

## Homework

3.) Don't Contain 110

OK 0010100

OK 0101111

Not OK 01110101

5.) DFA  $M$  recognizes language  $L$

Create DFA  $\bar{M}$

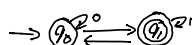
$M, \bar{M}$  have the same state

" " " transition

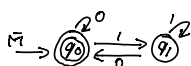
" " " Start state

States find in  $M$ , not found in  $\bar{M}$  and vice versa

Find language recognized by  $\bar{M}$



$M$  recognizes strings ending in 1  
Language  $L$



$\bar{M}$  recognizes string ending in a 0

## Notes

### Regular Operations

Def: If  $A$  and  $B$  are languages then

$$A \cup B = \{w \mid w \in A \text{ or } w \in B\}$$

union

(usually  $A, B$  have the same alphabet)

Concatenation -  $A \circ B = \{xy \mid x \in A \text{ and } y \in B\}$

Star -  $A^* = \{x_1, x_2, \dots, x_k \mid k \geq 0 \text{ and each } x_i \in A\}$

When  $k=0$ , you have the empty string,

denoted  $\epsilon \leftarrow \text{Epsilon}$

$$\Sigma = \{0, 1\}$$

$$A = \{10, 0, 11\}$$

$$B = \{011, 1, 01\}$$

$$A \cup B = \{10, 0, 11, 011, 1, 01\}$$

$$A \circ B = \{10011, 101, 1001,$$

$$0011, 01, 001$$

$$11011, 111, 1101\}$$

$$A^* = \{\epsilon, 10, 0, 11, 1010, 100$$

$$1011, 010, 00, 011, 1110$$

$$110, 1111, 101010, 1000$$

$$10111, \dots\}$$

Regular languages are closed under the operation  
 $\cup, \circ, *$

$\{w \mid w \text{ has an even number of 0's}$   
and an even number of 1's $\}$  Not a regular  
language

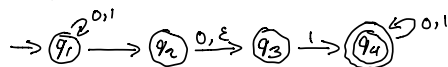
## 1.2

### Non deterministic Finite Automata (NFA)

There can be multiple possible transition with  
a given input.

The empty string  $\epsilon$  can be input.

The NFA can have no transition for  
a particular input



001 could end in  $q_1$  or  $q_2$  or  $q_3$   
but not  $q_4$ , Not recognized by NFA.