
WarWithArray.

PseudoCode:

```
Input: int k, Array a[]\nFor each string e in a[]:\n    For each string f in a[]:\n        check if the string "e+f" is valid(e+f)
```

```
function valid(s):\n    For each b = (k length substring in s):\n        Loop through our original array a:\n            check if b is in a
```

Runtime of compute2k():

The algorithm essentially 4 nested loops, they run n-times, n-times, k-times, and n-times.
So the run-time is $O(kn^3)$

WarWithBST.

PseudoCode:

```
Input: int k, Array a[]\nFor each string e in a[]:\n    For each string f in a[]:\n        check if the string "e+f" is valid(e+f)
```

```
function valid(s):\n    For each b = (k length substring in s):\n        search the BST for the substring b
```

Runtime of compute2k():

The algorithm essentially 4 nested loops, they run n-times, n-times, k-times, and log n-times.
So the run-time is $O(kn^2 \log n)$

WarWithHash.

PseudoCode:

```
Input: int k, Array a[]\
For each string e in a[]:
    For each string f in a[]:
        check if the string "e+f" is valid(e+f)
```

```
function valid(s):
    For each b = (k length substring in s):
        hash b and look it up in the HashSet
```

Runtime of compute2k():

The algorithm essentially 4 nested loops, they run n -times for the most outer loop, n -times for the second most outer loop, k -times for each substring of the $2k$ string, and k -times for the hash of the k -length string. So the run-time is $O(k^2n^2)$

WarWithRollHash.

PseudoCode:

Runtime of compute2k():