Exam Roll No. 00414902014

# END TERM EXAMINATION

FIRST SEMESTER [BCA] DEC.2014 - JAN.2015

Paper Code: BCA101

Subject: Mathematics-I

(Batch: 2011 onwards)

Time: 3 Hours

Maximum Marks:75

Note: Attempt any five questions including Q.no. 1 which is compulsory. Select one question from each unit.

Q1 (a) If  $A = \begin{bmatrix} 9 & 1 \\ 4 & 3 \end{bmatrix}$ ,  $B = \begin{bmatrix} 1 & 5 \\ 7 & 12 \end{bmatrix}$  find the matrix X such that 3A+5B+2X=0.(3)

(b). Prove that if (verify by finding AA-1)  $A = \begin{bmatrix} 2 & 3 \\ 4 & 2 \end{bmatrix}$  then  $A^{-1} = \begin{bmatrix} -1/4 & 3/8 \\ 1/2 & -1/4 \end{bmatrix}$  (3)

(c) Show that  $y = \frac{x^2 - 1}{x - 1}$  is continuous except at x=1. What is the nature (3)of the discontinuity?

(d) Find  $\lim_{x \to 0} \frac{\sqrt{x+1}-1}{x}.$ (3)

(e) Using Taylor's series, find the value of  $f\left(\frac{21}{20}\right)$  if  $f(x) = x^3 - 6x^2 + 7$ . (3)

(f) Show that  $\sin(x)(1+\cos x)$  is maximum when  $x=\frac{\pi}{3}$ . (3)

(g) Evaluate  $\int e^x \left(\frac{x-1}{x^2}\right) dx$ . (3)

(h) Evaluate  $\int e^x \cos^2 x dx$ . (4)

Q2 (a) Given  $A = \begin{bmatrix} 2 & 1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$ , find  $A^{-1}$  and  $A^{4}$  using Cayley-Hamilton

(6)

(b) If  $A = \begin{bmatrix} 1 & 3 & 0 \\ -1 & 2 & 1 \\ 0 & 0 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} 2 & 3 & 4 \\ 1 & 2 & 3 \\ -1 & 1 & 2 \end{bmatrix}$  compute AB and BA and show that (6.5)

(a) If the matrix  $\begin{bmatrix} 0 & 2b & c \\ a & b & -c \\ a & -b & c \end{bmatrix}$  is orthogonal, then find the values of a, b O3

(6)and c.

(b) Determine the rank of the following matrix using elementary row

$$\begin{bmatrix} 2 & 1 & -3 & 4 \\ 2 & 4 & -2 & 5 \\ 0 & 3 & 1 & 3 \\ 2 & 1 & -3 & -2 \end{bmatrix}$$

(a) For what value of x does  $y = \frac{x+1}{(x+2)(x+3)}$  tends to infinity? Indicate Q4 the form of the graph of the function and describe its discontinuities. (6)

(b) Evaluate 
$$\frac{\ln}{m \to \infty} P \left(1 + \frac{i}{m}\right)^{mn}$$
. (6.5)

Q5 (a) A function 
$$f$$
 is defined as follows:-  $f(x) = \begin{cases} \frac{9x}{x+2}, & \text{if } x < 1 \\ 3, & \text{if } x = 1. \text{ Examine} \\ \frac{x+3}{x}, & \text{if } x > 1 \end{cases}$ 

the continuity of f in the interval (-3,3).

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(b) Find the value of a so that the function  $f(x) = \begin{cases} ax + 5 & if & x \le 2 \\ x - 1 & if & x > 2 \end{cases}$  is continuous at x=2.

## **UNIT-III**

Q6 (a) Find  $\frac{dy}{dx}$  if-

(i)  $y = \sin \sqrt{x}$  (ii)  $y = \sin^3 2x$ . (6)

(b) Find all the asymptotes of the curve  $y^2(x-2a) = x^3 - a^2$ . (6.5)

(6)(a) Find the nth derivative of log(2x+3). Q7

(b) Show that the function  $f(x) = x^2 + \frac{250}{x}$  has a minimum value at x=5.(6.5)

(6)

(a) Find the following integrals:-

(i)  $\int xe^{-x}dx$  (ii)  $\int x^n \log x dx$ .

(b) Find out the Reduction Formulae for  $\int_0^{\pi/4} \sin^n x dx$ , n being a positive (6.5)/ integer.

(a) Prove that  $\beta(m,n) = \beta(m+1,n) + \beta(m,n+1)$ . (6)Q9

(b) Evaluate 
$$\int \frac{dx}{2x^2 + 3x + 5}$$
. (6.5)