Chapter - 12

Exponents and Powers

• Numbers with negative exponents obey the following laws of exponents.

(a)
$$a^m \times a^n = a^{m+n}$$

(b)
$$a^{m} \div a^{n} = a^{m-n}$$

(c)
$$\left(a^{\mathrm{m}}\right)^{\mathrm{n}} = a^{\mathrm{mn}}$$

(d)
$$a^{\mathrm{m}} \times b^{\mathrm{m}} = (ab)^{\mathrm{m}}$$

(e)
$$a^0 = 1$$

$$(f)\frac{a^{m}}{b^{m}} = \left(\frac{a}{b}\right)^{m}$$

- Very small numbers can be expressed in standard form using negative exponents.
- Use of Exponents to Express Small Number in Standard form:
 - (i) Very large and very small numbers can be expressed in standard form.
 - (ii) Standard form is also called scientific notation form.
 - (iii) A number written as $m \times 10^n$ is said to be in standard form if m is a decimal number such that $1 \le m < 10$ and n is either a positive or a negative integer.

Examples: $150,000,000,000 = 1.5 \times 10^{11}$.

• Exponential notation is a powerful way to express repeated multiplication of the same number. For any non-zero rational number 'a' and a natural number n, the product $a \times a \times a \times ... \times a(n \, times) = a^n$. It is known as the nth power of 'a' and is read as 'a' raised to the power n'. The rational number a is called the base and n is called exponent.