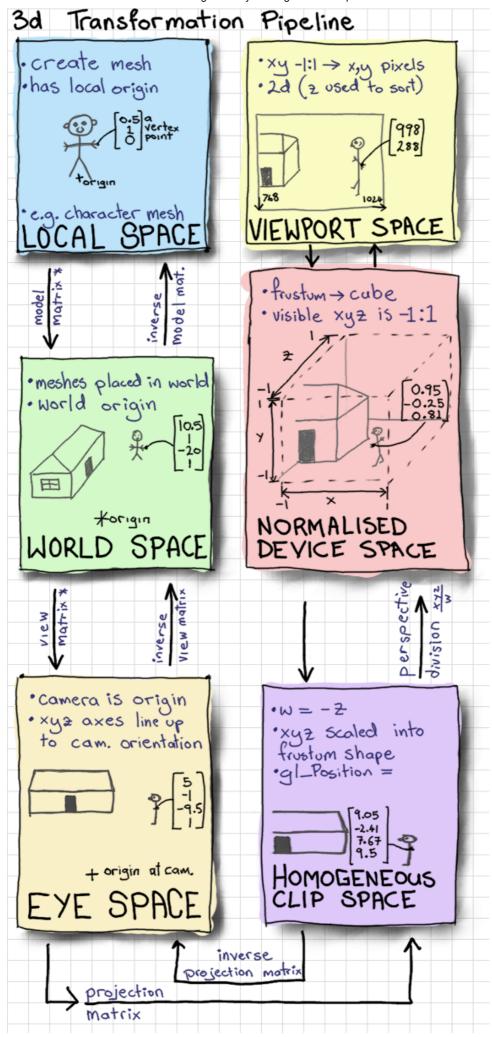
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# Mouse Picking with Ray Casting

Anton Gerdelan. Last Updated 2 October 2016

## **Overview**

It can be useful to click on, or "pick" a 3d object in our scene using the mouse cursor. **One way of doing this** is to project a 3d ray from the mouse, through the camera, into the scene, and then check if that ray intersects with any objects. This is usually called **ray casting**. This is an entirely mathematical exercise - we don't use any OpenGL code or draw any graphics - this means that it will apply to any 3d application the same way. The mathematical subject is usually called geometric **intersection testing**.



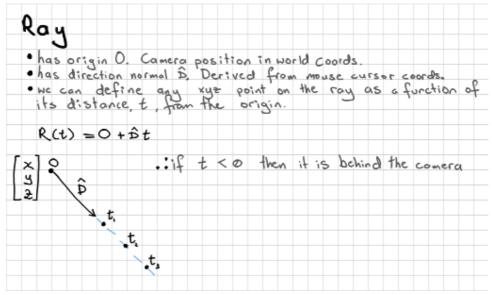
Instead of starting with a mesh in local space, we are starting with a 2d mouse cursor position in

viewport space. We work backwards through the transformation by using inverse matrices, and arrive with a ray in world space.

With ray picking we usually simplify a scene into bounding spheres or boxes. This makes the calculation a bit easier than testing all of the individual triangles. We don't need to create a 3d sphere out of triangles that can be rendered; we just represent the sphere as a simple function. The premise is that we have a mathematical formula for the points along a ray, and a mathematical formula for the points on a sphere. If we substitute the points on the sphere with the equation for points on a ray, then we get the intersection of points that are common to both. It's interesting to do this technique now because it shows us how we can use the transformation pipeline in reverse; from 2d screen to a 3d world space by using the inverse of our matrices e.g...inverse(view\_matrix) \*
inverse(projection\_matrix).... In a later tutorial we will look at an alternative technique using unique colours to determine where the mouse is hovering or clicking.

## Calculating a Ray from the Mouse

All ray casting starts with a ray. In this case it has an origin  $\mathbf{0}$  at the position of the camera. We can do ray intersections in any space (world, eye, etc.), but everything needs to be in the same space - let's assume that we are doing our calculations in world space. This means that our ray origin is going to be the world  $\mathbf{x}$ ,  $\mathbf{y}$ ,  $\mathbf{z}$  position of the camera.



This function expresses all the points, t, along an infinite ray projected from our camera location, O, in the direction D, which we will work out by modifying and normalising the mouse cursor position.

## **Step 0: 2d Viewport Coordinates**

range [0:width, height:0]

We are starting with mouse cursor coordinates. These are 2d, and in the **viewport coordinate** system. First we need to get the mouse x,y pixel coordinates. You might have set up a call-back function (with e.g. GLFW or GLUT) something like this:

void mouse\_click\_callback(int b, int s, int mouse\_x, int mouse\_y);

This gives us an x in the range of **0:width** and y from **height:0**. Remember that 0 is at the top of the screen here, so the y-axis direction is opposed to that in other coordinate systems.

### **Step 1: 3d Normalised Device Coordinates**

```
range [-1:1, -1:1, -1:1]
```

The next step is to transform it into 3d **normalised device coordinates**. This should be in the ranges of x [-1:1] y [-1:1] and z [-1:1]. We have an x and y already, so we scale their range, and reverse the direction of y.

```
float x = (2.0f * mouse_x) / width - 1.0f;
float y = 1.0f - (2.0f * mouse_y) / height;
float z = 1.0f;
vec3 ray_nds = vec3(x, y, z);
```

We don't actually need to specify a z yet, but I put one in (for the craic).

### Step 2: 4d Homogeneous Clip Coordinates

```
range [-1:1, -1:1, -1:1]
```

We want our ray's z to point forwards - this is usually the negative z direction in OpenGL style. We can add a w, just so that we have a 4d vector.

```
vec4 ray_clip = vec4(ray_nds.xy, -1.0, 1.0);
```

**Note:** we <u>do not need to reverse perspective division here</u> because this is a **ray** with no intrinsic depth. Other tutorials on ray-casting will, incorrectly, tell you to do this. Ignore the false prophets! We would do that only in the special case of points, for certain special effects.

### Step 3: 4d Eye (Camera) Coordinates

```
range [-x:x, -y:y, -z:z, -w:w]
```

Normally, to get into clip space from eye space we multiply the vector by a projection matrix. We can go backwards by multiplying by the inverse of this matrix.

```
vec4 ray_eye = inverse(projection_matrix) * ray_clip;
```

Now, we only needed to un-project the x,y part, so let's manually set the z,w part to mean "forwards, and not a point".

```
ray_eye = vec4(ray_eye.xy, -1.0, 0.0);
```

#### Step 4: 4d World Coordinates

```
range [-x:x, -y:y, -z:z, -w:w]
```

Same again, to go back another step in the transformation pipeline. Remember that we manually specified a -1 for the z component, which means that our ray isn't normalised. We should do this before we use it.

```
vec3 ray_wor = (inverse(view_matrix) * ray_eye).xyz;
// don't forget to normalise the vector at some point
ray_wor = normalise(ray_wor);
```

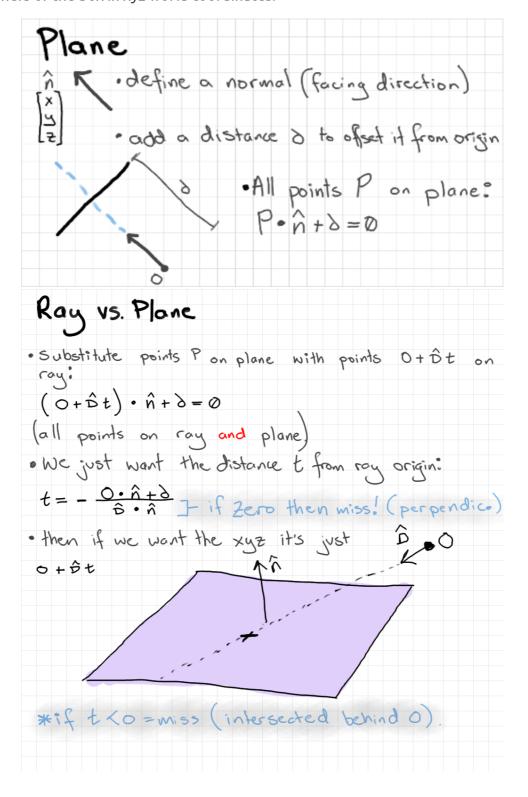
This should balance the up-and-down, left-and-right, and forwards components for us. So, assuming our camera is looking directly along the -Z world axis, we should get [0,0,-1] when the mouse is in the centre of the screen, and less significant z values when the mouse moves around the screen. This will depend on the aspect ratio, and field-of-view defined in the view and projection matrices. We now have a ray that we can compare with surfaces in world space.

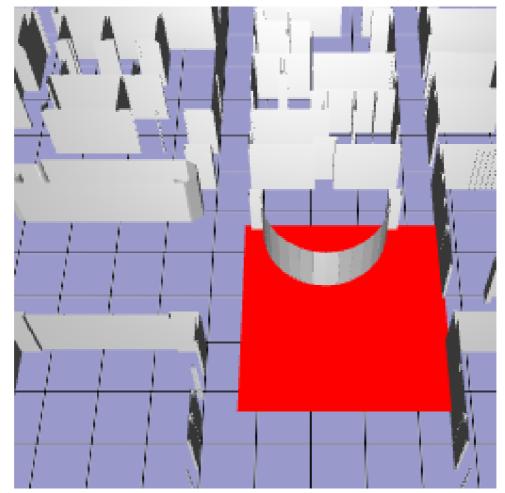
#### Shortcut

If you're happy with this theory then you can condense all of these instructions into one line.

# Ray vs. Plane

We can describe any surface as a plane. It's often useful to do this before doing more detailed (and more computationally expensive) intersection tests. We can test, for example, if a point is inside a region bounded by planes - if not, then no need to check versus individual triangles inside the region. In my case, I wanted to create an imaginary ground plane that I could use to help me click-and-drag boxes around scenery. I do 2 ray-plane intersections to get the top-left and bottom-right corners of the box in xyz world coordinates.

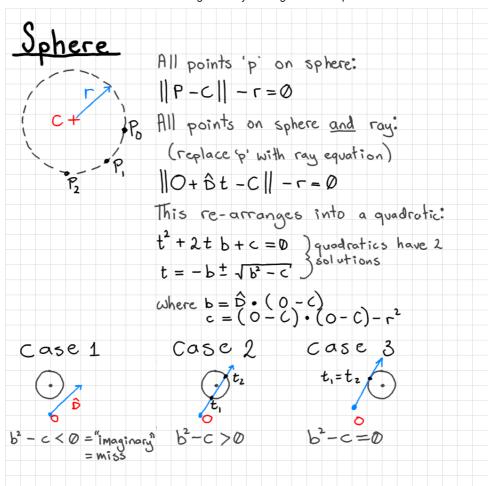




I used ray-plane intersection to allow a user to drag out a "zone" on the floor. This might be useful in strategy games where you want to select a group of units. Unless you're on a globe. In that case, read on. Note that the square is projected into depth - it isn't a true square on the 2d screen, but will be if looking from directly above it.

# Ray vs. Sphere

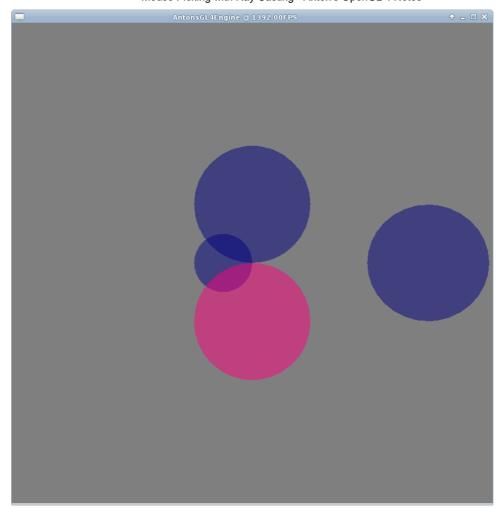
Probably the easiest method for selecting objects in a 3d scene. If you know a bounding radius, and centre point, of each object then we have the definition of its sphere. This might not be the best method to use for large, or irregularly shaped objects, which will have very large spheres that might overlap with smaller objects nearby.



Here I have an equation for all the points, P on a sphere's surface, which says "anything that is radius r distance from centre point C". The idea is to replace P with the points-along-a-ray equation, and solve for t. I skipped the re-arrangement steps, but if you're interested in a full discussion have a look at Akenine-Möller et al. Real-Time Rendering.

We can actually get 2 output intersections from a ray-sphere intersection because the ray can hit both the back and the front of the sphere. In this case we need to check for the closest intersection (smallest value of t). The ray can also miss the sphere, hit the very edge of the sphere (both t values are the same), or be cast from inside the sphere (one t value is negative).

Be sure to check the b^2 - c term <u>before</u> evaluating the expensive square root operator. If you miss the sphere entirely you will not get a sensible result for t. It is also possible that the ray will be cast from in front of or inside of the sphere, so you will need to check that your t values are positive.



Here I have a collection of spheres in 3d space. I generated these in Blender and scaled them to match the radius of my bounding sphere. They are all the same size, but one is farther away and behind the others - this was to test that only the closest intersection was being selected. When a sphere is clicked on, I changed its colour to pink. This helped me determine that the ray was being calculated correctly, and the intersection was returning the correct result. You can imagine each sphere surrounding a mesh or object that is being selected.

## **Optimisations**

You probably won't need to unless you're doing **a lot** of clicking on spheres, but you can reduce the cost of this algorithm by adding a few checks before getting to the square root. Compare squared distances between the ray origin and the sphere centre. You can project this as a 2d distance along the ray direction (dot product) and compare the end point's squared distance to the sphere origin (use Pythagoras' theorem) with the squared radius.

## Round-Up

Generally, if you want to draw on a shape (e.g. dragging boxes) then ray-casting is a good choice. If you want inaccuracy i.e. letting the user click in the general area of a fiddly little mesh to select it then ray-casting is a good choice. If you want accuracy then you're almost certainly better off using a colour-based picking method, which has the cost of one extra rendering pass, rather than 1-5 ray casts per selectable object in the scene.

# Further Things (That I Might or Might Not Add Later)

Axis-Aligned Bounding Box (AABB)

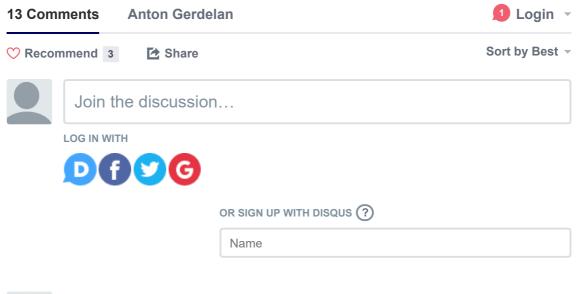
You can do ray versus axis-aligned box intersection, which is quite commonly used. An object in the world is considered to have a bounding box, rather than a bounding sphere. This has the weakness that irregularly shaped, rotating objects will create gigantic boxes, but it is quite easy to work out the extents, and use these to validate a set of ray-plane intersections.

#### Oriented Bounding Box (OBB)

If your shapes are actually boxes, or you want the box to rotate with the object inside, then you can do a ray versus oriented box intersection in much the same way. A few optimised methods exist (Haines "Essential Ray Tracing Algorithms", Chapter 2). I haven't had occasion to use this "in the wild".

#### Barycentric

Ray versus triangle collisions will let you determine exactly where on a more complex mesh that you have clicked on. If you need this much accuracy, you are probably better off using the colour buffer method and getting a pixel-correct method. It might be useful for things like shooting games where you want put a bullet hole image in an exact location though. I haven't found a good reason to use this one in a while either. Before testing several different surfaces of a complex object, it's generally advised to do a ray versus bounding sphere test first - no point testing all of the triangles if the ray has missed the whole object!





Tino Fleißner • 3 months ago

Thank you very much for this easy to understand tutorial, helped me a lot!

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Michael Fuller • 5 months ago

What additional math would be needed if your using nodes that can be embedded. Like say I have a root node at world (0,0,0) that has been arbitrarily rotated and it has a child that has been translated 25 units in the z direction. How would you get the world coordinate for that child node so I could check the ray against it? Is it the same math as when you render, take the (view matrix \* root matrix) \* child matrix?

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Anton Gerdelan Mod → Michael Fuller • 4 months ago

sorry, i didn't see this comment until now! you're describing a scene graph type of setup. when you have a parent->child relationship in a chain you can multiply their transformation matrices together in a chain to work out

the final position in world space. no, you wouldn't involve the view matrix here because that would push you into eye/view space and you want to stay in the world coordinate space.

world position = parent \* child \* childschild \* nodeoffsetposition;

reverse the order for row-major.

hope that helps someone - i guess you solved this already!



#### Michael Fuller → Anton Gerdelan • 4 months ago

Thanks, I powered through and figured it out with the node multiplication. Now the best thing that helped with implementing ray picking on my end was an example I found with input and expected output, so I could plug them into my solution and verify it actually produced the same thing.



Anton Gerdelan Mod → Michael Fuller • 4 months ago

hey that's a very good point...some test data isn't a bad idea.



#### debakanta kar • 5 months ago

can u explain me in obb algorithm instead of dot product of o and normal why they are doing it between delta and normal where delta is the vector difference of ray origin and centre of box.

See this link: http://www.opengl-tutorial....



#### Anton Gerdelan Mod Adebakanta kar • 4 months ago

as far as i recall the best reference for OBB is Eric Haines' slabs technique. i may have misremembered that! there's a whole chapter on this in the Real Time Rendering book. the diagrams there look like they are describing the same technique - i think best to go to the source!



tantk • 5 months ago

I think this works correctly only when near plane is set as 1.0.

Z component of eye coords should be distance from camera to near plane.

-> ray eye = vec4(ray eye.xy, -near, 0.0);



#### Anton Gerdelan Mod → tantk • 5 months ago

hi tantk, thanks for the feedback! i'm sure there are some subtle bugs in here because i came up with this entire thing out of my imagination during a boring conference talk without reading anything or having done it before, but i'm not sure about the particular issue that you mention. if you don't have one already there's a demo here if you want to try it out and tweak all the values https://github.com/capnrams... (it's number 07)

```
Renly Share
```



tantk - Anton Gerdelan • 5 months ago

My apologies. I deleted my comment after realized something wrong, but it seems not worked.

I actualy didn't understand that why setting z, w as -1, 0 on clip coordinates is necessary to get eye coordinates. Because z, w is totally not involved in the inverse projection multiplication. x, y of eye coordinates can be got just with  $x_{clip} / P[0][0]$ ,  $y_{clip} / P[1][1]$ . And it would be better that there is a discription mathematically why setting  $z_{eye}$  as -1 is necessay. It is caused from assuming  $z_{eye}$  as -1 to get clip coordinates(x,y) same as normallized device coordinates(x,y). If  $z_{eye}$  is -1,  $z_{eye}$  is just 1. So perspective division do nothing, and the reversion do nothing too. Anyway, I apogize again for the wrong discussion. And thank you for the great tutorial.

∧ | ∨ • Reply • Share ›



Anton Gerdelan Mod → tantk • 5 months ago

no need to apologise or delete comments - i think all discussion is good, otherwise mistakes and unclear part won't be addressed until everyone is an expert! i'm sure a more complete break-down would be good..i don't come from a background of geometric mathematics so there probably are some serious issues and things that only work under certain assumptions like that. i guess my main concern is that the very complete mathematical works are pretty tough going for 90%+ of people who i believe come to things like this page to get a result as quickly as possible. perhaps the solution is to link to a more authoritative mathematical analysis for further reading - if there's one out there that anyone finds i'd love to see it.

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Ricky658 • 6 months ago

Hi, I want to calculate the xyz intersection with plane XZ, for setting objets in the "ground" but I need distance from plane<-->ray before apply O+Dt, becouse I dont have t, in t formula need d :(



Anton Gerdelan Mod → Ricky658 • 6 months ago

d is not the distance between ray origin and plane, it's part of the definition of the plane. so it's probably 0 for you. if you have a ground plane with facing vector (0,1,0) and it's at height y=0 then the d is 0. that should do it. if your ground plane was moved up above y=0 then you can change d. A

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Vertex Buffer Objects - Anton's OpenGL 4 Notes

30 comments • 7 months ago•

Anton Gerdelan — check this video out for faster inverse() functions - https://youtu.be/7CxKAtWqHC8

Yash pal — Yea..Why not. Please:)

# **Cube Maps: Skyboxes and Environment Mapping - Anton's ...**

2 comments • a year ago•

Anton Gerdelan — hi albert! sorry, i was out of action for a few days short

#### **Shaders - Anton's OpenGL 4 Notes**

1 comment • 7 months ago•

Anton Gerdelan — hmm i think the diagram up near the top should probably not imply that /all/ of the ....