Formula)

The sum of numbers from 0 to n is given by the formula:

$$\text{total_sum} = (n \times (n + 1)) / 2$$

Steps:

Calculate `total_sum` using the formula above.

Calculate the sum of all elements in the input array.

The missing number is `total_sum - sum_of_array`.

Dry Run

Input: `nums = [3, 0, 1]`

n: 3 (length of the array)

total_sum: $3 \times (3 + 1) / 2 = 6$

sum_of_array: $3 + 0 + 1 = 4$

missing_number: $6 - 4 = 2$

Output: 2

Time and Space Complexity

Time Complexity: $O(n)$

We traverse the array once to compute the sum.

Space Complexity: $O(1)$

Only a few variables are used, no extra space proportional to input size.

JavaScript

C++

C

Java

Python

```
var missingNumber = function(nums) {  
    let n = nums.length;
```

```
let total_sum = (n * (n + 1)) / 2;  
let sum_of_array = 0;  
  
for (let num of nums) {  
    sum_of_array += num;  
}  
  
return total_sum - sum_of_array;  
};
```

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