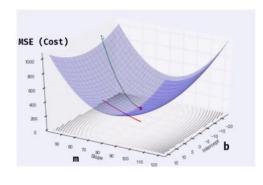
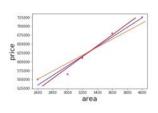
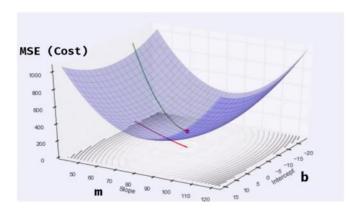


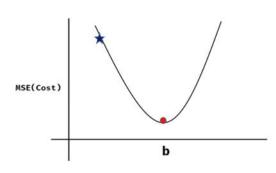
Mean Squared Error
$$ms\varepsilon = \frac{1}{n} \sum_{i=1}^{n} (y_i - (mx_i + b))^2$$
Cost Function

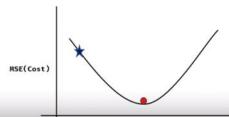
Gradient descent is an algorithm that finds best fit line for given training data set

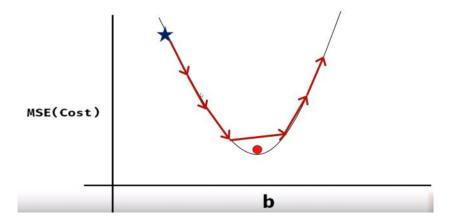




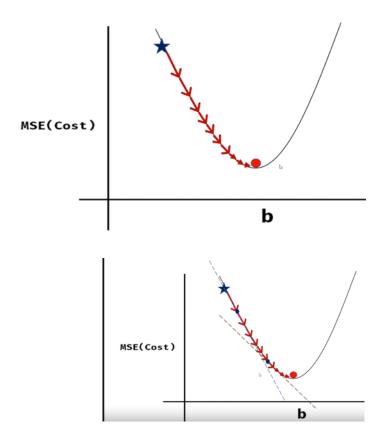








Fix values of y then we can miss the Minimum value of curvature.



Slope = Change in Y
Change in X

Change in X

We can find an **average** slope between two points.



average slope = $\frac{24}{15}$

But how do we find the slope at a point?

There is nothing to measure!



slope = $\frac{0}{0}$ = ???



But with derivatives we use a small difference ...

... then have it shrink towards zero.

We write dx instead of "Ax heads towards 0".

And "the derivative of" is commonly written $\frac{d}{dx}$:

$$\frac{d}{dx}x^2 = 2x$$

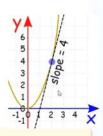
"The derivative of x^2 equals 2x" or simply "d dx of x^2 equals 2x"

What does $\frac{d}{dx}x^2 = 2x$ mean?

It means that, for the function x^2 , the slope or "rate of change" at any point is 2x

So when x=2 the slope is 2x = 4, as shown here:

Or when x=5 the slope is 2x = 10, and so on.



Note: sometimes f'(x) is also used for "the derivative of":

$$f'(x) = 2x$$

$$f(x,y) = x^3 + y^2$$

$$\frac{\partial f}{\partial x} = 3x^2 + 0 = 3x^2$$

$$\frac{\partial f}{\partial y} = 0 + 2y = 2y$$

$$ms\varepsilon = \frac{1}{n} \sum_{i=1}^{n} (y_i - (mx_i + b))^2$$

To solve our problem

We need to find the partial derivative of m and b

Partial derivatives gives the slope

$$\partial/\partial m = \frac{2}{n} \sum_{i=1}^{n} -x_i \left(y_i - (mx_i + b) \right)$$

$$\partial/\partial b = \frac{2}{n}\sum_{i=1}^{n} -(y_i - (mx_i + b))$$

$$m = m - learning rate * \frac{\partial}{\partial m}$$

$$b = b - learning rate * \frac{\partial}{\partial b}$$

