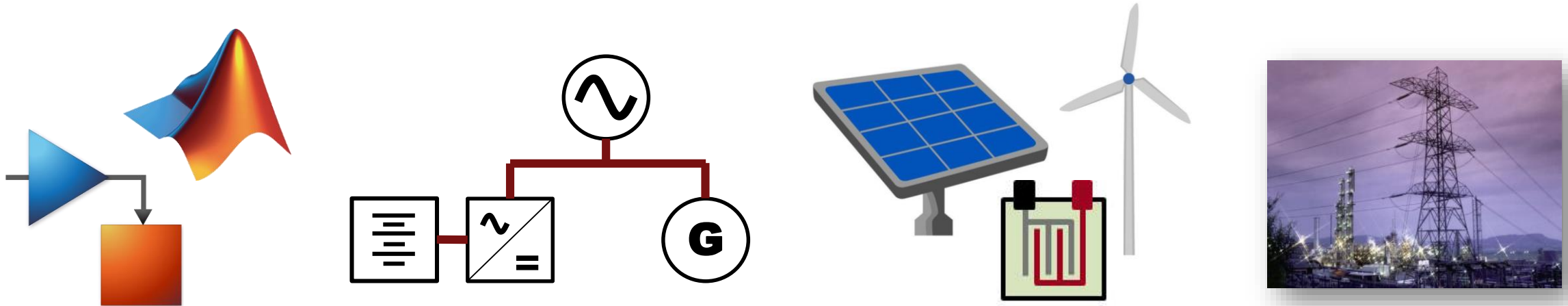


# Microgrid Energy Management System Development Using Optimization-based Methods



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# Demo – Microgrid EMS

## Using Model-Based Design and Optimization

### HEMS example – *microgrid with loads*

#### PV Panels:

- MPPT Control
- Power electronics



#### Decision Logic:

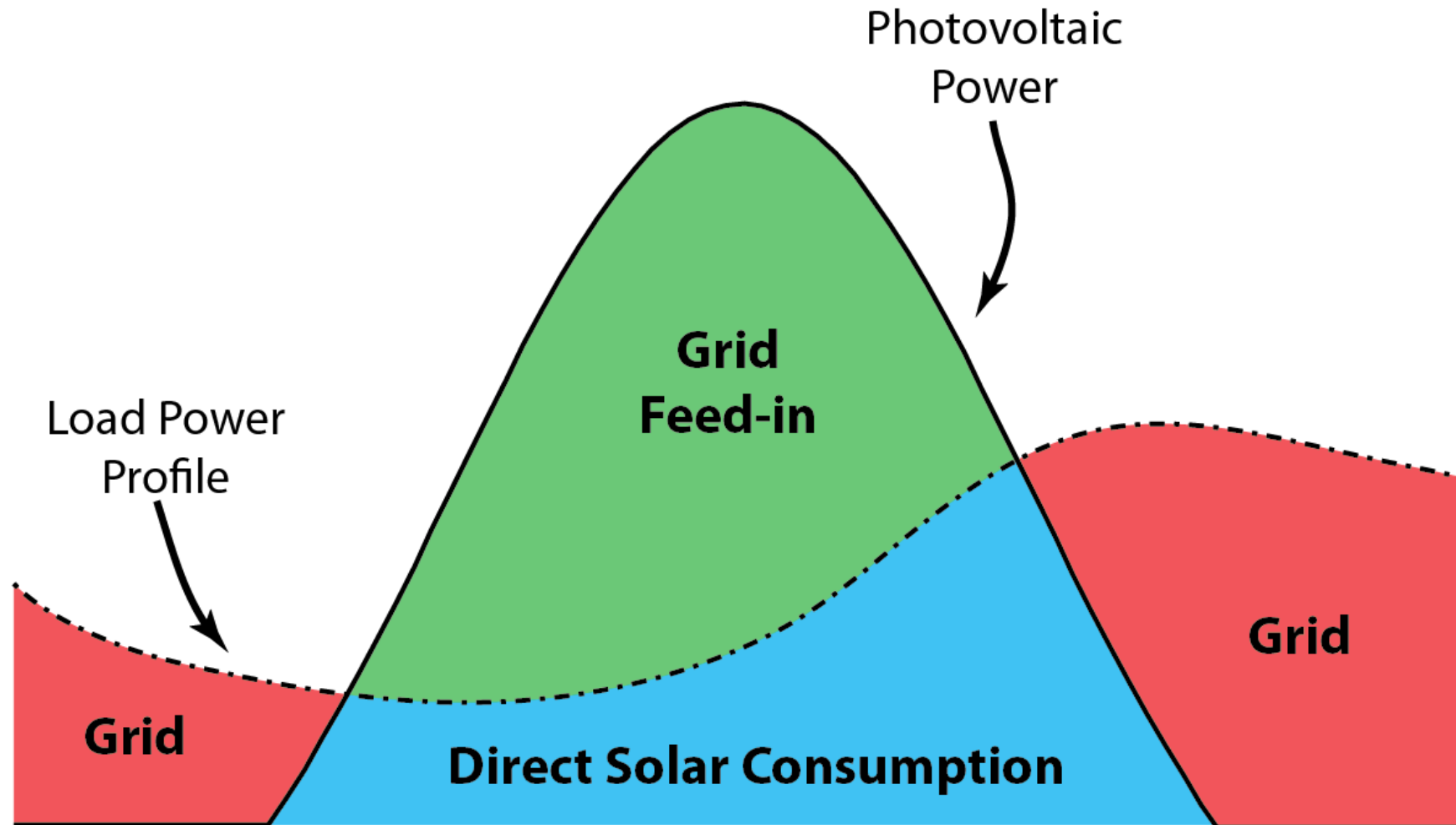
- Store/draw power
- Use external grid
- Optimize energy

#### Battery System:

- Charge controls
- Discharge controls
- Power electronics

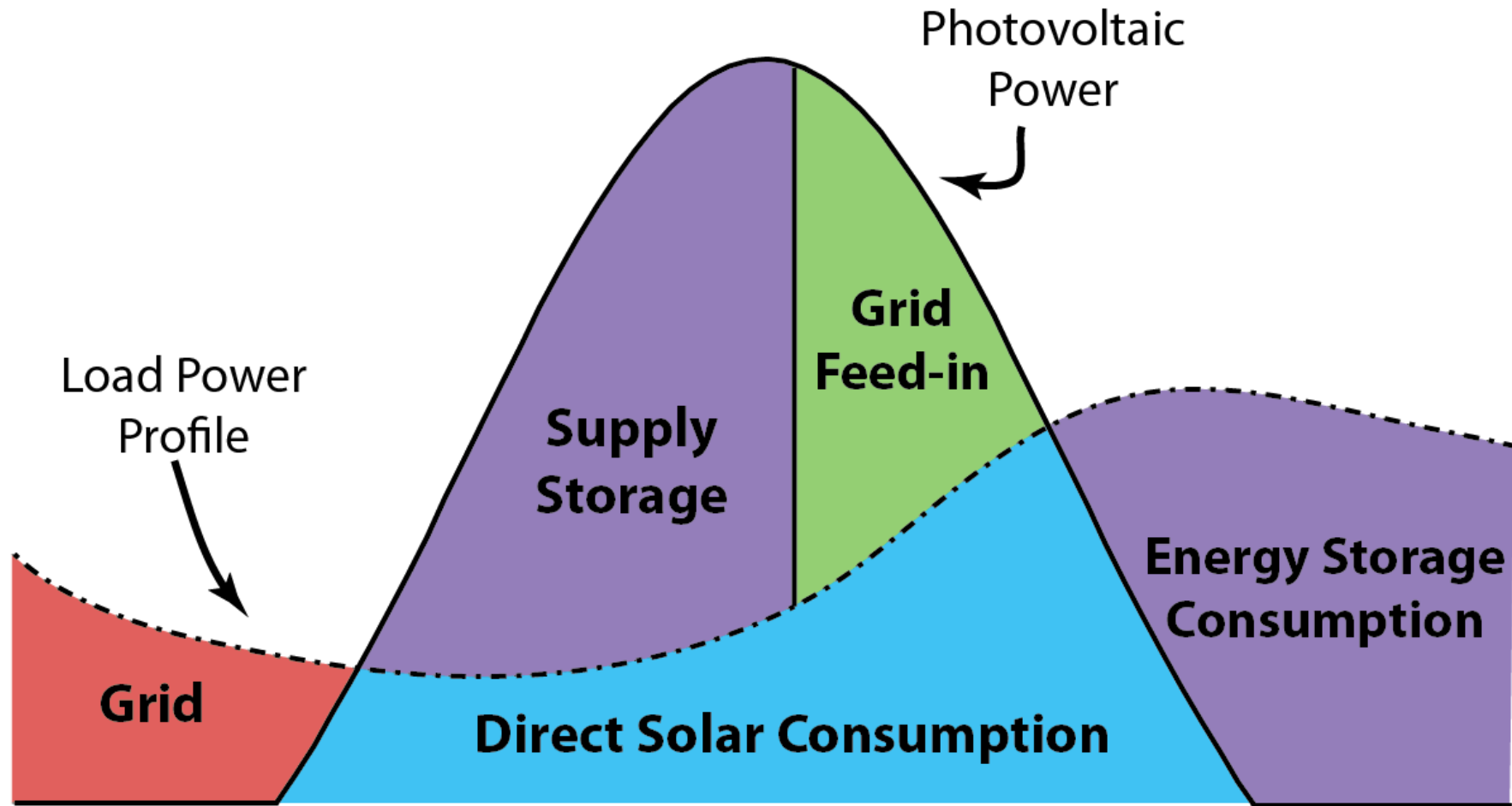


# Why energy storage with solar?



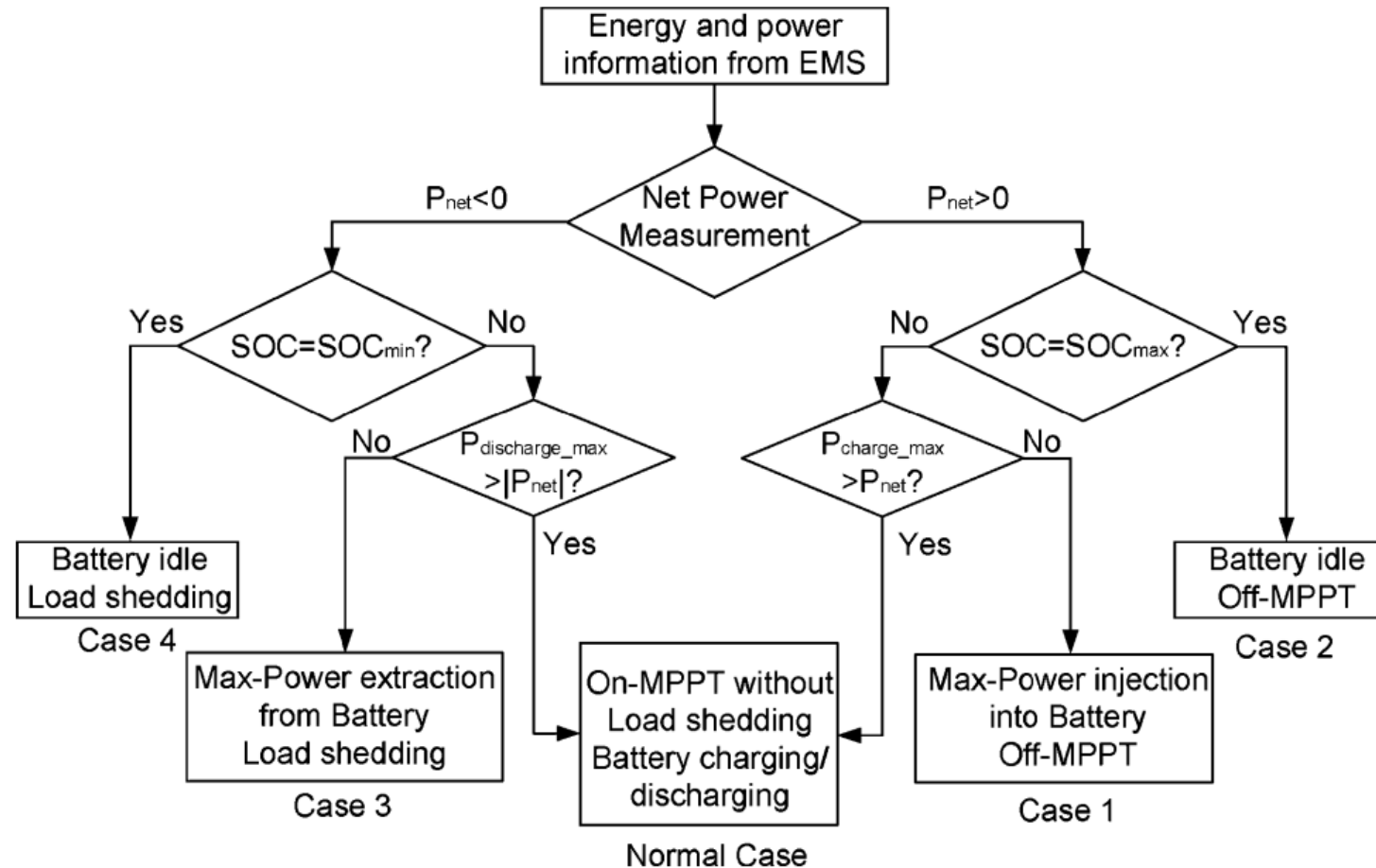
Adapted from: Smart EnergySystems Website  
<http://www.smart-energy.ag/products/ac-gekoppelte-speicherlosung-smartenergy-ac/?lang=en>

# Peak Demand Shift using Energy Storage

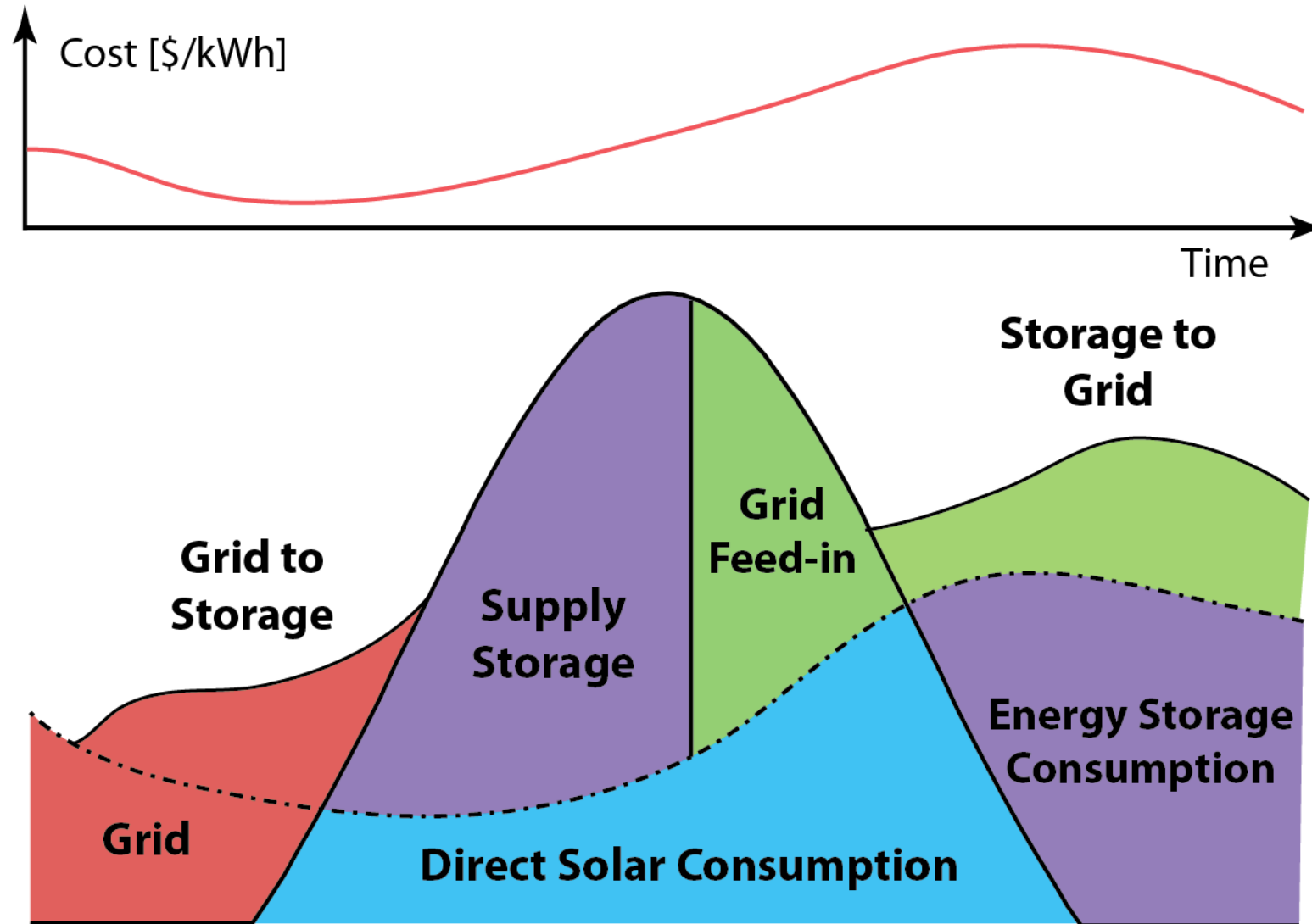


Adapted from: Smart EnergySystems Website  
<http://www.smart-energy.ag/products/ac-gekoppelte-speicherlosung-smartenergy-ac/?lang=en>

# Implementation of Energy Management Logic



# Factoring in Variable Electricity Cost



# Optimization-based Peak Demand Shift

- Objective function: *what do we want to minimize/optimize?*
  - Minimize total cost of variable priced electricity

$$C_{tot} = \sum_{k=0}^N C_{grid}(k) \cdot E_{grid}(k)$$

- Constraints: *how does our system operate?*
  - Power input/output to battery

$$E_{batt}(k) = E_{batt}(k - 1) + P_{batt}(k)\Delta T$$

- Power balance

$$\underbrace{P_{pv}(k) + P_{grid}(k) + P_{batt}(k)}_{\text{Sources}} = \underbrace{P_{load}(k)}_{\text{Loads}}$$

# Linear program-based Optimization

- Standard form for the Linear program (LP) - linprog

$$\min_x f^T x \text{ such that } \begin{cases} A \cdot x \leq b \\ A_{eq} \cdot x = b_{eq} \end{cases}$$

- Define states (x) necessary for LP optimization
  - $P_{grid}(1:N)$  – Power from grid used from time step 1 to N
  - $P_{batt}(1:N)$  – Power from battery
  - $E_{batt}(1:N)$  – Energy stored in battery

$$x = [P_{grid}(1:N) \quad P_{batt}(1:N) \quad E_{batt}(1:N)]^T$$



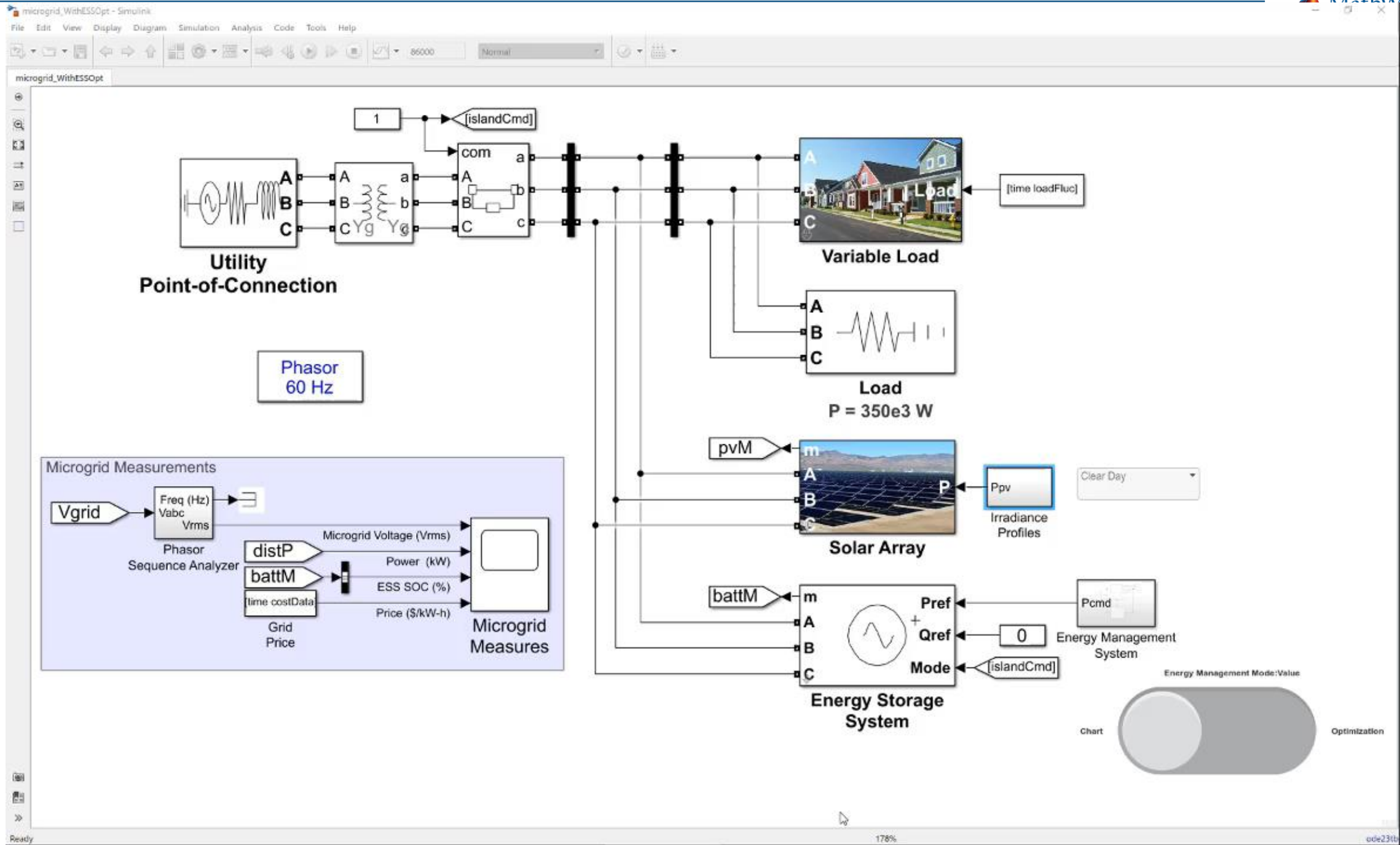
# Linear program-based Optimization

- Equivalent constraint

$$\begin{aligned}
 & \overbrace{\begin{bmatrix} I_{N \times N} & I_{N \times N} & 0_{N \times N} \\ 0_{N \times N} & Y_{N \times N} & \Phi_{N \times N} \end{bmatrix}}^{A_{eq}} x = \overbrace{\begin{bmatrix} P_{load}(1:N) - P_{pv}(1:N) \\ E_{batt}(1) \\ 0_{N-1} \end{bmatrix}}^{b_{eq}} \\
 & Y_{3 \times 3} = \begin{bmatrix} 0 & 0 & 0 \\ \Delta T & 0 & 0 \\ 0 & \Delta T & 0 \end{bmatrix} \quad \Phi_{3 \times 3} = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}
 \end{aligned}$$

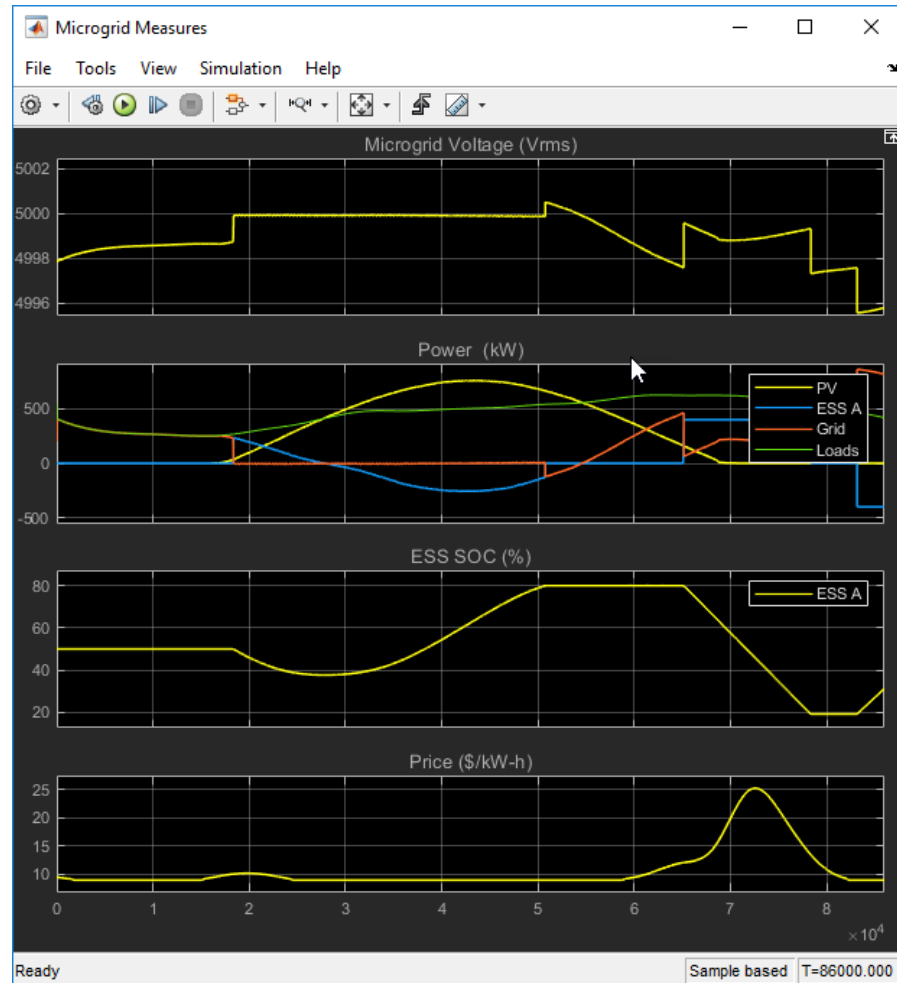
- Inequality constraints

$$\begin{aligned}
 & \overbrace{\begin{bmatrix} 0_{N \times N} & I_{N \times N} & 0_{N \times N} \\ 0_{N \times N} & -I_{N \times N} & 0_{N \times N} \\ 0_{N \times N} & 0_{N \times N} & I_{N \times N} \\ 0_{N \times N} & 0_{N \times N} & -I_{N \times N} \end{bmatrix}}^A x \geq \overbrace{\begin{bmatrix} P_{max} \\ -P_{min} \\ E_{max} \\ -E_{min} \end{bmatrix}}^b
 \end{aligned}$$



# Policy Comparison

## Heuristic



## Optimized

