## hw1p3

## September 26, 2023

```
[]: import numpy as np from scipy.optimize import fsolve
```

Possible to have different answers for these datasets, but they will all be pretty close to making the dataset work

## Dataset 1

```
[2]: def f(p): #Formula's followed in the neural network plus the addition of
      subtracting the outout value, as fsolve revolves around making the equation
      ⇔equal to 0
         input = [0,1,2,3,4,5,6,7,8,9,10,11,12]
         output = [8, 6, 4, 2, 0, 2, 4, 2, 0, 2, 4, 6, 8]
         return [p[12] + p[8]*max(0,p[0]*input[0] + p[4]) + p[9]*max(0,p[1]*input[0]_
       \downarrow+ p[5]) + p[10]*max(0,p[2]*input[0] + p[6]) + p[11]*max(0,p[3]*input[0] +
      \rightarrowp[7]) - output[0],
         p[12] + p[8]*max(0,p[0]*input[1] + p[4]) + p[9]*max(0,p[1]*input[1] + p[5])
      \hookrightarrow+ p[10]*max(0,p[2]*input[1] + p[6]) + p[11]*max(0,p[3]*input[1] + p[7]) - \Box
      →output[1],
         p[12] + p[8]*max(0,p[0]*input[2] + p[4]) + p[9]*max(0,p[1]*input[2] + p[5])_{u}
      \Rightarrow+ p[10]*max(0,p[2]*input[2] + p[6]) + p[11]*max(0,p[3]*input[2] + p[7]) - \Box
      →output[2],
         p[12] + p[8]*max(0,p[0]*input[3] + p[4]) + p[9]*max(0,p[1]*input[3] + p[5])
      \hookrightarrow+ p[10]*max(0,p[2]*input[3] + p[6]) + p[11]*max(0,p[3]*input[3] + p[7]) - \Box
       →output[3],
         p[12] + p[8]*max(0,p[0]*input[4] + p[4]) + p[9]*max(0,p[1]*input[4] + p[5])
      \hookrightarrow+ p[10]*max(0,p[2]*input[4] + p[6]) + p[11]*max(0,p[3]*input[4] + p[7]) - \Box
      output [4],
         p[12] + p[8]*max(0,p[0]*input[5] + p[4]) + p[9]*max(0,p[1]*input[5] + p[5])
      \hookrightarrow+ p[10]*max(0,p[2]*input[5] + p[6]) + p[11]*max(0,p[3]*input[5] + p[7]) - \Box
       →output[5],
         p[12] + p[8]*max(0,p[0]*input[6] + p[4]) + p[9]*max(0,p[1]*input[6] + p[5])
      \hookrightarrow + p[10]*max(0,p[2]*input[6] + p[6]) + p[11]*max(0,p[3]*input[6] + p[7]) - \Box
      ⇔output[6],
         p[12] + p[8]*max(0,p[0]*input[7] + p[4]) + p[9]*max(0,p[1]*input[7] + p[5])_{\square}
      \Rightarrow+ p[10]*max(0,p[2]*input[7] + p[6]) + p[11]*max(0,p[3]*input[7] + p[7]) - \Box
       \hookrightarrowoutput [7],
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p[12] + p[8] *max(0,p[0] *input[8] + p[4]) + p[9] *max(0,p[1] *input[8] + p[5])__
      + p[10]*max(0,p[2]*input[8] + p[6]) + p[11]*max(0,p[3]*input[8] + p[7]) - 
      output[8],
         p[12] + p[8]*max(0,p[0]*input[9] + p[4]) + p[9]*max(0,p[1]*input[9] + p[5])_{\bot}
      + p[10] *max(0,p[2] *input[9] + p[6]) + p[11] *max(0,p[3] *input[9] + p[7]) -
      output [9],
         p[12] + p[8]*max(0,p[0]*input[10] + p[4]) + p[9]*max(0,p[1]*input[10] + |
      \neg p[5]) + p[10]*max(0,p[2]*input[10] + <math>p[6]) + p[11]*max(0,p[3]*input[10] + <math>\mu
      \rightarrowp[7]) - output[10],
         p[12] + p[8]*max(0,p[0]*input[11] + p[4]) + p[9]*max(0,p[1]*input[11] + [1])
      \neg p[5]) + p[10]*max(0,p[2]*input[11] + p[6]) + <math>p[11]*max(0,p[3]*input[11] + \Box
      \rightarrowp[7]) - output[11],
         \neg p[5]) + p[10]*max(0,p[2]*input[12] + <math>p[6]) + p[11]*max(0,p[3]*input[12] + <math>p[6]
      →p[7]) - output[12]]
[3]: initial_guess = np.random.normal(size =13)
     solution = fsolve(f, initial guess)
     while not(np.all(np.isclose(f(solution),[0]*13)==True)):
      new_guess = np.random.normal(size =13)
       solution = fsolve(f, new_guess)
     solution
    C:\Users\Anil\AppData\Local\Programs\Python\Python310\lib\site-
    packages\scipy\optimize\ minpack py.py:177: RuntimeWarning: The iteration is not
    making good progress, as measured by the
      improvement from the last ten iterations.
      warnings.warn(msg, RuntimeWarning)
    C:\Users\Anil\AppData\Local\Programs\Python\Python310\lib\site-
    packages\scipy\optimize\_minpack_py.py:177: RuntimeWarning: The iteration is not
    making good progress, as measured by the
      improvement from the last five Jacobian evaluations.
      warnings.warn(msg, RuntimeWarning)
[3]: array([-7.82455998e-01, -5.16665284e-01, 1.32120087e+00, -3.55189485e+00,
             6.25964798e+00, 3.09863545e+00, -1.05696070e+01, 1.42169031e+01,
             2.55605428e+00, -7.76233237e+00, 1.51377436e+00, 1.12912342e+00,
             2.69958647e-11])
[4]: f(solution) #Closer to 0 the better
[4]: [-1.751665479332587e-11,
     -2.9530156098189764e-11,
     -4.154543375989306e-11,
      -5.356071142159635e-11,
      -6.557229412229582e-11,
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-1.637445734559151e-11,

-6.759481863127803e-12,

-1.2145839889399213e-12,

2.6995864717007652e-11,

3.0686564400639327e-13,

2.851052727237402e-13,

2.6290081223123707e-13,

2.398081733190338e-13]
```

## Dataset 2

```
[5]: def f(p): #Added 2 repetitive lines at the bottom of this one so that the shape
      ⇒would line up but it doesn't affect the actual results
         input = [0,1,2,3,4,5,6,7,8,9,10]
         output = [0,1,2,3,2,1,2,3,4,5,6]
         return [p[12] + p[8]*max(0,p[0]*input[0] + p[4]) + p[9]*max(0,p[1]*input[0]_
      \Rightarrow+ p[5]) + p[10]*max(0,p[2]*input[0] + p[6]) + p[11]*max(0,p[3]*input[0] + \Box
      \rightarrowp[7]) - output[0],
         p[12] + p[8]*max(0,p[0]*input[1] + p[4]) + p[9]*max(0,p[1]*input[1] + p[5])
      + p[10]*max(0,p[2]*input[1] + p[6]) + p[11]*max(0,p[3]*input[1] + p[7]) -
      ⇔output[1],
         p[12] + p[8]*max(0,p[0]*input[2] + p[4]) + p[9]*max(0,p[1]*input[2] + p[5])_{U}
      \Rightarrow+ p[10]*max(0,p[2]*input[2] + p[6]) + p[11]*max(0,p[3]*input[2] + p[7]) -
      ⇔output[2],
         p[12] + p[8]*max(0,p[0]*input[3] + p[4]) + p[9]*max(0,p[1]*input[3] + p[5])_{11}
      \hookrightarrow + p[10]*max(0,p[2]*input[3] + p[6]) + p[11]*max(0,p[3]*input[3] + p[7]) - \Box
      →output[3],
         p[12] + p[8]*max(0,p[0]*input[4] + p[4]) + p[9]*max(0,p[1]*input[4] + p[5])_{\sqcup}
      \Rightarrow+ p[10]*max(0,p[2]*input[4] + p[6]) + p[11]*max(0,p[3]*input[4] + p[7]) - \Box
      →output[4],
         p[12] + p[8]*max(0,p[0]*input[5] + p[4]) + p[9]*max(0,p[1]*input[5] + p[5])
      \Rightarrow+ p[10]*max(0,p[2]*input[5] + p[6]) + p[11]*max(0,p[3]*input[5] + p[7]) -
      →output[5],
         p[12] + p[8]*max(0,p[0]*input[6] + p[4]) + p[9]*max(0,p[1]*input[6] + p[5])_{u}
      + p[10]*max(0,p[2]*input[6] + p[6]) + p[11]*max(0,p[3]*input[6] + p[7]) -
      ⇔output[6],
         p[12] + p[8]*max(0,p[0]*input[7] + p[4]) + p[9]*max(0,p[1]*input[7] + p[5])
      + p[10] *max(0,p[2] *input[7] + p[6]) + p[11] *max(0,p[3] *input[7] + p[7]) - 1
      \hookrightarrowoutput [7],
         p[12] + p[8]*max(0,p[0]*input[8] + p[4]) + p[9]*max(0,p[1]*input[8] + p[5])_{\bot}
      + p[10]*max(0,p[2]*input[8] + p[6]) + p[11]*max(0,p[3]*input[8] + p[7]) -
      ⇔output[8],
         p[12] + p[8]*max(0,p[0]*input[9] + p[4]) + p[9]*max(0,p[1]*input[9] + p[5])_{u}
      \downarrow+ p[10]*max(0,p[2]*input[9] + p[6]) + p[11]*max(0,p[3]*input[9] + p[7]) -
      →output[9],
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p[12] + p[8]*max(0,p[0]*input[10] + p[4]) + p[9]*max(0,p[1]*input[10] + [10])
       \neg p[5]) + p[10]*max(0,p[2]*input[10] + <math>p[6]) + p[11]*max(0,p[3]*input[10] + <math>\mu
       \rightarrowp[7]) - output[10],
         p[12] + p[8]*max(0,p[0]*input[10] + p[4]) + p[9]*max(0,p[1]*input[10] + [10])
       \neg p[5]) + p[10]*max(0,p[2]*input[10] + <math>p[6]) + p[11]*max(0,p[3]*input[10] + <math>p[6]
       \rightarrowp[7]) - output[10],
         p[12] + p[8]*max(0,p[0]*input[10] + p[4]) + p[9]*max(0,p[1]*input[10] + |
       \neg p[5]) + p[10]*max(0,p[2]*input[10] + p[6]) + p[11]*max(0,p[3]*input[10] + <math>\square
       \rightarrowp[7]) - output[10]]
[6]: initial guess = np.random.normal(size =13)
     solution = fsolve(f, initial guess)
     while not(np.all(np.isclose(f(solution),[0]*13)==True)):
       new_guess = np.random.normal(size =13)
       solution = fsolve(f, new_guess)
     solution
[6]: array([ -0.35614338,
                              0.05176055,
                                              0.04679073,
                                                             4.26739128,
                              0.69438611,
                                              0.33182292, -21.3355306,
               1.06854914,
              -5.61759265, -20.45828289,
                                             1.24519253,
                                                             0.46882705,
              19.79543786])
[7]: f(solution)
[7]: [4.218847493575595e-15,
      7.105427357601002e-15,
      6.217248937900877e-15,
      3.552713678800501e-15,
      8.881784197001252e-16,
      4.440892098500626e-16,
      0.0,
      1.7763568394002505e-15,
      2.6645352591003757e-15,
      -8.881784197001252e-16,
      1.7763568394002505e-15,
      1.7763568394002505e-15,
      1.7763568394002505e-15]
[]:
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