

# ASSIGNMENT 1

For  
Kleb Data Mining

Submitted to

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Submitted on

30/09/2021

## Simulation

Q- Simulate the algorithm genRules(F) for the just found out frequent item sets.

TID	List of item_IDs
T100	I1, I2, I5
T200	I2, I4
T300	I2, I3
T400	I1, I2, I4
T500	I1, I3
T600	I2, I3
T700	I1, I3
T800	I1, I2, I3, I5
T900	I1, I2, I3

## Algorithm

Algorithm genRules(F)

// F is the set of all frequent itemsets

- 1 for each frequent k-itemset  $f_k$  in F,  $k \geq 2$  do
- 2 output every 1-item consequent rule of  $f_k$  with confidence  $\geq \text{minconf}$  and

$\text{Support} \leftarrow f_k \cdot \text{count} / n$  //  $n$  is the total number of transactions in  $T$

3  $H_1 \leftarrow \{\text{consequents of all 1-item consequent rules derived from } f_k \text{ above}\};$

4  $\text{ap-genRules}(f_k, H_1);$

5 endfor

Procedure  $\text{ap-genRules}(f_k, H_m)$  //  $H_m$  is the set of

1 if  $(k > m+1) \text{ AND } (H_m \neq \emptyset)$  then  $m$ -item consequents

2  $H_{m+1} \leftarrow \text{candidate-gen}(H_m);$

3 for each  $h_{m+1}$  in  $H_{m+1}$  do

4  $\text{conf} \leftarrow f_k \cdot \text{count} / (f_k - h_{m+1}) \cdot \text{count};$

5 if  $(\text{conf} \geq \text{minconf})$  then

6 output the rule  $(f_k - h_{m+1}) \rightarrow h_{m+1}$  with  
confidence =  $\text{conf}$  and  $\text{support} = f_k \cdot \text{count} / n;$   
//  $n$  is the total number of transactions  
in  $T$

7 else

8 delete  $h_{m+1}$  from  $H_{m+1};$

9 endfor

10 ap-genRules (fk, tlm+1);

11 endif

### Generation of strong association rule

#3

Itemset	Support count
{I1, I2, I3}	2
{I1, I2, I5}	2

Since the frequent itemsets satisfies the Apriori property ie, if an itemset has minimum support, then every non empty subset of this itemset also has minimum support.

Hence for Itemset = {I1, I2, I3} with minsup = 2 have the following itemsets and support counts.

Case 1: {I1, I2, I3}

Itemset	Support count
{I1}	6
{I2}	7
{I3}	6
{I1, I2}	4
{I1, I3}	4
{I2, I3}	4



Following are the various association rules that can be generated from this itemset,

1.  $\{I_1\} \rightarrow \{I_2, I_3\}$
2.  $\{I_2\} \rightarrow \{I_1, I_3\}$
3.  $\{I_3\} \rightarrow \{I_1, I_2\}$
4.  $\{I_1, I_2\} \rightarrow \{I_3\}$
5.  $\{I_1, I_3\} \rightarrow \{I_2\}$
6.  $\{I_2, I_3\} \rightarrow \{I_1\}$
7.  $\{I_1, I_2, I_3\} \rightarrow \emptyset$  (Not considering since it is a nullset)

\* Confidence of Rule 1.  $[\{I_1\} \rightarrow \{I_2, I_3\}]$

$$\begin{aligned} \text{Confidence} &= \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_1\})} \\ &= \frac{2}{6} = \frac{1}{3} = \frac{0.33}{1} = \underline{\underline{33.33\%}} \end{aligned}$$

\* Confidence of Rule 2.  $[\{I_2\} \rightarrow \{I_1, I_3\}]$

$$\begin{aligned} \text{Confidence} &= \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_2\})} \\ &= \frac{2}{7} = 0.2857 = \underline{\underline{28.7\%}} \end{aligned}$$

\* Confidence of Rule 3  $\{I_3\} \rightarrow \{I_1, I_2\}$

$$\text{confidence} = \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_3\})}$$

$$= \frac{2}{6} = \underline{\underline{33.3\%}}$$

\* Confidence of Rule 4  $\{I_1, I_2\} \rightarrow \{I_3\}$

$$\text{confidence} = \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_1, I_2\})}$$

$$= \frac{2}{4} = \underline{\underline{50\%}}$$

\* Confidence of Rule 5  $\{I_1, I_3\} \rightarrow \{I_2\}$

$$\text{confidence} = \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_1, I_3\})}$$

$$= \frac{2}{4} = \underline{\underline{50\%}}$$

\* Confidence of Rule 6  $\{I_2, I_3\} \rightarrow \{I_1\}$

$$\text{confidence} = \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_2, I_3\})}$$

$$= \frac{2}{4} = \underline{\underline{50\%}}$$

Since none of the generated association rules have confidence  $\geq \text{minconf}$  i.e., 70%. These rules are not strong association rules.

Case 2:

Frequent itemset =  $\{I_1, I_2, I_5\}$  with support count = 2

Subsets of items	Support count
$\{I_1\}$	6
$\{I_2\}$	7
$\{I_5\}$	2
$\{I_1, I_2\}$	4
$\{I_1, I_5\}$	4
$\{I_2, I_5\}$	2

Following are the various association rules that can be generated from this itemset

1.  $\{I_1\} \rightarrow \{I_2, I_5\}$
2.  $\{I_2\} \rightarrow \{I_1, I_5\}$
3.  $\{I_5\} \rightarrow \{I_1, I_2\}$
4.  $\{I_1, I_2\} \rightarrow \{I_5\}$

$$5. \{I1, I5\} \rightarrow \{I2\}$$

$$6. \{I2, I5\} \rightarrow \{I1\}$$

$$\{I1, I2, I5\} \rightarrow \emptyset \text{ (Since it is nullset)}$$

\* Confidence of Rule 1  $[\{I1\} \rightarrow \{I2, I5\}]$

$$\text{Confidence} = \frac{\text{sup.count}(\{I1, I2, I5\})}{\text{sup.count}(\{I1\})}$$

$$= \frac{2}{6} = \frac{1}{3} = \underline{\underline{33.3\%}}$$

\* Confidence of Rule 2  $[\{I2\} \rightarrow \{I1, I5\}]$

$$\text{Confidence} = \frac{\text{sup.count}(\{I1, I2, I5\})}{\text{sup.count}(\{I2\})}$$

$$= \frac{2}{7} = \underline{\underline{28.5\%}}$$

\* Confidence of Rule 3  $[\{I5\} \rightarrow \{I1, I2\}]$

$$\text{Confidence} = \frac{\text{sup.count}(\{I1, I2, I5\})}{\text{sup.count}(\{I5\})}$$

$$= \frac{2}{2} = \underline{\underline{100\%}}$$



\* Confidence of Rule 4  $\{I_1, I_2\} \rightarrow \{I_3\}$

$$\text{confidence} = \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_1, I_2\})}$$

$$= \frac{2}{4} = \underline{\underline{50\%}}$$

\* Confidence of Rule 5  $\{I_1, I_5\} \rightarrow \{I_2\}$

$$\text{confidence} = \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_1, I_5\})}$$

$$= \frac{2}{2} = \underline{\underline{100\%}}$$

\* Confidence of Rule 6  $\{I_2, I_5\} \rightarrow \{I_1\}$

$$\text{confidence} = \frac{\text{sup.count}(\{I_1, I_2, I_3\})}{\text{sup.count}(\{I_2, I_5\})}$$

$$= \frac{2}{2} = \underline{\underline{100\%}}$$

Minimum confidence of association rules are 70%  
Association rules having min.conf  $\geq 70\%$  are strong  
association rules.

Here strong association rules that can be generated from the given market basket data frequent itemset  $I_3$  is

$\{I_5\} \rightarrow \{I_1, I_2\}$  with conf = 100%

$\{I_1, I_5\} \rightarrow \{I_2\}$  with conf = 100%

$\{I_2, I_5\} \rightarrow \{I_1\}$  conf = 100%.

F2

Itemset	Sup. count
$\{I_1, I_2\}$	4
$\{I_1, I_3\}$	4
$\{I_1, I_5\}$	2
$\{I_2, I_3\}$	4
$\{I_2, I_4\}$	2
$\{I_2, I_5\}$	2

i)  $\{I_1, I_2\}$

Subsets are  $\{I_1\}$   $\{I_2\}$  and  $\{I_1, I_2\}$

①  $\{I_1\} \rightarrow \{I_2\}$

2.  $\{I_2\} \rightarrow \{I_1\}$

3.  $\{I_1, I_2\} \rightarrow \emptyset$  - Not possible

Confidence of Rule ①  $\{I_1\} \rightarrow \{I_2\}$

$$\text{Conf} = \frac{\text{sup. count}(\{I_1, I_2\})}{\text{sup count}(\{I_1\})}$$

$$= \frac{4}{6} = \frac{2}{3} = \underline{\underline{66\%}}$$

\* Confidence of Rule ②  $\{I_2\} \rightarrow \{I_1\}$

$$\text{conf} = \frac{4}{7} = \underline{\underline{57\%}}$$

ii)  $\{I_1, I_3\}$

③  $\{I_1\} \rightarrow \{I_3\}$

④  $\{I_3\} \rightarrow \{I_1\}$

confidence of ③  $\{I_1\} \rightarrow \{I_3\}$

$$\text{conf} = \frac{4}{6} = \underline{\underline{66\%}}$$

confidence of ④  $\{I_3\} \rightarrow \{I_1\}$

$$\text{conf} = \frac{4}{6} = \underline{\underline{66\%}}$$

iii)  $\{I_1, I_5\}$

⑤  $\{I_1\} \rightarrow \{I_5\}$

⑥  $\{I_5\} \rightarrow \{I_1\}$

confidence of ⑤  $\{I_1\} \rightarrow \{I_5\}$

$$\text{conf} = \frac{2}{6} = \underline{\underline{33.3\%}}$$

iv)  $\{I_2, I_3\}$ 

(7)  $\{I_2\} \rightarrow \{I_3\}$

(8)  $\{I_3\} \rightarrow \{I_2\}$

Conf. of Rule (7)  $\{I_2\} \rightarrow \{I_3\}$ 

$$\text{conf} = \frac{4}{7} = \underline{\underline{57\%}}$$

Confidence of Rule (8)  $\{I_3\} \rightarrow \{I_2\}$ 

$$\text{conf} = \frac{4}{6} = \underline{\underline{66\%}}$$

v)  $\{I_2, I_4\}$ 

(9)  $\{I_2\} \rightarrow \{I_4\}$

(10)  $\{I_4\} \rightarrow \{I_2\}$

Confidence of Rule (9)  $\{I_2\} \rightarrow \{I_4\}$ 

$$\text{conf} = \frac{2}{7} = 28\%$$

Confidence of Rule (10)  $\{I_4\} \rightarrow \{I_2\}$ 

$$\text{conf} = \frac{2}{2} = \underline{\underline{100\%}}$$

vi)  $\{I_2, I_5\}$ 

(11)  $\{I_2\} \rightarrow \{I_5\}$



$$(12) \{I5\} \rightarrow \{I2\}$$

Confidence of Rule (11)  $\{I2\} \rightarrow \{I5\}$

$$\text{conf} = \frac{2}{7} = \underline{\underline{28.7\%}}$$

Confidence of Rule (12)  $\{I5\} \rightarrow \{I2\}$

$$\text{conf} = \frac{2}{2} = \underline{\underline{100\%}}$$

$\text{minconf} \geq 70\%$ . hence, strong association rules from  $F2$  are

$$\{I4\} \rightarrow \{I2\} \quad \text{conf} = 100\%$$

$$\{I5\} \rightarrow \{I2\} \quad \text{conf} = \underline{\underline{100\%}}$$

$F1$

Itemset	Support count
$\{I1\}$	6
$\{I2\}$	7
$\{I3\}$	6
$\{I4\}$	2
$\{I5\}$	2

Since all these Itemsets are satisfying Apriori properties

their subsets will also have minimum support count. But here  $F_1$  is 1-frequent itemset whose subsets are the same itemset itself which generates  $\phi$ . Hence the algorithm is terminated.

Strong association rules generated for this market basket data is as follows,

$$\{I_4\} \rightarrow \{I_2\}$$

$$\{I_5\} \rightarrow \{I_2\}$$

$$\{I_5\} \rightarrow \{I_1, I_2\}$$

$$\{I_1, I_5\} \rightarrow \{I_2\}$$

$$\{I_2, I_5\} \rightarrow \{I_1\}$$