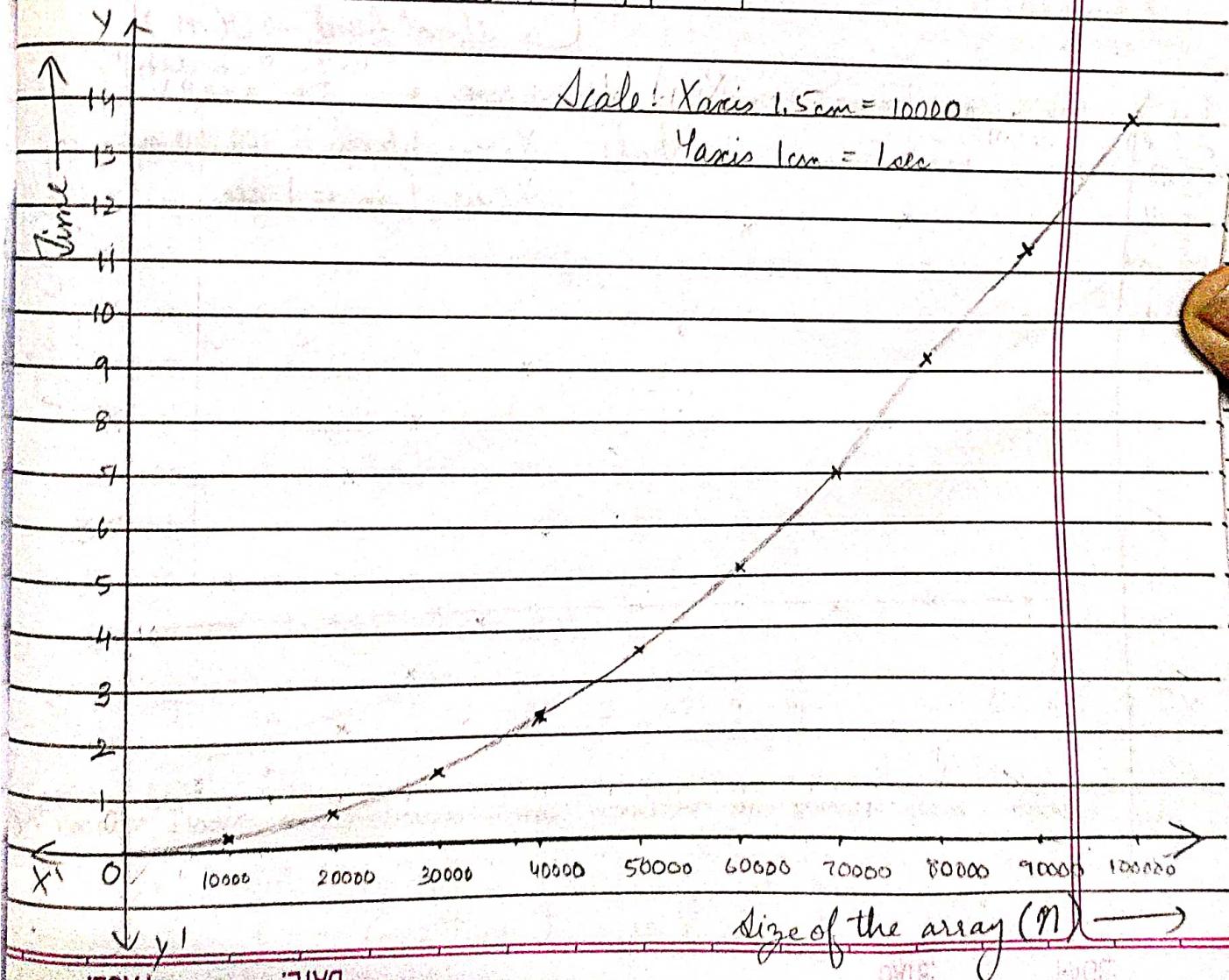


# ADA Lab

## i) Selection Sort (no sleep)

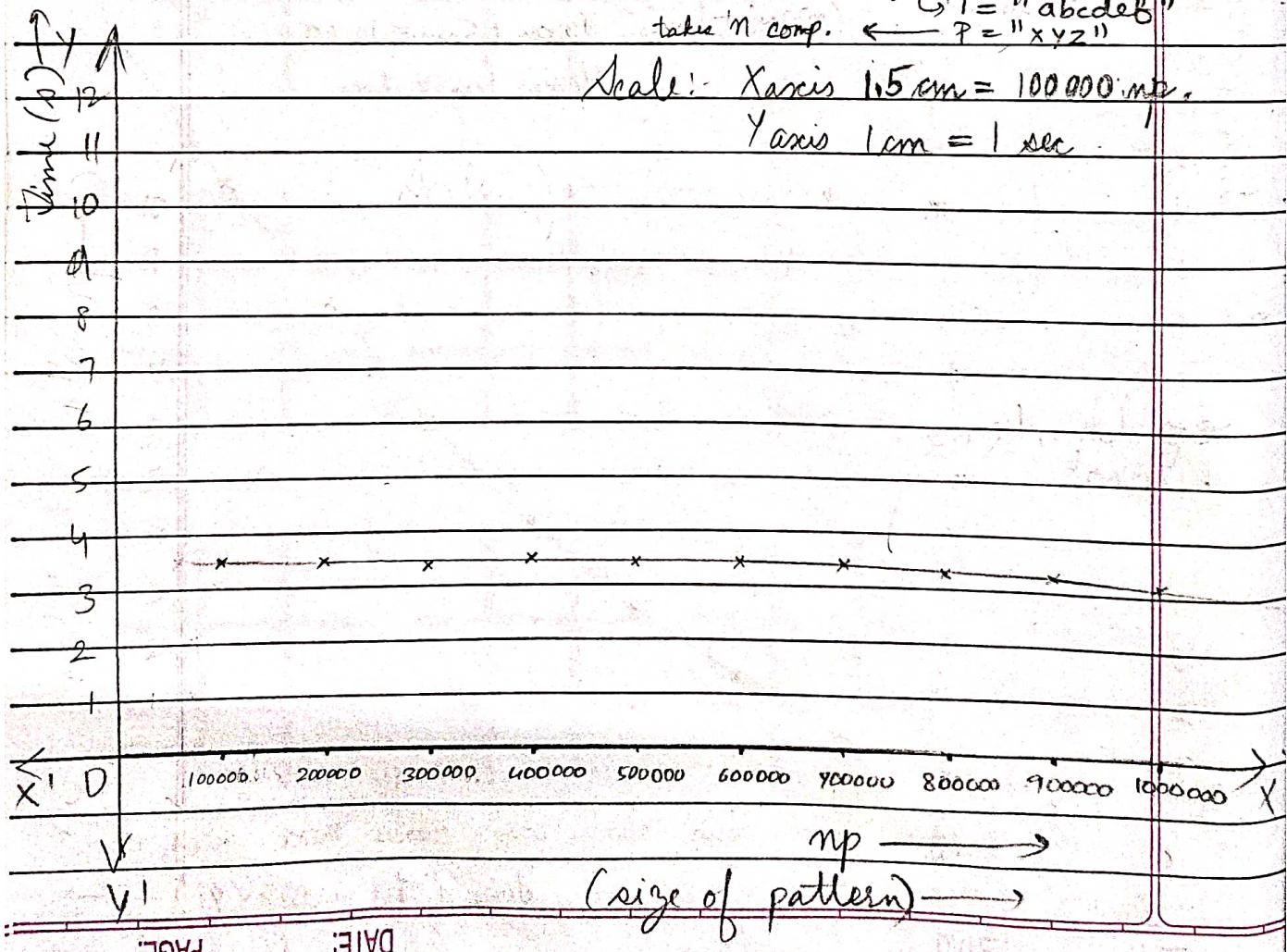
$n$	$t$	$\approx t$		
10000	0.151890	0.2		
20000	0.572826	0.6		
30000	1.267554	1.3		
40000	2.263620	2.3	Best	$O(n^2)$
50000	3.564726	3.6	Avg	$O(n^2)$
60000	5.077233	5.1	Worst	$O(n^2)$
70000	6.959399	7.0		Space:
80000	9.228300	9.2		Worst $O(1)$ auxiliary.
90000	11.428874	11.4		
100000	14.023419	14		



2) Brute force string matching (ifleep(0,1) in inner while loop)  
 $m = n = 1,000,000$  (1 crore)

( $m^2$ )

$mp$	$t$	$\approx t$	
100 000	3.495001	3.5	
200 000	3.370467	3.4	
300 000	3.338601	3.3	
400 000	3.366675	3.4	
500 000	3.3994913	3.3	
600 000	3.267052	3.3	
700 000	3.254268	3.3	
800 000	3.186548	3.2	
900 000	3.176783	3.2	Worst $\rightarrow O(nm)$
10 000 000	3.096119	3.1	Avg $\rightarrow O(n+m)$ in the Avg. Best $\rightarrow$ if pattern found $\rightarrow O(m)$ $\hookrightarrow$ if not found $\rightarrow O(n)$



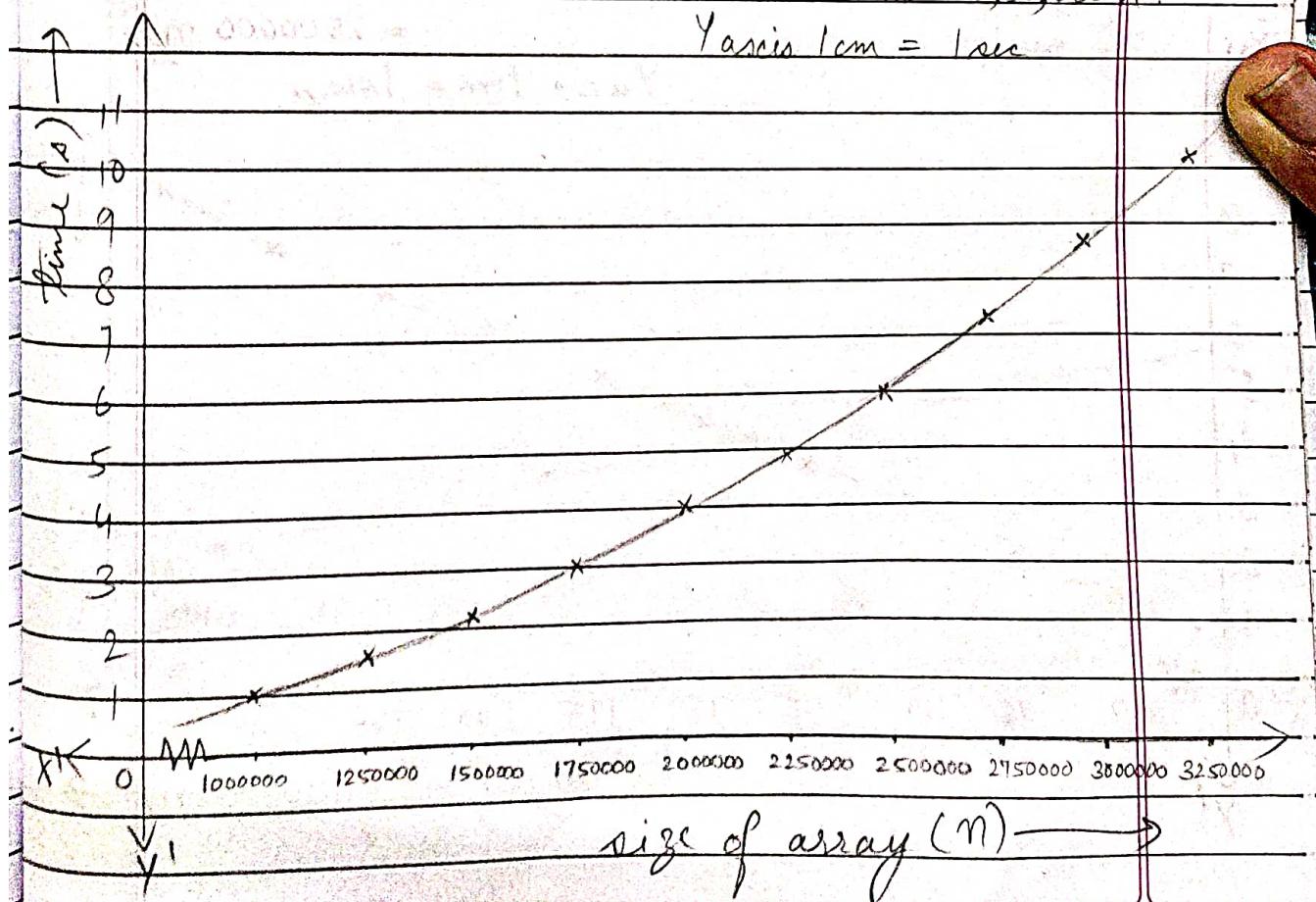
### 3) QuickSort (no swap)

Case 1: performance

$n$	$t$	$\approx t$	Best	$O(n \log n)$
10 00 000	1.015733	1.0	Avg	$O(n \log n)$
12 50 000	1.558347	1.6	Worst	$O(n^2)$
15 00 000	2.209464	2.2		
17 50 000	2.993569	3.0		thus we did
20 00 000	3.912658	4.0		random 1000
22 50 000	4.899253	4.9		so many copies
25 00 000	6.023231	6.0		of same no.,
27 50 000	7.281868	7.3		(use quicksort 3 to avoid this)
30 00 000	8.705107	8.7		
32 50 000	10.091069	10.1		that's why there's a difference in the no. of ele quick sort merge cost in next page

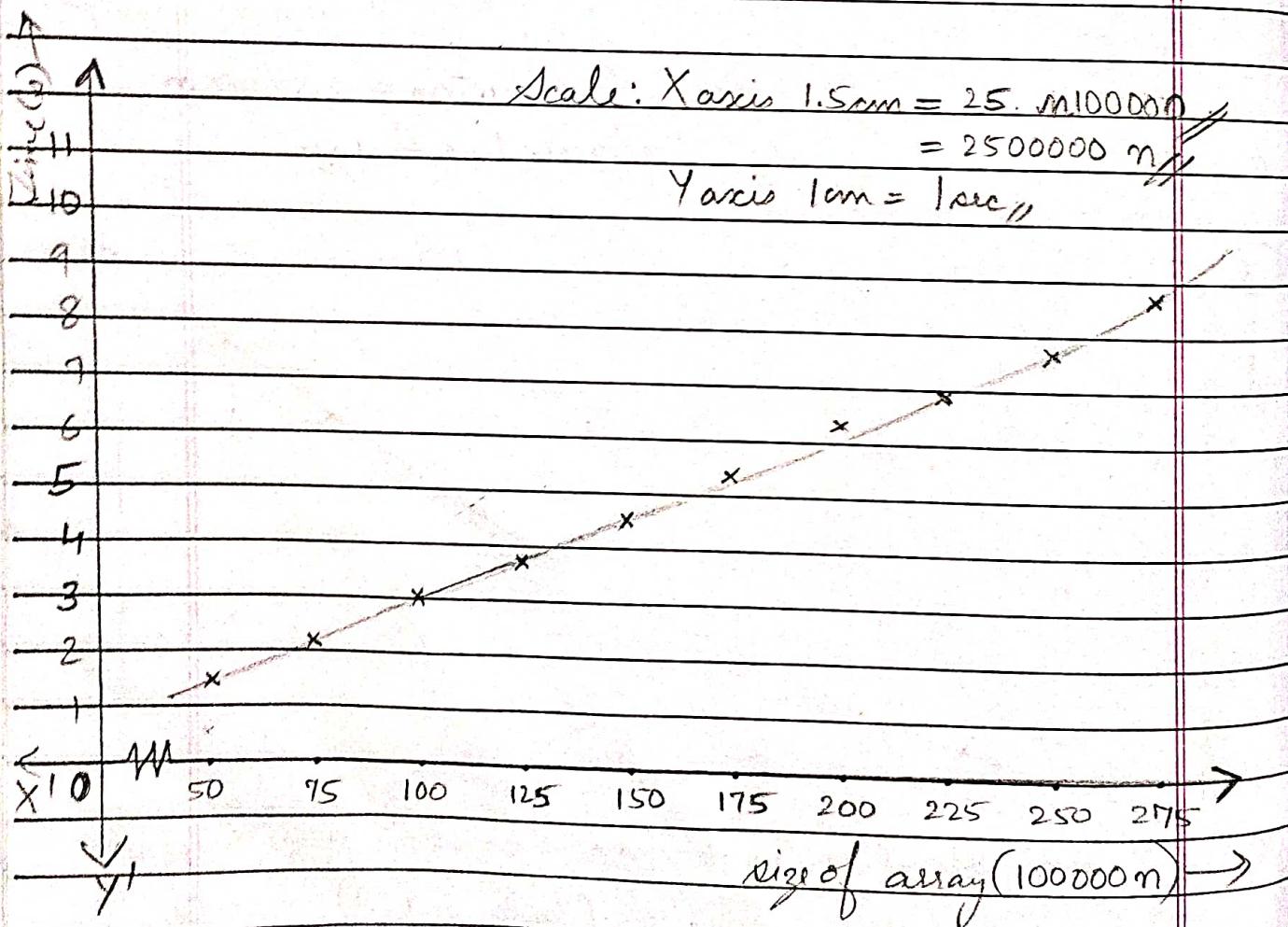
Scale: X axis 1.5cm = 2,50,000 n.

Y axis 1cm = 1 sec



# 4) MergeSort (no sleep)

$n$	$t$	$\approx t$	Case B,A,W	Performance $O(n \log n)$
50 00 000	1.481491	1.5		
75 00 000	2.211617	2.1		$O(n)$ <del>Processor Comp.</del>
100 00 000	3.003953	3.0		
125 00 000	3.718443	3.7		
150 00 000	4.497951	4.5		
175 00 000	5.312698	5.3		
200 00 000	6.211526	6.2		
225 00 000	6.879394	6.9		
250 00 000	7.584053	7.6		
275 00 000	8.576077	8.6		



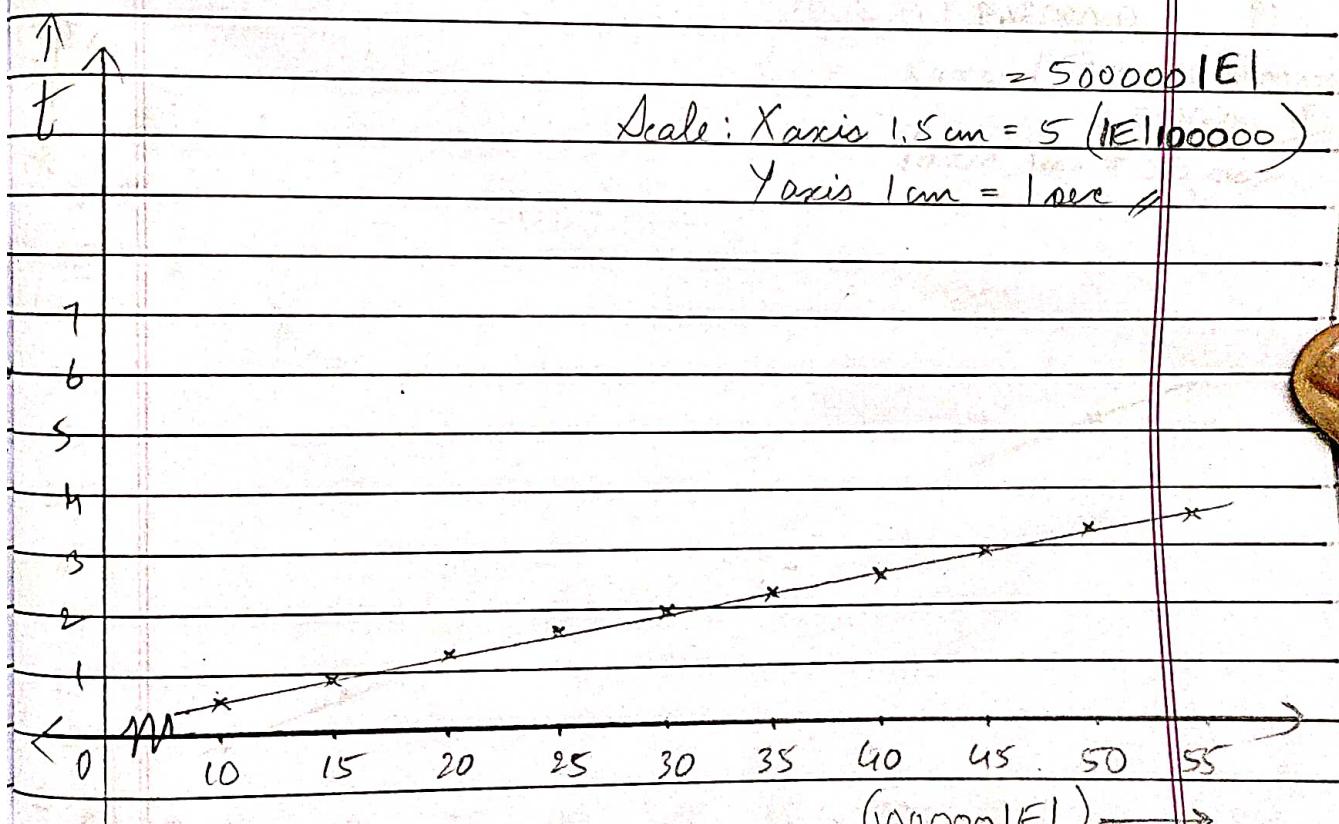
5) Kruskal's Algorithm (no sleep)

$|V| = 10,000,000$  (constant)

$ E $	$t$	$\approx t$
1000000	0.607917	0.6
1500000	0.932571	0.9
2000000	1.260241	1.3
2500000	1.575254	1.6
3000000	1.871444	1.9
3500000	2.236771	2.2
4000000	2.523163	2.5
4500000	2.865025	2.9
5000000	3.216166	3.2
5500000	3.511158	3.5

$O(E \log E)$

$O(E \log V)$



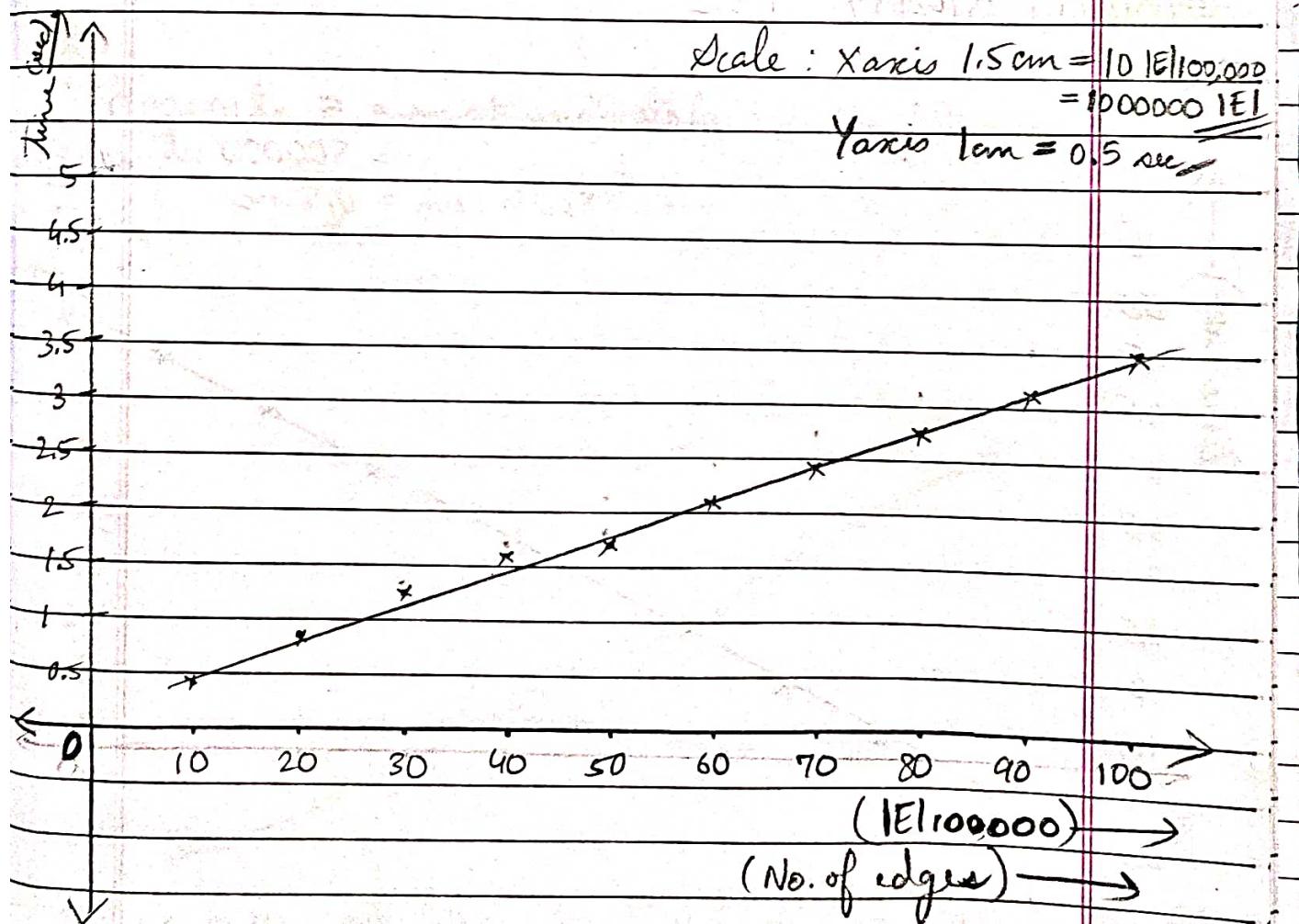
$E \log E / E \log V$ .

## 6) BFS (no sleep)

$|V| = 10000$  (i.e.  $\text{rand}() \% 10000$ )

$ E $	$t$	$\approx t$
1000000	0.432915	0.4
2000000	0.825106	0.8
3000000	1.268006	1.3
4000000	1.663508	1.6
5000000	1.721398	1.7
6000000	2.059086	2.1
7000000	2.377281	2.4
8000000	2.733710	2.7
9000000	3.114764	3.1
10000000	3.505273	3.5

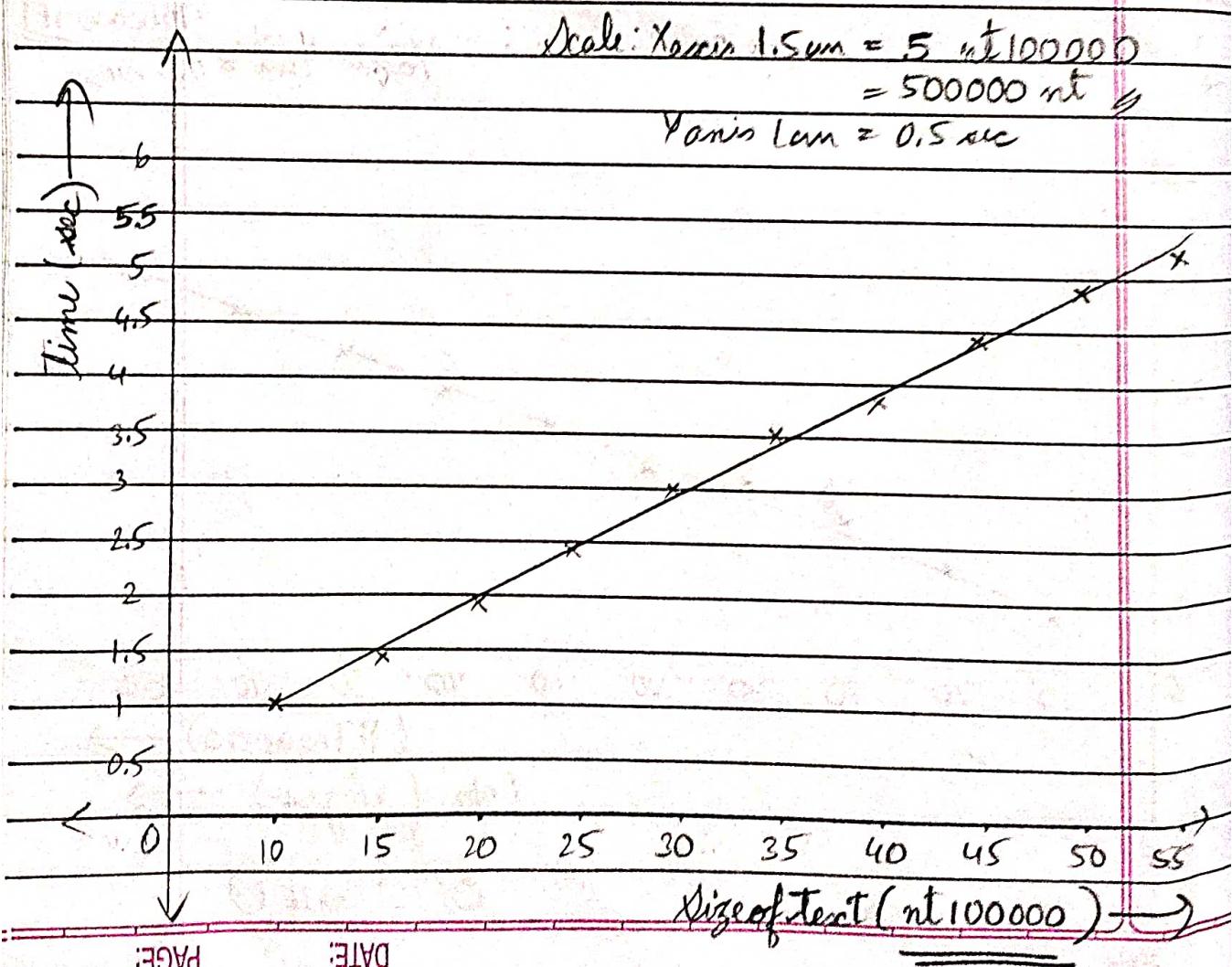
adjacency list  $\rightarrow O(V+E)$   
 adjacency matrix  $\rightarrow O(V^2)$ ,  
 $O(V+E)$  we are doing here.



7) Horner (sleep 0.1)

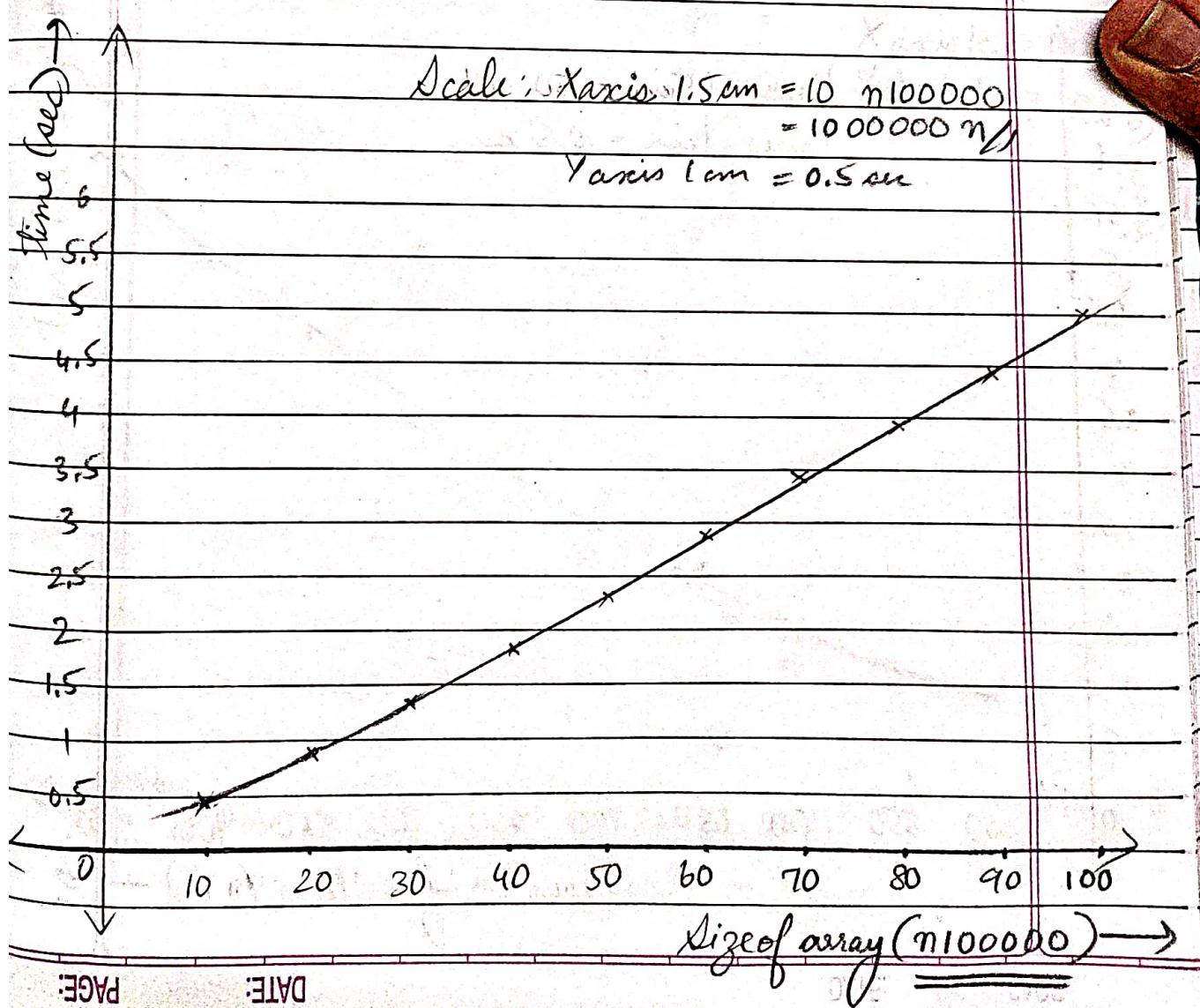
$m_p = 20$  (fixed)

$n_t$	$t$	$\approx t$	
10 00 000	0.954643	1.0	Best case $\rightarrow$ sub-linear
15 00 000	1.417405	1.4	Average case $\rightarrow O(n)$
20 00 000	1.901902	1.9	Worst case $\rightarrow O(n^m)$
25 00 000	2.413174	2.4	
30 00 000	2.933515	3.0	
35 00 000	3.502000	3.5	
40 00 000	3.820820	3.8	
45 00 000	4.407284	4.4	
50 00 000	4.857511	4.8	
55 00 000	5.162197	5.2	



### 8) Heapsort (No sleep)

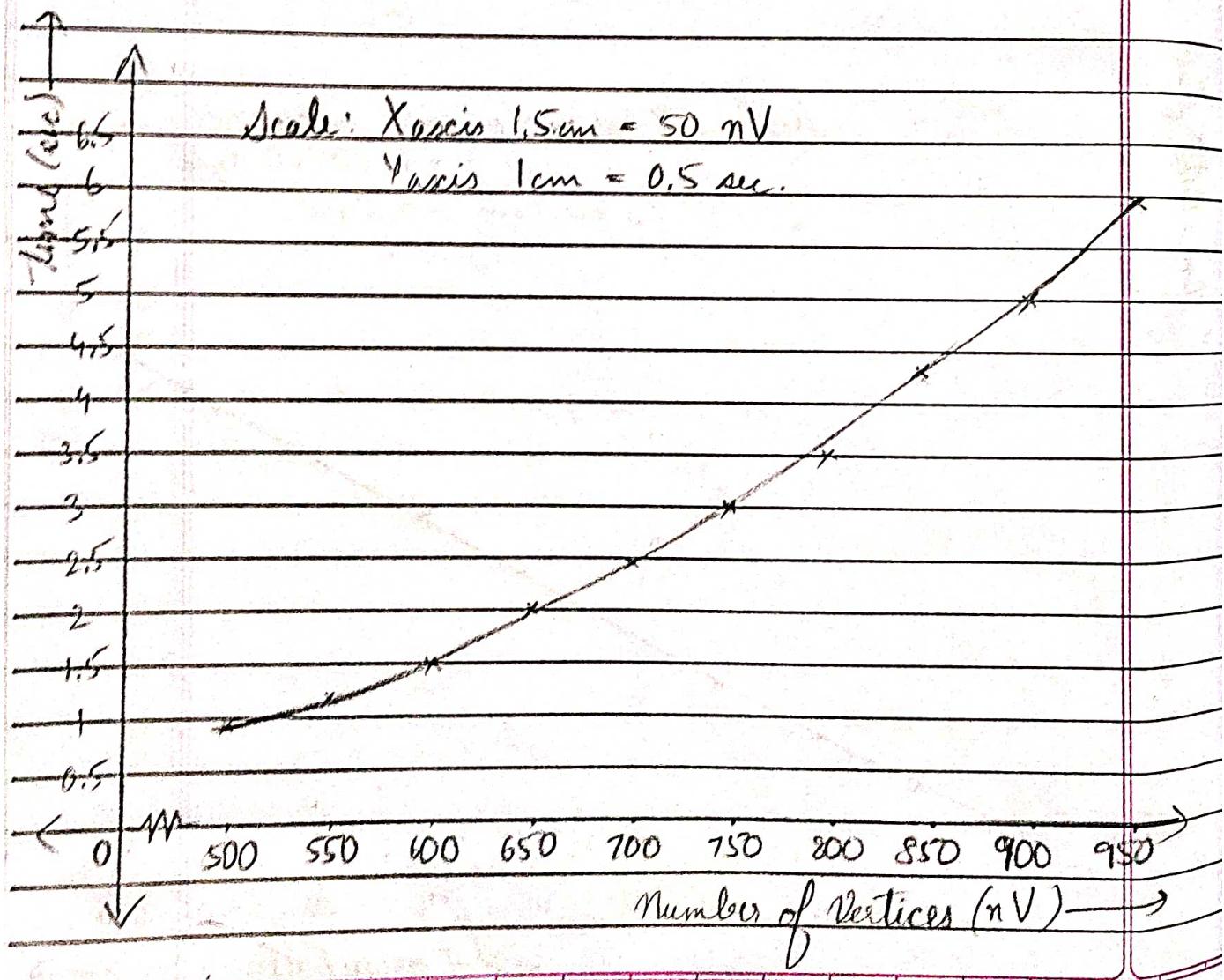
$n$	$t$	$= t$	
10 00 000	0.397414	0.4	Avg, best $O(n \log n)$
20 00 000	0.818897	0.8	
30 00 000	1.290093	1.3	Best $\rightarrow$ distinct keys $\rightarrow O(n \log n)$
40 00 000	1.760143	1.8	$\hookdownarrow$ equal keys $\rightarrow O(n^2)$
50 00 000	2.268754	2.3	
60 00 000	2.770901	2.8	
70 00 000	3.380562	3.4	
80 00 000	3.884239	3.9	
90 00 000	4.409547	4.4	
100 00 000	5.007718	5.0	



graph algo. Better with adjacency matrix than adjacency list  
for this algo.

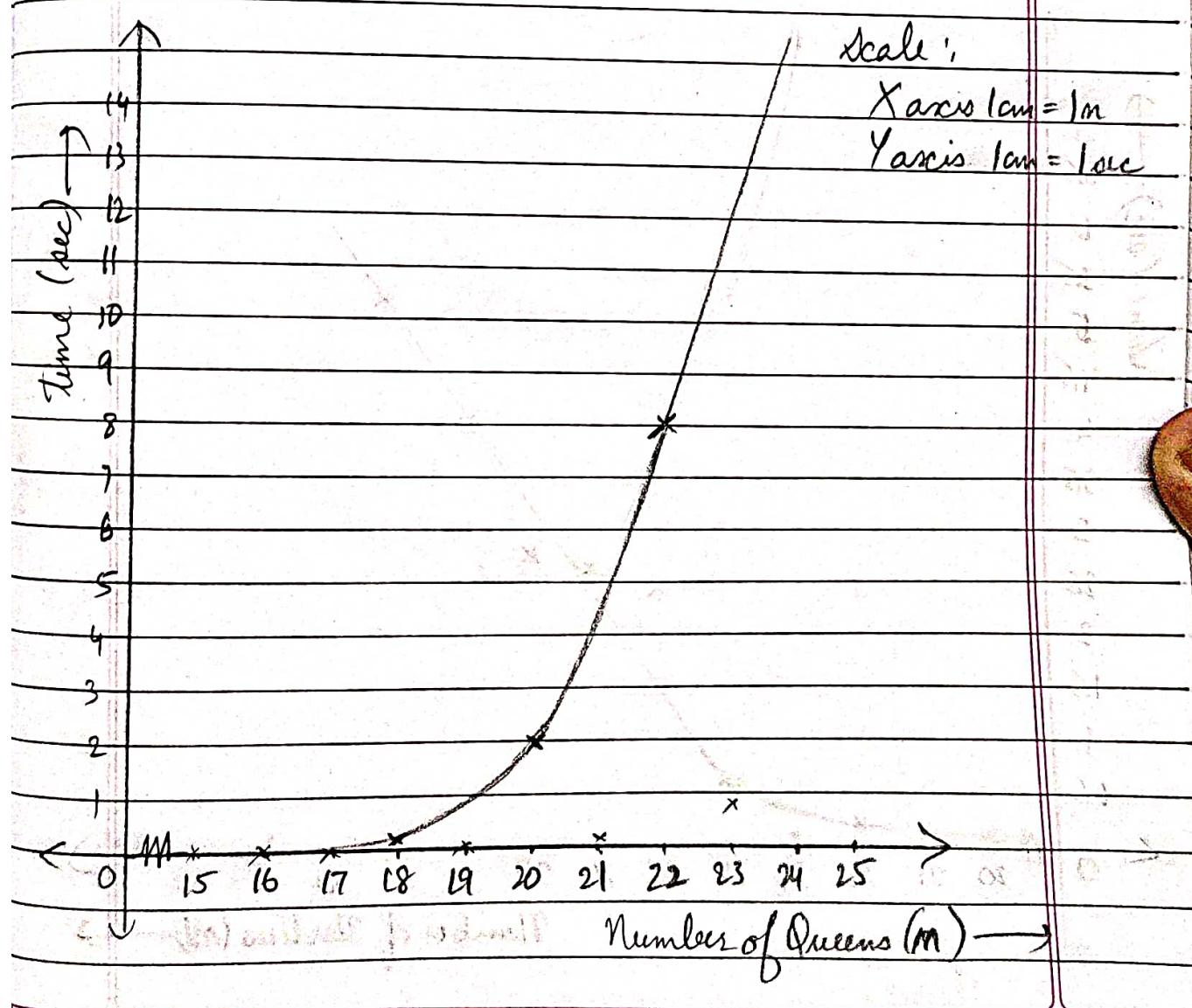
### 9) Floyd-Warshall (No sleep)

$nV$	$t$	$\approx t$
500	0.884352	0.9
550	1.1704111	1.2
600	1.5401111	1.5
650	1.921768	2.0
700	2.434800	2.4
750	2.907238	3.0
800	3.563287	3.5
850	4.267111	4.3
900	4.948280	5.0
950	5.889677	5.9



## 10) nQueen (no sleep)

$n$	$t$	$\approx t$
15	0.001754	0.0
16	0.033800	0.0
17	0.005706	0.0
18	0.206935	0.2
19	0.019543	0.0
20	2.044740	2.0
21	0.123243	0.1
22	7.984163	8.0
23	0.842578	0.8
24	63.239379	63.2



$$O(N-1)! = O(2^{m-1})$$

## II] Travelling Salesman (No sleep)

$nV$	$t$	$\approx t$
20	0.108445	0.1
21	0.149911	0.2
22	0.25713	0.3
23	0.12551	0.1
24	0.574786	0.6
25	2.43544	2.4
26	2.55434	2.6
27	2.74792	2.7
28	4.05655	4.0
29	5.20842	5.2

$O(n^2 * 2^m)$

