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Wait-free synchronisation for inter-process communication in real-time systems

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Declaration of Originality

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Kurzfassung

Vorhersehbare und korrekte Interprozesskommunikation (IPC) ist für Echtzeitsysteme von entscheidender Bedeutung, da Verzögerungen, Unvorhersehbarkeit oder inkonsistente Datenstände zu Instabilität und Ausfällen führen können. Traditionelle Synchronisationsmechanismen verursachen Blockierungen, die zu Prioritätsinversionen und erhöhten Antwortzeiten führen. Um diese Herausforderungen zu bewältigen, bietet die wartefreie Synchronisation eine Alternative, die den Abschluss von, wie der Austausch von Daten zwischen mehreren Prozessen, in einer begrenzten Anzahl von Schritten garantiert und so die Systemreaktionsfähigkeit und -zuverlässigkeit sicherstellt.

Diese Arbeit untersucht die Nutzung von wait-free Datenstrukturen für IPC in Echtzeitsystemen mit Fokus auf deren Implementierung in Rust. Das Eigentumsmodell und die strengen Nebenläufigkeitsgarantien von Rust machen es besonders geeignet für die Entwicklung latenzarmer und hochzuverlässiger Synchronisationsmechanismen. Diese Arbeit analysiert bestehende wait-free Methoden für IPC in Echtzeitsystemen und bewertet ihre Leistung im Vergleich zu herkömmlichen Synchronisationsmethoden.

Stichwörter: Echtzeitsysteme, wait-free Synchronisation, lock-free Synchronisation, Interprozesskommunikation, rust

Abstract

Predictable and correct Inter-Process Communication (IPC) is essential for Real-Time System (RTS), where delays, unpredictability or inconsistent data can lead to instability and failures. Traditional synchronization mechanisms introduce blocking, leading to priority inversion and increased response times. To overcome these challenges, wait-free synchronization provides an alternative that guarantees operation completion, such as the completion of data exchange between multiple processes, within a bounded number of steps, ensuring system responsiveness and reliability.

This thesis explores the use of wait-free data structures for IPC in RTS, focusing on their implementation in Rust. Rust's ownership model and strict concurrency guarantees make it well-suited for developing low-latency and high-reliability synchronization mechanisms. This work examines existing wait-free techniques for real-time IPC, and evaluates their performance against conventional synchronization methods.

Keywords: real-time systems, wait-free synchronization, lock-free synchronization, inter-process communication, rust

Contents

Kurzfassung	ii
Abstract	iii
1. Introduction	1
1.1. Motivation	1
1.2. Objective	2
1.3. Structure of the Thesis	2
2. Background	3
2.1. Real-Time Systems	3
2.2. Inter-Process Communication	3
2.2.1. Shared Memory	4
2.3. Synchronization	4
2.3.1. Mutual Exclusion	5
2.4. Lock-Free Synchronization	7
2.4.1. Michael and Scott's Lock-Free Queue	8
2.4.2. Atomic Primitives	10
2.5. Wait-Free Synchronization	11
2.6. Rust Programming Language	12
3. Related Work	13
4. Methodology	15
5. Analyzing existing Wait-Free Data Structures and Algorithms	17
5.1. Optimal Wait-Free Data Structure	17
5.2. Wait-Free Algorithms	17
5.2.1. Single Producer Single Consumer (SPSC)	18
5.2.2. Multi Producer Single Consumer (MPSC)	28
5.2.3. Single Producer Multi Consumer (SPMC)	35
5.2.4. Multi Producer Multi Consumer (MPMC)	36
6. Implementation	52
7. Benchmarking and Results	53
8. Conclusion and Future Work	54

Contents

Bibliography	55
List of Acronyms	61
A. Appendix	65

1. Introduction

1.1. Motivation

In modern manufacturing and automation, control systems must operate under strict timing constraints to function reliably. If a system fails to meet these constraints, unexpected delays can disrupt processes, leading to instability or even hazardous failures in safety-critical environments. For this reason, RTS and low-level programming languages like C or Rust are widely used to ensure predictable execution times.

To achieve these strict timing requirements, many real-time applications involve multiple tasks that must run concurrently and share resources efficiently. Without proper synchronization, problems such as data corruption or race conditions can occur leading to unpredictable behavior. Traditional synchronization methods with locks are commonly used to manage access to shared resources by blocking processes so that only one process at a time accesses the shared resource to exchange data in a proper way. However, these blocking mechanisms introduce significant challenges in real-time settings. Since Traditional synchronization methods require processes to wait for resource availability, they can lead to increased response times, potential deadlocks, potential process starvations, and potential priority inversions. These delays are unacceptable in systems that require strict timing guarantees. [1]–[3]

To overcome these limitations, there is an increasing interest in synchronization techniques without any blocking mechanisms. A lock-free algorithm for instance functions without any locking mechanism thus no blocking. This guarantees that at least one process completes in a finite number of steps, regardless of contention (multiple processes try to access the same shared resource). This property ensures that at least the system will still work even though one process might be lagging. The only problem is that this will not handle starvation since there is no guarantee that every process will finish its task. [4]

While lock-free algorithms represent a significant improvement, wait-free algorithms guarantee that every operation completes in a finite number of steps, regardless of contention. This property ensures system responsiveness and predictability, which are essential for real-time applications. By eliminating blocking and contention-based delays, wait-free synchronization prevents priority inversion and ensures that high-priority tasks execute without interference. [1], [2], [4]

These synchronization mechanisms are particularly important in the context of IPC, which plays a crucial role in RTS. IPC allows processes to exchange data efficiently, but its performance is heavily influenced by the synchronization techniques used. Traditional IPC mechanisms, which often rely on blocking some processes, can introduce significant latency and reduce throughput. Wait-free data structures offer a promising alternative by ensuring that communi-

1. Introduction

cation operations complete within predictable time bounds. However, selecting appropriate wait-free data structures and evaluating their performance in real-time environments remains a challenge. [5]–[8]

To implement these advanced synchronization techniques safely, the choice of programming language is crucial. The Rust programming language provides useful features for implementing real-time synchronization mechanisms. Its ownership model and strict type system prevents data races and enforce safe concurrency. Additionally, Rust offers fine-grained control over system resources, making it a strong candidate for real-time applications that demand both low latency and high reliability. [9], [10]

The concepts and methods introduced here, including RTS, IPC, synchronization techniques and problems, wait-free synchronization, and the rust programming language are explored in greater depth in chapter 2.

1.2. Objective

The primary goal of this research is to find wait-free data structures that can be used to implement a wait-free synchronization for IPC though shared memory in RTS using Rust. To do so, this study aims to:

- Identify and analyze existing wait-free synchronization techniques for IPC through shared memory for RTS.
- Implement and compare the performance of existing wait-free synchronization mechanisms for IPC through a shared memory for real-time scenarios with each other.
- Choose and analyze which wait-free data structure for IPC through shared memory in a real-time setting using Rust that is best suited.

By addressing these objectives, this work contributes to the field of wait-free synchronization for IPC in RTS by providing a practical solution with rust. The insights gained from this research can help improve the reliability and performance of real-time applications across various domains.

1.3. Structure of the Thesis

2. Background

To establish a clear foundation for the concepts and definitions introduced throughout this thesis, a fundamental overview of the key topics relevant to this research will be provided. This includes an introduction to RTS, Inter-Process Communication (IPC), and synchronization techniques, with a particular focus on wait-free synchronization. Additionally, the Rust programming language will be examined, as it serves as the primary development environment for this study. Furthermore, existing synchronization methods in RTS will be explored to contextualize the motivation and contributions of this work.

2.1. Real-Time Systems

In RTS the correctness of the system does not only depend on the logical results of computations, but also on timing constraints. These systems can be classified into Hard Real-Time System (HRTS) or Soft Real-Time System (SRTS). HRTS have strict timing constraints, and missing a constraint is considered a system failure and may lead to a catastrophic disaster. The system must guarantee that every timing constraint has to be met. An use case would be industrial automation where all the machines and robotic modules have to communicate with each other as quick as possible to ensure no blockage of the manufacturing line. [11]

On the other hand, SRTS try to stick to the timing constraints as much as possible, but missing some timing constraints is not considered a system failure. Infrastructure wise SRTS are similar to HRTS, since it is still considered important to meet these timing constraints. An example would be a multimedia system where it would be considered fine if sometimes frames are dropped to guarantee the video stream. [11]

Sometimes these two systems appear in combination, where some functions have hard real-time constraints and some have soft real-time constraints. Krishna K. gives a good example in his paper where he describes that for the apollo 11 mission some components for the landing processes had soft real-time behavior and the rest still functioned with hard real-time constraints. [11]

Since the workfield of this thesis is within HRTS, the term RTS will be used synonymously with the terminology HRTS.

2.2. Inter-Process Communication

Processes used in a RTS also have to share information with each other so the system can function. So some kind of IPC is needed. IPC allows processes to share information with each

2. Background

other using different kind of methods like a shared memory region, which will be the method used and explained later in this thesis. In general, IPC is needed in all computing systems, because processes often need to work together (e.g. a producer process passes data to a consumer process). Lets take the brake-by-wire technology as example. Brake-by-wire is a technology for driverless cars where some mechanical and hydraulic components from the braking systems are replaced by wires to transmit braking signals, since there is no driver anymore to press on the braking pedal [12]. This of course requires different processes to share information together. In the context of this thesis this kind of communication requires strict timing constraints as stated as before, since any kind of delay or blockage would lead to fatal consequences. [13], [14]

2.2.1. Shared Memory

To achieve any kind of information sharing between processes, these processes will need to have access to the same data regularly. With a shared memory segment, multiple processes can have access to the same memory location. So all processes which are part of the IPC can read and write to this common memory space avoiding unnecessary data copys. With that, processes exchange information by directly manipulating memory. This kind of IPC is particular useful for real-time applications, which handle large volumes of data or are required to quickly transfer data between sensors and control tasks. What is also important to know is that the section of the code, that programs these data accesses by different processes is called critical section. The problem with this is that the system somehow has to manage how the processes access the shared memory segment. This is mostly done by using different kind of synchronization techniques. Without any synchronization mechanism race conditions or inconsistent data can occur. [15]

2.3. Synchronization

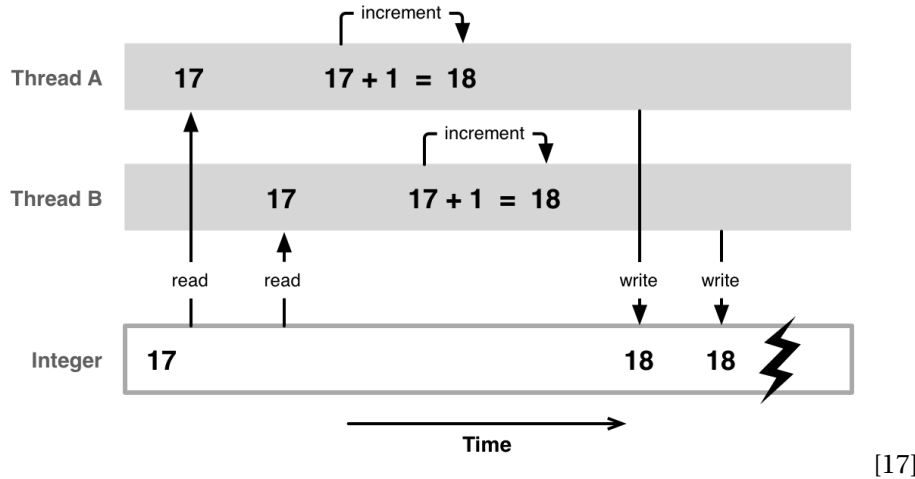
As observed, synchronization is a crucial part of IPC in RTS, especially when processes communicate via shared memory. Communication through shared memory always has a risk of race conditions and data inconsistency if the processes are not properly synchronized. Traditional synchronization techniques ensure mutual exclusion (only one process at a time uses shared resource) thus avoiding race conditions and ensuring data consistency. Race conditions happen when for example two processes write to the same resource. Lets take a single counter instance with value 17 as a shared resource in a shared memory region. If one has process p1 and one process p2 increments that number, the end result should be 19. But what could happen is that p1 could read the value 17 before p2 increments it and then before p1 increments that value p2 could also read the value 17. Now internally both processes increment that number to 18 and both processes would write 18 to that shared resource. To understand this example more in detail fig. 2.1 visualizes a race condition with threads.

The difference between processes and threads is just, that threads are part of a process which can perform multiple tasks via threads simultaneously within that process. Another

2. Background

difference that will later be important in this thesis is that processes have their own private memory space, while threads share the memory space of the process they are part of. So naturally a process can not access the memory of another process. Regardless the following concept in fig. 2.1 can be used for processes too. [16]

Figure 2.1.: Race condition between two threads, which write to the same shared variable.



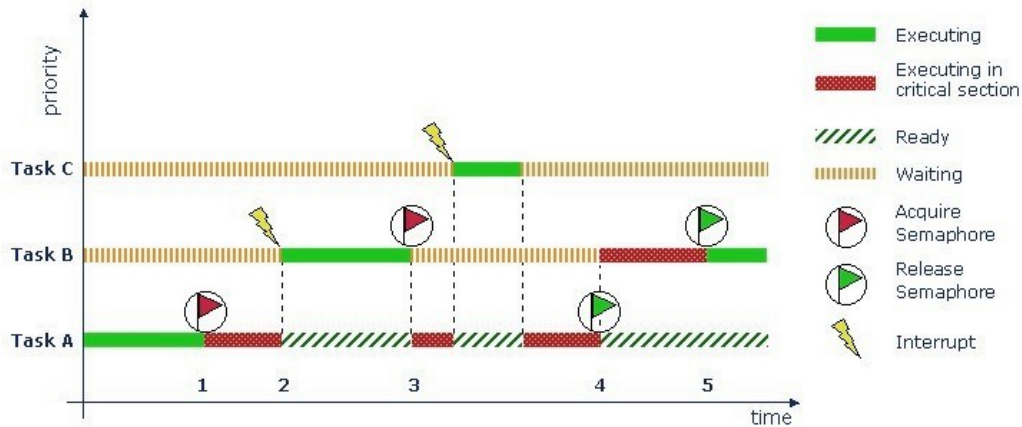
2.3.1. Mutual Exclusion

As discussed mutual exclusion does only allow one process or thread to access the shared resource at a time. This includes that if a process p_1 already accessed the shared resource x and is still working on it, a second process p_2 , which tries to access that shared resource x has to wait until the process p_1 finishes its task, where it needs that shared resource x . To achieve this mostly synchronisation techniques based on locks or semaphores are used to block the entry of an process to an already accessed and in use shared resource of an other process. See fig. 2.2 to gain an deeper understanding on how this works. This paper will not go into detail how traditional synchronisation techniques like locks or semaphores work, since for this work it is only important that these kind of methods manage the access of processes to shared resources in shared memorys via some kind of locks. A process will acquire a lock to access a shared resource and will release it when its task is done. Another process trying to access the same resource while its in use has to wait until the lock is released for that resource.

It is clear that this approach inherently relies on blocking a set of processes. This may lead to several issues, including deadlocks, process starvation, priority inversion, and increased response times. The sequence which process might acquire the lock first to enter the critical section, when multiple processes wait for the access is mostly set by a scheduler. Since wait-free methods explained later in section 2.5 are lock-free, a scheduler is not needed and as a result of that scheduling will not be explained more in detail in this work. [2], [19]

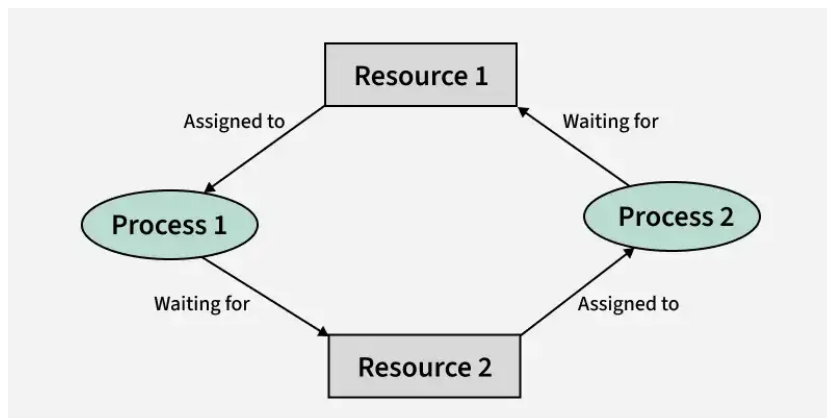
2. Background

Figure 2.2.: Mutual exclusion between three tasks(processes), which access the same critical section. Multiple processes need to stop working and just wait for other processes to finish their work. See the waiting phase of the processes.



[18]

Figure 2.3.: Deadlock between two processes, which wait for each other to release the needed resources.



[20]

Process Starvation

Another problem would be, what if when multiple processes try to enter the shared resource one after the other and one process keeps getting outperformed in acquiring a lock to enter the critical section. This process would wait for an indefinite time and will never enter the shared resource. A process that will never access a shared resource that it tries to enter starves out. This usually happens when a synchronization method allows one or more processes to make progress while ignoring a particular process or processes. This mostly happens in environments where some sort of process prioritization exists and processes are classified into low and high priority processes. When there are always high priority processes available and

2. Background

some low priority processes, it might happen that these low priority processes will never be able to enter the critical section. This is a problem, since these low priority processes might be important for the system too. [21]

Deadlock

Even worse, what if two or more processes already accessed a resource and now each of them wait that the other process releases the lock for the resource each of them aquired? This results in a situation seen in fig. 2.3 where these processes now indefinetlywait for each other and never terminate. So the resources that these waiting processes hold are also never released and are also never available to other processes maybe needed by other systems. As one can see, this a system into a state which would make no progress any further and would also not respond to any command anymore. [20], [22]

For instance a driverless car with a brake-by-wire system, where processes responsible for braking are in a deadlock, could eventually not brake if needed and a fatal car crash would happen.

Priority Inversion

Now lets say no process starvations or deadlocks happen. What could happen too is that a lower priority process already accessed a shared resource and after that a higher priority process needs to access that specific resource too. If the lower priority process now gets delayed, the higher priority process gets delayed too. This would be called priority inversion now; a low priority process delaying an high priority process. [23]

Increased Response Times

As demonstrated traditional synchronization is based on mutual exclusion via blocking processes. The result is processes that are waiting, which leads to increased response times of a system. This results in not meeting the timing constraints of a HRTS environment.

2.4. Lock-Free Synchronization

Therefore synchronization techniques are required that do not block processes with any kind of locking mechanism. One way could be the implementation of lock-free syschronization techniques. This would allow multiple processes to access the shared resource concurrently. Lock-free synchronization ensures that at least one process will make progress in a finite number of steps. However some processes may be unable to proceed, because lock-free synchronization does not guarantee that all processes will complete their operations in a finite number of steps. This means that starvation or even priority inversion is still possible, as some processes, even high priority processes may be indefinitely delayed by others. There are different kind of mechanisms to achieve this. One way to accomplish lock-freedom for

2. Background

example is the lock-free technique introduced by Michael and Scott, which is also the basis for some other wait-free algorithms.

2.4.1. Michael and Scott's Lock-Free Queue

Michael and Scott developed an algorithm seen in algorithm 1 using a linked-list as a shared data structure with an enqueue and a dequeue function to introduce lock-freedom. A linked-list is a list containing nodes containing data and a pointer called next which references the next node in the list, which can only be traversed in a single direction. There is also a pointer called head, which references the beginning node of the list and a pointer called tail, which references the end node of the list. The core concept of the algorithm is the enqueue and dequeue functions beginning at line 7 and 26 in algorithm 1, which are used to add and remove nodes to the shared data structure. When a process tries to add a node to the list, it first creates a new node and sets its next pointer to NULL, see line 8 to 10 of the enqueue function. Beginning from line 11 to line 23 following happens: The process first checks if the pointer referencing to the next node after the tail node is NULL, see line 15. If it is null it tries to link the new node to the end of the list by using a Compare and Swap (CAS) seen in line 16. This operation atomically compares the current value of the tail pointer with the expected value and, if they match, updates the tail pointer to point to the new node. The tail itself would be updated in line 24. [24]

So let's say 2 processes p1 and p2 until line 16 executes one after the other. What could happen now is that if p1 executes line 16 before p2, p2 will fail the CAS from line 16. Now if p1 would not execute further thus not finalizing the enqueue with line 24 and p2 retries the loop until line 15, the condition in line 15 would not be TRUE anymore for p1 and p1 would execute line 19 and 20 to help p2 to finalize its enqueue so other processes can work further with this algorithm. [24]

The dequeue function works analogously, but instead of adding a node to the end of the list it removes a node from the front of the list. And since another process which could not finish its enqueue would cause confusion for other processes in the dequeue function, the process which could not finish its enqueue will also be helped in the dequeue function. [24]

Initialization starts at line 1 in algorithm 1, which is just used to create dummy nodes when there's no node in the list. This just simplifies the algorithm so that the head and tail pointers are not null. It can be observed that this approach does not need any locks explained in section 2.3. Still this approach has one major problem. If for instance process p1 is trying to enqueue, it can happen that the CAS loop might fail indefinitely if for an indefinite time other processes are always executing line 16 immediately before p1 could execute line 16. This means that in very high contention scenarios, a process may be delayed indefinitely and starve out. In a HRTS this could lead to violating timing constraints, since the process would not finish his task in the defined timing window, which is unacceptable. This is why a slightly different approach which guarantees that every process will complete its operation in a finite number of steps is in need. [24]

2. Background

Algorithm 1 Michael and Scott's Lock-Free Queue

```

1: function INITIALIZE(Q : pointer to queue_t)
2:   node = new node()                                ▷ Allocate a dummy node
3:   node.next.ptr = NULL                               ▷ Make it the only node in the list
4:   Q.Head = node                                     ▷ Both Head and Tail point
5:   Q.Tail = node                                     ▷ to this dummy node
6: end function
7: function ENQUEUE(Q : pointer to queue_t, value : data_type)
8:   node = new node()                                ▷ Allocate a new node from the free list
9:   node.value = value                                ▷ Copy enqueue value into node
10:  node.next.ptr = NULL                               ▷ Set next pointer of node to NULL
11:  loop                                                ▷ Keep trying until Enqueue is done
12:    tail = Q.Tail                                    ▷ Read Tail (pointer + count) together
13:    next = tail.ptr.next                             ▷ Read next ptr + count together
14:    if tail == Q.Tail then                             ▷ Are tail & next consistent?
15:      if next.ptr == NULL then                             ▷ Tail is the last node?
16:        if CAS(&tail.ptr.next, next, (node, next.count + 1)) then
17:          break                                          ▷ Link the new node; Enqueue is done
18:        end if
19:      else                                              ▷ Tail not pointing to the last node
20:        CAS(&Q.Tail, tail, (next.ptr, tail.count + 1))  ▷ Move Tail forward (helping another enqueueer)
21:      end if
22:    end if
23:  end loop
24:  CAS(&Q.Tail, tail, (node, tail.count + 1))           ▷ Final attempt to swing Tail to the inserted node
25: end function
26: function DEQUEUE(Q : pointer to queue_t, pvalue : pointer to data_type)
27:  loop                                                ▷ Keep trying until Dequeue is done
28:    head = Q.Head
29:    tail = Q.Tail
30:    next = head.ptr.next                               ▷ Read head->next
31:    if head == Q.Head then                               ▷ Still consistent?
32:      if head.ptr == tail.ptr then                       ▷ Empty or Tail behind?
33:        if next.ptr == NULL then                           ▷ Queue is empty
34:          return FALSE
35:        else                                              ▷ Tail is behind, help move it
36:          CAS(&Q.Tail, tail, (next.ptr, tail.count + 1))
37:        end if
38:      else                                              ▷ No need to adjust Tail
39:        *pvalue = next.ptr.value                          ▷ Read value before CAS
40:        if CAS(&Q.Head, head, (next.ptr, head.count + 1)) then
41:          break                                          ▷ Dequeue is done
42:        end if
43:      end if
44:    end if
45:  end loop
46:  free(head.ptr)                                       ▷ Safe to free old dummy node
47:  return TRUE
48: end function

```

[24]

While Michael and Scott's algorithm relies on the CAS primitive, other atomic primitives provide alternative approaches that other algorithms shown later in this thesis use. A overview on the atomic primitives that are used in this thesis context is given in the following section.

2.4.2. Atomic Primitives

Atomic primitives are hardware instructions that conduct a set of steps atomically, meaning with no interruption from other processes [25]. This will be important in the algorithms analyzed later in this thesis, since these primitives are used to implement wait-free synchronization. There are different kind of atomic primitives:

Load-Linked and Store-Conditional (LL/SC)

Abbreviation of the instructions Load-Linked (LL) and Store-Conditional (SC), which is an operation available on ARM, MIPS and Alpha architectures usually implied with a Validate-Link (VL) instruction.

- LL(R) returns value of register r
- “SC(R, v) changes the value in register R to v and returns true, if and only if no other process performed a successful SC since the most recent call of LL of the current process. So SC fails if the value of the register has changed since it has been read” [26]
- “VL(R) returns true if no other process performed a successful SC on register R, which allows to test a register value without changing it” [26]

[26]

Compare and Swap (CAS)

It is already explained how CAS works in section 2.4.1. Furthermore to the explanation in section 2.4.1 CAS is an atomic primitive that is supported on “intel x386, x64 and most general purpose architectures with operands that are restricted to pointer size” [26].

- “CAS(R,e,n) returns true and sets the value of R to n if the value in R is e. Otherwise, it returns false.” [26]

The problem with CAS furthermore than the issue explained earlier in section 2.4.1 is that it can lead to the ABA problem, which can also occur in wait-free algorithms:

- Process 1 reads value A from a shared variable.
- Process 2 changes the value to B and then back to A.
- Process 1’s CAS operation succeeds, because it compares the value A it read earlier with the current value A, even though the value was changed in between.

This is a fundamental limitation of CAS. One solution would be to replace CAS with LL/SC, but that is not possible on x86 processors. So other solutions are needed that are discussed in chapter 6. [26]

2. Background

Swap

Swap is an atomic read-modify-write operation that unconditionally exchanges a value in memory with a new value and returns the old value. $\text{Swap}(R, v)$ atomically stores value v into location R and returns the previous value that was in R . This operation always succeeds. [27].

Fetch and Add (FAA)

This primitive is used to increment “the value of a variable by a given offset and [return] the result. This instruction always succeeds.” [26]

Fetch and Store (FAS)

This atomically stores a value into a variable and returns the previous value. This is similar to CAS, but it does not require a comparison and a retry loop. This is faster than CAS, if conditions before updating do not need to be checked. [28]

2.5. Wait-Free Synchronization

Lock-freedom solves the problem of a system getting into a deadlock. But this is not enough, in a fully automated car for example it is undesirable that any process does not complete its task, since that could mean that some processes that are responsible for braking would not finish their work in a worst case scenario. And such an occasion where the car would need to brake a fatal car crash would be the outcome. Consequently a solution is necessary where every process finishes their task in a finite number of steps instead of just one process. So something is needed which builds upon such mechanisms and expands them. This is exactly what wait-free synchronization is. It guarantees that every process will complete its operation in a finite number of steps, regardless of contention. This means that even process starvation is by definition not possible anymore. So by definition starvation cannot happen anymore. Also priority inversion is eliminated too, because processes do not have to wait for other processes anymore. This ensures system responsiveness and predictability thus the ability to define strict timing constraints to meet these vital timing constraints, which are essential for HRTS applications. But even wait-free algorithms introduce one problem. Wait-free algorithms are in most cases slower than their lock-free counterpart in execution. A solution to this problem was the fast-path / slow path method by Kogan and Petrunkin, where operations on a data structure are first done with a bounded lock-free operation, and when failed a slower wait-free operation will substitute the failed lock-free operation [4]. This will be analysed more in detail in chapter 5.

2.6. Rust Programming Language

The question now is which programming language suits best for this kind of research. Since a fast communication between the processes is compulsory to meet all HRTS timing constraints, the C programming language would be a good choice. C provides low-hardware control and therefore also allows the implementation of fast low-latency communication. What is also important and necessary for a RTS is, that C does not have an automatic garbage collector, which gets active and stops all processes from working to clean up allocated but no longer used memory space. Because of that all Real-Time Operating System (RTOS) are written in C. The main problem with C is that it does not provide any kind of memory safety, since C implements memory operations that are prone to buffer overflows or control-flow attacks. In the industry around 70% of vulnerabilities happen because of memory safety issues. If the real-time application would run on an isolated system with no internet connection, this would not be a problem. But in modern automation, where systems need to be connected to the internet for data exchange, such systems would be prone to security attacks. RTS nowadays is an integral part in various connected devices, including critical fields such as health or transportation. Conclusively it is extremely important that the security of such devices is guaranteed. With the rust programming language the problems of memory safety features are gone. The difference to C is that it can be as fast as C with the possibility to support low-level control and high-level programming features, while providing memory safety features in a real-time setting. The memory safety aspect is achieved by an ownership concept that controls how memory is handled in programs. This is strictly checked and therefore the executable program has guaranteed memory safety. In the model every value has a single owner represented by a variable. The owner is in charge of the lifetime and deallocation of that value. Rust will automatically free the memory associated with that value, when the owner goes out of scope. This behaviour is automatically done by using the memory reference feature provided by rust. Creating such references is also called borrowing. This allows the usage of these values without transferring the ownership. These references have its own lifetime, which can be explicitly defined by the programmer or implicitly inferred by rusts compiler. This ensures that the references are valid and do not exist longer as needed. Hence this also can play a role in lock-freedom, which is needed for wait-free synchronization, since shared resources can be shared with this ownership concept. Additionally rust is a type-safe language, which can be helpfull during implementation to avoid bugs and errors, since this also needs to be avoided in a RTS. As seen rust is a good choice for implementing wait-free synchronization mechanisms for IPC in RTS. [9], [29].

Further mechanisms on how with rust different kind of common memory safety issues are solved will not be discussed in detail, as that would go beyond the scope of this thesis. It is only important to know the basics on how rust is a type-safe and memory-safe programming language, to understand why rust is used for this work.

3. Related Work

The early foundations regarding wait-freedom was done indirectly by Leslie Lamport in 1977 and 1983 [30], [31]. While these works did not directly address or formally define wait-freedom, they laid the groundwork for lock-freedom, which Maurice Herlihy later extended to wait-freedom [1].

In 1977, Lamport he showed how one writer and multiple readers can share data without the need of locks, eliminating writer delays due to reader interference. It works by using atomic byte-wise read and write operations. The writer will atomically write a value to a memory location from right to left, while the reader uses the same memory location to read the value from left to right. So even if the writer is still in the process of writing, the reader will not block the writer while reading (and vice versa) and still see a correct snapshot of the data. To prevent a reader process from saving inconsistent data (for example while the writer process writes), the writer process will tag each update by incrementing a start counter before an end counter after writing. Readers take the start counter, read the data, and compare if the start counter matches the end counter. If they do not match it means the data is inconsistent and the reader will retry reading the data until it gets a consistent value. To understand this better imagine a date with the format DD/MM/YYYY, where every digit is written as one byte from right to left and read from left to write. This solves the problem of contention between readers and a single writer. If multiple writers are involved, the writers still have to be mutually exclusive, which means that they have to use locks to block each other to prevent inconsistency (So with multiple writers this algorithm cannot be lock-free anymore). [30]

In 1983 Leslie Lamport then gave a formal method to write and prove the correctness of any concurrent module in a simple and modular way independent of the used data structure, which he refers to as modules. These modules consist of three components:

- state functions, which are abstract variables describing the module's state.
- initial conditions, which are predicates on the state functions.
- properties, which are a mix of safety and liveness requirements.

Safety requirements define what must never happen (e.g., a queue must never drop an element), while liveness requirements define what must eventually happen (e.g., a non-empty queue must eventually allow dequeuing). He also defines the usage of action sets and environment constraints, which separate the module action from the environments (e.g., the program where the data structure runs in). For example, a First In First Out (FIFO) queue specification would include:

3. Related Work

- State Functions: queue contents, operation parameters, return values.
- Initial Conditions: queue starts empty.
- Safety Condition: queue maintains FIFO ordering.
- Liveness Condition: dequeue operation will eventually return a value.

This systematic methodology to prove the correctness of concurrent data structures laid the necessary groundwork for later developments too. [31]

Building on methodologies to prove concurrent data structure correctness Herlihy and Wing provided linearizability as a correctness condition for concurrent objects, which is a guarantee that every operation performed appears to take effect instantaneously at some point between the call and return of the operation [32]. This correctness condition was then used to formalize wait-freedom in 1991 [1]. In the latter work Herlihy proved that any sequential data structure can be transformed into a wait-free concurrent data structure [1]. A wait-free data structure must satisfy following three constraints:

- Linearizability: operations take effect instantaneously at some point between the call and return of the operation.
- Bounded steps: operations end in a finite number of steps.
- Independence: operations finish regardless of other processes' execution (for later understanding: a process waiting for another process for a maximum number of time and then returning an error if that time is exceeded would still be considered wait-free, since it will finish regardless of the other process).

From this perspective the algorithm provided by Lamport in 1977 is already wait-free, even though the term was not yet defined at that time. [1], [32]

Herlihy's universal construction and principles (or work that builds upon his work) appear conceptually throughout all of these wait-free algorithms [4], [27], [28], [33]–[49]. [1]

Kogan and Petrunkin later invented a method called fast-path slow-path, where first usually a lock-free method (the fast-path) is used to try to complete an operation, since lock-free algorithms are usually faster than wait-free algorithms. These lock-free paths are bounded by a maximum number of steps and if the operation does not complete within that bound the algorithm tries to complete the operation using a wait-free method (the slow-path). So in cases where the fast-path succeeds often without switching to the slow path, the algorithm in general completes in a shorter time than a pure wait-free algorithm. This method is used by two algorithms with one of them having a great performance advantage, which will be demonstrated later in this thesis [38], [40]. [4]

4. Methodology

To achieve the goal that is defined in section 1.2, first all wait-free data structures that could be used for IPC through shared memory in HRTS need to be found. To do this a method was used that is more known from mapping studys or literature reviews. Multiple python scripts were implemented to do this [50]. A web scraper script was written to scrape over google scholar with the following queries:

- “wait-free queue”
- “wait-free” (“mpmc” OR “multi-producer multi-consumer” OR “multi-writer multi-reader” OR “many-to-many”) “queue”
- “wait-free” (“mpsc” OR “multi-producer single-consumer” OR “single-writer multi-reader” OR “many-to-one”) “queue”
- “wait-free” (“spsc” OR “single-producer single-consumer” OR “single-writer single-reader” OR “one-to-one”) “queue”
- “wait-free” (“sPMC” OR “single-producer multi-consumer” OR “multi-writer single-reader” OR “one-to-many”) “queue”

In google scholar a whitespace is considered as an AND. The rest is interpreted as read. With this approach i got a list of 1324 papers. The papers were then written into a csv file split into query, rank (number of paper), title, year, authors, venue, citations, abstract snippet, full_abstract and url with “;” as an delimiter. To extract all of this the information in google scholar was extracted and then for the full abstract the scraper went onto the source url and extracted the abstract there. If the url was a direct pdf link, a pdf reader was used to find the abstract. If an abstract was not extractable (some source site which was not considered or other problems), “ABSTRACT_NOT_FOUND” was written instead or if the paper was accessible the full paper was written instead into that cell. Because a lot of scientific web pages will put ceptchas if continuously requests are made undetected_chromedriver was importet and used as the web driver. It is an enhanced version of chromedriver which bypasses anti bot detections. After that I also implemented a regex analyzer to analyze the abstracts of the found papers on the words “lockfree”, “waitfree”, and “obstructionfree” and also again without a hyphon inbetween these words. If these keywords were not found in the abstract or the abstract contained the flag “ABSTRACT_NOT_FOUND” the paper was removed from the csv. This left 475 papers that contained at least one of these words in their abstract. After that the duplicates were removed by the algorithm, which left 325 papers. The duplicates were

4. Methodology

removed by checking the url of the paper. Now what was left had to be manually analyzed to see if the paper was relevant for the topic. Since libre office and microsoft excel has a limit of 32.767 charachters per cell a abstract splitter had to be build to split the abstract into multiple cells. Analyzing was done by reading the paper and checking if the paper was developing an wait-free fifo queue. While dooing that also backward and forward search was done to even find more papers. Papers where only included, if and only if:

- All three of Herlihys constraints were met, that we listed in chapter 3.
- The algorithms could be implemented on x86 architecture using rust, since this is the architecture and programming language that is used in the implementation of this thesis. The reason x86 is used, is because that is the architecture available and it is also the architecture that is used in most modern computers. For example Khanchandani and Wattenhofer [51] created a queue using theoretical atomic primitives called half-increment and half-max. These primitives do not exist on real hardware. The same goes for Bédin et al. [52] who created a queue using theoretical atomic primitives called memory-to-memory.
- The algorithm runs in an acceptable time complexity to even benchmark it. For example the algorithm by Johnen et al. [53] and Naderibeni and Ruppert [54] were running so slow that they were not been considered to be benchmarked, since they take too long to run and wait for results. Both use a really complex to implement tree structure that is creating an extreme overhead for just producing and consuming items.

In the end 17 papers were included from the 325 papers and 3 more paper were included by backward and forward search of the papers that were included. The papers were then split into 4 contention categories:

- MPMC queues [33], [35], [37], [39], [40]
- MPSC queues [28], [41], [43], [44]
- SPMC queues [27]
- SPSC queues [31], [45], [47]–[49]

Now the wait-free fifo queues had to be compared performance wise. Some papers were just improvements of other papers so only the improved version was used for the comparison. Some other papers showed multiple ways of implementing a wait-free fifo datastructure. In the end 5 MPMC queues, 4 MPSC queues, 1 SPMC queue and 11 SPSC queues were included into this work.

5. Analyzing existing Wait-Free Data Structures and Algorithms

5.1. Optimal Wait-Free Data Structure

An important question is what data structure to use for the implementation of a wait-free synchronisation technique for IPC. M. Herlihy showed that every sequential data structure can be made wait-free [1]. So it is important to choose the optimal data structure for our use. Considering that the reason of this work is to optimize modern manufacturing and automation, some form of correct data flow order is as well necessary for correct work flow for instance in an modern manufacturing line or more critical in a driverless car. Hence an already natural fit like FIFO queues. Natural because in such queues a producer process can enqueue messages and the consumer process can dequeue messages sequentially. This models real-world data flows (sensor readings, commands, network packets), which are inherently sequential. Consequently with such queues the order of the data flow is preversed without the need of implementing additional functionalities. In contrast, data structures like stacks, sets, or maps do not maintain this kind of arrival order and moreover add semantics like Last In First Out (LIFO) order or key-value pairs, which are in most cases not desired or even unnecessary. This would bring in the need of additional functions to just get rid of undesired side effects. Furthermore in a queue only two operations exist, an enqueue and an dequeue operation. All the other data structures introduce more operations and therefore more complexity and therefore more performance overhead. The less operations exist, the less complex the implementation will be. Because of these advantages and also because of the fact that in most publications in the wait-free domain queues are beeing used, limiting this thesis to queues only is reasonable. [43]

5.2. Wait-Free Algorithms

With the appropriate data structure established, an important consideration is the selection of suitable algorithms. In chapter 4 4 different contention categories are defined. Which kind of algorithm going to be used will be decided contention based. Since all of them have different complexity in runtime, it is important to choose the right contention category for the right use case to save resources and have faster execution times to meet the timing constraints of HRTS. In modern manufacturing and automation devices are used which can run multiple applications on a single device. This could mean that every application running on one device could be a producer and a consumer to each other (MPMC) and also maybe some single application of all applications running on one device produces data for just a single other

5. Analyzing existing Wait-Free Data Structures and Algorithms

consuming application (SPSC). And maybe some single application is a producer for multiple consuming applications (SPMC) and multiple applications are producers of a single consuming application (MPSC). So it can be that all cases can occur in just one device. This means that all the different cases of contention have to be considered. In the following the different cases and their algorithms will be discussed. Moreover they will be implemented and their performance tested via a benchmarked (how fast an algorithm can produce and consume items concurrently). Subsequently from each category the best algorithm will be chosen and their performance will be compared with each other to identify, if 4 different categories are necessary. The reason for that is, that for instance the best performed MPMC algorithm could outperform all other algorithms even for their contention category, since a MPMC approach can cover all contention cases. The goal with this approach is to have as little overhead as possible, since an algorithm explicitly implemented for a MPMC use case could have extreme overhead for a SPSC case. The implementation will be discussed in chapter 6 and the results of the performance readings will be discussed in chapter 7. The following subsections will give an overview of the different contention categories and their algorithms found. The subsections will also shortly describe how the enqueue and dequeue in these algorithms work. Given that all algorithms found are about inter-thread communication and not IPC, the following explanation of the specific algorithms will include the terminology of threads to be precise about the papers. In chapter 6 it will be elaborated how these thread based algorithms are adapted to IPC in Rust. Other minor Rust-specific deviations from the following algorithms (different types required by Rust's safety model, additional memory fences, etc.) can be seen in the GitHub repository accompanying this thesis [50]. These are not detailed here as such explanations would provide limited value to the topic of this work, and while a comprehensive analysis would be relevant, it would require more extensive exploration than is feasible within the scope of this work.

5.2.1. Single Producer Single Consumer (SPSC)

This is the most simple form of IPC. In SPSC there is nearly no contention from other processes, because only one producer and one consumer is working. The only contention is between the consumer and producer. This leads to the producer and consumer finish in a bounded number of steps without special synchronisation techniques like helping or atomic primitives. The only concern is that the data the consumer reads is consistent. Different approaches were tested in different papers, that will be seen here. Since Batched Lamport Queue (BLQ), Lazy Lamport Queue (LLQ), Batched Improved FastForward Queue (BIFFQ) and Improved FastForward Queue (IFFQ) are from the same paper, explanations and variables are shared between these algorithms to avoid redundancy:

Lamport's Circular Buffer Queue

Uses a circular array with two shared indices for synchronization, based on the algorithm originally proposed by Leslie Lamport in 1983 [31] and shown here in algorithm 2 following

5. Analyzing existing Wait-Free Data Structures and Algorithms

Maffione et al.'s version [48]. The producer first checks if the queue is full (reached capacity N) in line 2, which requires reading the consumer's `read` index. If the queue is not full, it writes the input data to the slot at position `write & mask` in line 5, where the bitwise AND operation wraps the index around when it reaches the array end. The producer then increments `write` to signal that the written data is available in line 7. The consumer mirrors this behavior by checking if the queue is empty in line 12, which requires reading the producer's `write` index. If the queue is not empty, the consumer reads data from the slot at position `read & mask` in line 16, using the same modulo arithmetic through bitwise AND, and incrementing its `read` index to signal that the slot is available in line 17. This wraparound behavior creates the circular buffer structure, allowing the fixed-size array to be reused continuously. Unfortunately each operation requires accessing both shared indices plus the data slot, causing up to three cache misses per item when the queue moves between nearly empty and nearly full states. According to Drepper, cache misses occur when requested data is not in the local CPU core's cache and must be fetched from another core's cache, with the cache coherence protocol ensuring memory consistency across all cores [55]. Drepper showed that performance can degrade by 390%, 734%, and 1,147% for 2, 3, and 4 threads respectively. This happens because cache lines, the 64-byte blocks (on x86 architectures) that move between CPU caches, ping-pong between the producer's and consumer's cores as they take turns accessing the same memory locations [55].

Algorithm 2 Lamports Queue [48]

```

1: function LQ_ENQUEUE( $q, e$ )
2:   if  $q.write - q.read = N$  then                                     ▷ Check if full
3:     return -1                                                       ▷ No space
4:   end if
5:    $q.slots[q.write \wedge q.mask] \leftarrow e$ 
6:   store_release_barrier()
7:    $q.write \leftarrow q.write + 1$ 
8:   return 0
9: end function
10:
11: function LQ_DEQUEUE( $q$ )
12:   if  $q.read = q.write$  then                                         ▷ Check if empty
13:     return NULL_ELEM                                               ▷ Queue empty
14:   end if
15:   load_acquire_barrier()
16:    $e \leftarrow q.slots[q.read \wedge q.mask]$ 
17:    $q.read \leftarrow q.read + 1$ 
18:   return  $e$ 
19: end function

```

[48]

Lazy Lamport Queue

Reduces the described cache misses by postponing index reads until necessary, as shown in algorithm 3. Additionally to Lamports original enqueue function the producer maintains a local `read_shadow` copy and only updates it when running out of known free slots in lines

5. Analyzing existing Wait-Free Data Structures and Algorithms

2 - 6. Similarly, the consumer uses `write_shadow` to avoid repeatedly checking for new items. Additionally, LLQ keeps K slots (where K is slots per cache line) permanently empty, preventing producer and consumer from touching the same cache line when the queue is full. This works well when one thread is faster than the other, reducing worst-case misses from 3 to about 2 per item. [48]

Algorithm 3 Lazy Lamport Queue Operations [48]

```

1: function LLQ_ENQUEUE( $q, e$ )
2:   if  $q.write - q.read\_shadow = N - K$  then                                ▷ Lazy load check
3:      $q.read\_shadow \leftarrow q.read$                                        ▷ Update shadow
4:     if  $q.write - q.read\_shadow = N - K$  then
5:       return -1                                                         ▷ No space
6:     end if
7:   end if
8:    $q.slots[q.write \wedge q.mask] \leftarrow e$ 
9:   store_release_barrier()
10:   $q.write \leftarrow q.write + 1$ 
11:  return 0
12: end function
13:
14: function LLQ_DEQUEUE( $q$ )
15:   if  $q.read = q.write\_shadow$  then                                       ▷ Lazy load check
16:      $q.write\_shadow \leftarrow q.write$                                    ▷ Update shadow
17:     if  $q.read = q.write\_shadow$  then
18:       return NULL_ELEM
19:     end if
20:   end if
21:   load_acquire_barrier()
22:    $e \leftarrow q.slots[q.read \wedge q.mask]$ 
23:    $q.read \leftarrow q.read + 1$ 
24:   return  $e$ 
25: end function

```

Batched Lamport Queue

Extends LLQ with explicit batching to further reduce synchronization costs, as detailed in algorithm 4. The producer accumulates items using private `write_priv` in line 11, filling slots without updating the shared `write` index. Only the function `blq_enqueue_publish` in lines 15 - 18 makes the batch visible by advancing `write` in line 17. The consumer works symmetrically, using `read_priv` in line 32 for local progress before updating `read` in line 40. With typical batch sizes like $B = 32$, synchronization overhead is amortized across operations, reducing cache misses. However, the application using this queue design must explicitly call the publish functions even with partial batches to avoid unbounded latency, because items remain invisible to the consumer until published. This design particularly benefits applications that naturally process data in batches, such as network packet processing, where batch boundaries are well-defined. [48]

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 4 Batched Lamport Queue Operations [48]

```

1: function BLQ_ENQUEUE_SPACE( $q$ ,  $needed$ )
2:    $space \leftarrow N - K - (q.write\_priv - q.read\_shadow)$ 
3:   if  $space < needed$  then
4:      $q.read\_shadow \leftarrow q.read$  ▷ Update shadow
5:      $space \leftarrow N - K - (q.write\_priv - q.read\_shadow)$ 
6:   end if
7:   return  $space$ 
8: end function
9:
10: function BLQ_ENQUEUE_LOCAL( $q$ ,  $e$ )
11:    $q.slots[q.write\_priv \wedge q.mask] \leftarrow e$ 
12:    $q.write\_priv \leftarrow q.write\_priv + 1$ 
13: end function
14:
15: function BLQ_ENQUEUE_PUBLISH( $q$ )
16:    $store\_release\_barrier()$ 
17:    $q.write \leftarrow q.write\_priv$ 
18: end function
19:
20: function BLQ_DEQUEUE_SPACE( $q$ )
21:    $available \leftarrow q.write\_shadow - q.read\_priv$ 
22:   if  $available = 0$  then
23:      $q.write\_shadow \leftarrow q.write$  ▷ Update shadow
24:      $available \leftarrow q.write\_shadow - q.read\_priv$ 
25:   end if
26:   return  $available$ 
27: end function
28:
29: function BLQ_DEQUEUE_LOCAL( $q$ )
30:    $load\_acquire\_barrier()$ 
31:    $e \leftarrow q.slots[q.read\_priv \wedge q.mask]$ 
32:    $q.read\_priv \leftarrow q.read\_priv + 1$ 
33:   return  $e$ 
34: end function
35:
36: function BLQ_DEQUEUE_PUBLISH( $q$ )
37:    $q.read \leftarrow q.read\_priv$ 
38: end function

```

FastForward Queue

Synchronization by embedding control information directly within the data slots, eliminating separate shared indices shown in algorithm 5. Unlike Lamport's queue which requires checking both `head` and `tail` indices, FFQs producer simply examines if the next slot contains `NULL` in line 2 before writing. When the slot is empty (`NULL`), the producer writes the data directly and advances its private `head` index in lines 5 and 6. The consumer follows a similar pattern by reading from the current slot position in line 11 and then checks in line 12 data is present (non-`NULL`). If not `NULL` it retrieves the value and writes `NULL` to mark the slot empty in line 15. Then it advances its private `tail` index in the line after that. This couples synchronization control and the actual data, reducing shared memory accesses from three (`head`, `tail`, `buffer`) to just one (`buffer` slot). Each thread maintains its own private index that never needs synchronization. The producer tracks where to write next through `head`, while the

5. Analyzing existing Wait-Free Data Structures and Algorithms

consumer tracks where to read next through `tail`. The `NULL` value serves dual purpose as both an empty indicator and the synchronization mechanism. While this approach reduces memory barriers and cache misses significantly, it still has the ping-pong effect when the queue has few elements, causing the producer and consumer to operate on the same cache line. [49]

Algorithm 5 FastForward Queue Operations [49]

```
1: function FFQ_ENQUEUE( $q, data$ )
2:   if  $q.buffer[q.head] \neq \text{NULL}$  then
3:     return EWOULDBLOCK
4:   end if
5:    $q.buffer[q.head] \leftarrow data$ 
6:    $q.head \leftarrow \text{NEXT}(q.head)$ 
7:   return 0
8: end function
9:
10: function FFQ_DEQUEUE( $q$ )
11:    $data \leftarrow q.buffer[q.tail]$ 
12:   if  $data = \text{NULL}$  then
13:     return EWOULDBLOCK
14:   end if
15:    $q.buffer[q.tail] \leftarrow \text{NULL}$ 
16:    $q.tail \leftarrow \text{NEXT}(q.tail)$ 
17:   return  $data$ 
18: end function
```

Improved FastForward Queue

Prevents cache conflicts through spatial separation using a look-ahead mechanism shown in algorithm 6. The producer checks if a slot H positions ahead (4 cache lines ahead) is empty before proceeding in line 4, ensuring it works far ahead of the consumer. This check happens only once every H items when `write` reaches `limit` in line 2. The consumer delays clearing slots through the function `iffq_dequeue_publish` seen in lines 23 - 28, maintaining separation between producer and consumer regions. With $2H$ permanently unused slots as a buffer zone, producer and consumer operate on different cache lines, reducing cache misses even more. [48]

Batched Improved FastForward Queue

Addresses IFFQs weakness when the queue is nearly empty by adding producer-side buffering, as shown in algorithm 7. Items first accumulate in a thread-local buffer seen in line 10, then the function `biffq_enqueue_publish` beginning at line 15 writes them to the queue in a rapid burst in lines 15 - 18. Also like in BLQ the application using this queue must call this function explicitly to avoid deadlocks. This behavior creates an intended race condition, which is beneficial if all writes complete before the consumer notices. The cache line stays with the producer to avoid ping-pong effects. The consumer side remains unchanged from IFFQ. While theoretical worst-case behavior is similar to IFFQ, practical measurements show

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 6 Improved FastForward Queue Operations [48]

```

1: function IFFQ_ENQUEUE( $q, e$ )
2:   if  $q.write = q.limit$  then                                     ▷ Check limit
3:      $next\_limit \leftarrow q.limit + H$ 
4:     if  $q.slots[next\_limit \wedge q.mask] \neq NULL\_ELEM$  then
5:       return  $-1$                                                ▷ No space
6:     end if
7:      $q.limit \leftarrow next\_limit$                                ▷ Free partition
8:   end if
9:    $q.slots[q.write \wedge q.mask] \leftarrow e$ 
10:   $q.write \leftarrow q.write + 1$ 
11:  return  $0$ 
12: end function
13:
14: function IFFQ_DEQUEUE_LOCAL( $q$ )
15:   $e \leftarrow q.slots[q.read \wedge q.mask]$ 
16:  if  $e = NULL\_ELEM$  then
17:    return  $NULL\_ELEM$ 
18:  end if
19:   $q.read \leftarrow q.read + 1$ 
20:  return  $e$ 
21: end function
22:
23: function IFFQ_DEQUEUE_PUBLISH( $q$ )
24:  while  $q.clear \neq next\_clear(q.read)$  do
25:     $q.slots[q.clear \wedge q.mask] \leftarrow NULL\_ELEM$ 
26:     $q.clear \leftarrow q.clear + 1$ 
27:  end while
28: end function

```

significant improvement when the queue operates near empty, making BIFFQ effective across all operating conditions. [48]

Algorithm 7 Batched Improved FastForward Queue Operations [48]

```

1: function BIFFQ_WSPACE( $q, needed$ )
2:   $space \leftarrow q.limit - q.write$ 
3:  if  $space < needed$  then
4:    return  $space$                                                ▷ Force limit update
5:  end if
6:  return  $space$ 
7: end function
8:
9: function BIFFQ_ENQUEUE_LOCAL( $q, e$ )
10:   $q.buf[q.buffered] \leftarrow e$                                 ▷ Store in buffer
11:   $q.buffered \leftarrow q.buffered + 1$ 
12: end function
13:
14: function BIFFQ_ENQUEUE_PUBLISH( $q$ )
15:  for  $i \leftarrow 0$  to  $q.buffered - 1$  do
16:     $q.slots[q.write \wedge q.mask] \leftarrow q.buf[i]$              ▷ Fast burst
17:     $q.write \leftarrow q.write + 1$ 
18:  end for
19:   $q.buffered \leftarrow 0$ 
20:   $q.limit \leftarrow q.write + H$                                ▷ Update limit
21: end function

```

B-Queue

Addresses the deadlock issues inherent in batching approaches through a self-adaptive backtracking mechanism that dynamically adjusts to production rates shown in algorithm 8. The producer maintains local `head` and `batch_head` pointers, probing `BATCH_SIZE` positions ahead when needed in line 3. The consumer's adaptive backtracking algorithm from lines 27 - 41 maintains a `batch_history` variable that records successful batch sizes from previous operations. When searching for data, it starts from this historical value rather than always beginning at `BATCH_SIZE`, significantly reducing latency when the producer operates slowly. If in line 29 - 31 the recorded size is below `BATCH_MAX`, the algorithm optimistically increments `batch_size` by `INCREMENT` (typically one cache line) to probe for higher throughput when the producer accelerates. The binary search then proceeds from this adaptive starting point, halving the batch size until finding available data or reaching zero. In the dequeue function, the consumer uses this computed value to update `batch_tail` in line 15. This eliminates the need for manual parameter adjustment or manual calling of a publish function while maintaining cache line separation and preventing deadlocks. [47]

Dynamic Single Producer Single Consumer

A dynamically space allocating queue using a linked list with node caching to reduce memory allocation overhead, as shown in algorithm 9. Unlike bounded circular buffers like the Lamport Queue, dSPSC dynamically allocates nodes as needed, making it suitable for scenarios where queue size cannot be predetermined. The implementation maintains a dummy head node `head` to ensure producer and consumer always operate on different nodes to prevent cache line conflicts. The `SPSC_Buffer` (line 4, which is just a Lamport Queue) serves as a node cache to recycle deallocated nodes to minimize `malloc` or `free` calls. When pushing, the producer first checks the cache for a recycled node in line 8, falling back to `malloc` only when the cache is empty in line 11. After setting the data and next pointer, a memory barrier ensures correct ordering before linking the new node into the list in lines 20-22. The consumer checks for available data by testing if the dummy head points to a data node in line 28. Upon a successful pop, the consumer advances the head pointer so the data node becomes the new dummy and then attempts to cache the old dummy for reuse in lines 30-33. While node caching improves performance, reading and referencing the pointer so often causes memory accesses spread over multiple cache lines. As shown earlier this leads to cache misses. [45]

Unbounded Single Producer Single Consumer

An unbounded queue that links multiple Lamport Queues to combine the cache efficiency of Lamports circular buffer queues with unlimited capacity, as shown in algorithm 10. Unlike dSPSC which uses scattered linked list nodes, uSPSC maintains spatial locality by keeping data in contiguous circular buffers while only linking the buffers themselves. The implementation uses two pointers `buf_w` pointing to the producer's current write buffer and `buf_r` pointing to the consumer's current read buffer. When pushing, the producer checks if the current buffer

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 8 B-Queue with Self-Adaptive Backtracking[47]

```

1: function BQUEUE_ENQUEUE( $q, e$ )
2:   if  $q.head = q.batch\_head$  then                                ▷ No empty slots
3:     if  $q.buffer[(q.head + BATCH\_SIZE) \bmod q.size] \neq \text{NULL}$  then
4:       return -1                                                ▷ Queue full
5:     end if
6:      $q.batch\_head \leftarrow q.head + BATCH\_SIZE$ 
7:   end if
8:    $q.buffer[q.head \bmod q.size] \leftarrow e$ 
9:    $q.head \leftarrow q.head + 1$ 
10:  return 0
11: end function
12:
13: function BQUEUE_DEQUEUE( $q$ )
14:  if  $q.tail = q.batch\_tail$  then                                ▷ No filled slots
15:     $batch\_tail \leftarrow \text{ADAPTIVE\_BACKTRACK}(q)$ 
16:    if  $batch\_tail = -1$  then
17:      return NULL
18:    end if
19:     $q.batch\_tail \leftarrow batch\_tail$ 
20:  end if
21:   $e \leftarrow q.buffer[q.tail \bmod q.size]$ 
22:   $q.buffer[q.tail \bmod q.size] \leftarrow \text{NULL}$ 
23:   $q.tail \leftarrow q.tail + 1$ 
24:  return  $e$ 
25: end function
26:
27: function ADAPTIVE_BACKTRACK( $q$ )
28:   $batch\_size \leftarrow q.batch\_history$                                 ▷ Start from historical value
29:  if  $batch\_size < BATCH\_MAX$  then
30:     $batch\_size \leftarrow batch\_size + INCREMENT$                     ▷ Try larger batch
31:  end if
32:  while  $batch\_size > 0$  do
33:     $batch\_tail \leftarrow q.tail + batch\_size$ 
34:    if  $q.buffer[(batch\_tail - 1) \bmod q.size] \neq \text{NULL}$  then
35:       $q.batch\_history \leftarrow batch\_size$                         ▷ Remember successful size
36:      return  $batch\_tail$ 
37:    end if
38:     $batch\_size \leftarrow batch\_size / 2$                                 ▷ Binary search
39:  end while
40:  return -1
41: end function

```

is full in line 2, and if so, requests a new buffer from the pool via `next_w()` in line 3 before writing the data to `buf_w`. The consumer first checks if its current buffer is empty in line 10. If empty, it determines whether the queue is truly empty by comparing read and write buffer pointers in line 11. If they point to the same buffer, no more data exists. Otherwise, after rechecking emptiness to prevent race conditions in line 14, the consumer obtains the next buffer via `next_r()` and releases the empty buffer back to the pool for recycling in lines 15-17. This double-check prevents data loss when the producer writes to the current buffer between the initial emptiness check and the buffer comparison. By reusing entire buffers rather than individual nodes, uSPSC matches bounded SPSC queues cache behavior while providing unbounded capacity. [45]

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 9 Dynamic List-based SPSC Queue (dSPSC) Operations [45]

```

1: struct Node { void* data; Node* next; }
2: Node* head;                                ▷ Points to dummy node
3: Node* tail;                                ▷ Points to last data node
4: SPSC_Buffer cache;                          ▷ Bounded cache for node recycling
5:
6: function ALLOCNODE
7:   Node*  $n \leftarrow$  NULL
8:   if cache.pop(& $n$ ) then                    ▷ Try cache first
9:     return  $n$ 
10:  end if
11:   $n \leftarrow$  (Node*)malloc(sizeof(Node))
12:  return  $n$ 
13: end function
14:
15: function PUSH(void* data)
16:   Node*  $n \leftarrow$  allocnode()              ▷ Get node from cache or malloc
17:    $n \rightarrow$ data  $\leftarrow$  data
18:    $n \rightarrow$ next  $\leftarrow$  NULL
19:   WMB()                                       ▷ Write Memory Barrier
20:   tail->next  $\leftarrow$   $n$                      ▷ Link new node
21:   tail  $\leftarrow$   $n$                            ▷ Update tail pointer
22:   return true
23: end function
24:
25: function POP(void** data)
26:   if head->next  $\neq$  NULL then              ▷ Check if data available
27:     Node*  $n \leftarrow$  head                  ▷ Save current dummy
28:     *data  $\leftarrow$  (head->next)->data        ▷ Extract data
29:     head  $\leftarrow$  head->next                ▷ Advance to next node
30:     if !cache.push( $n$ ) then                ▷ Try to recycle old dummy
31:       free( $n$ )                             ▷ Free if cache full
32:     end if
33:     return true
34:   end if
35:   return false                             ▷ Queue empty
36: end function

```

MultiPush Single Producer Single Consumer

Reduces the ping-pong effect in Lamport's circular buffer by batching multiple elements before insertion, as shown in algorithm 11. Instead of writing elements one by one directly to the shared buffer, MultiPush Single Producer Single Consumer (mSPSC) accumulates items in a thread-local array `batch`. The producer stores incoming data in the batch array in lines 2 and 3, and when the batch reaches `BATCH_SIZE` in line 4, the producer calls `multipush` to insert all elements at once in line 5. The `multipush` function first calculates the final write position in line 11 and checks if sufficient space exists in line 12. As seen in lines 15 - 17 elements are written in reverse order, starting from the furthest position and working backwards. This backward insertion creates distance between the write pointer and where the consumer is reading, ensuring they operate on different cache lines. A write memory barrier in line 18 ensures all batch writes are visible before updating the write pointer in line 19. The batch counter resets in line 20, preparing for the next batch. The `flush` function in lines 24 -

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 10 Unbounded Single Producer Single Consumer Operations[45]

```

1: function USPSC_PUSH(q, data)
2:   if q.buf_w.full() then                                     ▷ Current buffer full
3:     q.buf_w ← q.pool.next_w()                               ▷ Get new buffer
4:   end if
5:   q.buf_w.push(data)
6:   return true
7: end function
8:
9: function USPSC_POP(q, data)
10:  if q.buf_r.empty() then
11:    if q.buf_r = q.buf_w then                                   ▷ Same buffer?
12:      return false                                             ▷ Queue truly empty
13:    end if
14:    if q.buf_r.empty() then                                     ▷ Recheck after comparison
15:      tmp ← q.pool.next_r()
16:      q.pool.release(q.buf_r)                                   ▷ Recycle buffer
17:      q.buf_r ← tmp
18:    end if
19:  end if
20:  return q.buf_r.pop(data)
21: end function

```

29 allows forcing partial batch writes when needed. While adding an extra copy per element from batch to buffer, the improved cache behavior from reduced traffic from the coherence protocol compensates for this overhead. [45]

Jayantis SPSC Queue

A queue specifically for composability in larger MPSC structures, as shown in algorithm 12. Unlike traditional SPSC queues, this implementation includes `readFront` operations that enables observation of the queue's head element, crucial for the MPSC construction. The queue maintains a linked list where the tail always points to a dummy node. When enqueueing, the producer converts the current dummy node into a data node by writing the value in line 4. Then the producer links a new dummy node in line 5 and updates the tail pointer in line 6. This ensures the consumer never sees a partially constructed node. The `Help` variable in line 15 stores the dequeued value, allowing concurrent `readFront_e` operations to obtain valid data even after the original node is removed. The announcement mechanism prevents use-after-free errors. When the producer calls `readFront_e`, it writes the front node pointer to `Announce` in line 32, signaling the consumer not to immediately free that node. If the consumer encounters an announced node in line 17, it defers the node's deallocation to `FreeLater` in lines 18-20, ensuring the producer can safely read the node's value. The separate `readFront_d` operation in lines 41-47 is simpler since the consumer knows no concurrent dequeue can occur. This coordination enables wait-free progress while supporting the propagation mechanism, the process of pushing each local queue's minimum timestamp up through a binary tree to maintain a global minimum, needed for the logarithmic-time MPSC operations as seen in section 5.2.2. [44]

Algorithm 11 MultiPush Single Producer Single Consumer Operations[45]

```

1: function MSPSC_PUSH( $q, data$ )
2:    $q.batch[q.count] \leftarrow data$ 
3:    $q.count \leftarrow q.count + 1$ 
4:   if  $q.count = BATCH\_SIZE$  then
5:     return MULTIPUSH( $q, q.batch, q.count$ )
6:   end if
7:   return true
8: end function
9:
10: function MULTIPUSH( $q, batch, len$ )
11:    $last \leftarrow q.write + len - 1$  ▷ Calculate end position
12:   if  $q.slots[last \bmod q.size] \neq NULL$  then
13:     return false ▷ Not enough space
14:   end if
15:   for  $i \leftarrow len - 1$  downto 0 do ▷ Reverse order
16:      $q.slots[(q.write + i) \bmod q.size] \leftarrow batch[i]$ 
17:   end for
18:   WMB() ▷ Ensure all writes visible
19:    $q.write \leftarrow (last + 1) \bmod q.size$ 
20:    $q.count \leftarrow 0$  ▷ Reset batch counter
21:   return true
22: end function
23:
24: function FLUSH( $q$ )
25:   if  $q.count > 0$  then
26:     return MULTIPUSH( $q, q.batch, q.count$ )
27:   end if
28:   return true
29: end function
    
```

5.2.2. Multi Producer Single Consumer (MPSC)

This is a bit more complex to implement than the SPSC case. Multiple producers can enqueue items at the same time while a single consumer dequeues items. This includes implementing other strategies than just adding some memory barriers, such as helping and atomic primitives to maintain wait-freedom and consistency between the producers. There are multiple approaches that are available from different papers to achieve this:

Jayantis MPSC Queue

Achieves logarithmic time complexity by distributing the global queue across n local SPSC queues implemented like in section 5.2.1 and organized under a binary tree, as shown in algorithm 13. Each producer owns a dedicated local queue, eliminating producer-producer contention. When enqueueing, a producer obtains a global timestamp via LL/SC on a shared counter in lines 2-3, creating a unique ordering even if the SC fails, since some other producer must have incremented it. If LL/SC not supported on system architecture it can be replaced with versioned CAS. The producer then inserts a timestamped pair into its local queue in line 4 and propagates this timestamp up the tree in line 5. The tree maintains the invariant that each internal node holds the minimum timestamp of its subtree. The `propagate` function

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 12 Jayanti's SPSC Queue Operations [44]

```

1: function ENQUEUE( $q, v$ )
2:    $newNode \leftarrow \text{new Node}()$                                 ▷ Create new dummy node
3:    $tmp \leftarrow q.Last$                                        ▷ Get current dummy tail
4:    $tmp.val \leftarrow v$                                        ▷ Convert dummy to data node
5:    $tmp.next \leftarrow newNode$                                 ▷ Link new dummy
6:    $q.Last \leftarrow newNode$                                   ▷ Update tail pointer
7: end function
8:
9: function DEQUEUE( $q$ )
10:   $tmp \leftarrow q.First$                                        ▷ Get head node
11:  if  $tmp = q.Last$  then                                       ▷ Only dummy remains?
12:    return  $\perp$                                                ▷ Queue empty
13:  end if
14:   $retval \leftarrow tmp.val$                                      ▷ Read value
15:   $q.Help \leftarrow retval$                                     ▷ Help concurrent readFront
16:   $q.First \leftarrow tmp.next$                                 ▷ Remove from queue
17:  if  $tmp = q.Announce$  then                                    ▷ Was announced by readFront?
18:     $tmp' \leftarrow q.FreeLater$                                 ▷ Get old deferred node
19:     $q.FreeLater \leftarrow tmp$                                 ▷ Defer current node
20:     $\text{free}(tmp')$                                              ▷ Free old deferred node
21:  else
22:     $\text{free}(tmp)$                                                ▷ Free immediately
23:  end if
24:  return  $retval$ 
25: end function
26:
27: function READFRONT_E( $q$ )                                     ▷ Called by enqueueer
28:   $tmp \leftarrow q.First$                                        ▷ Read head pointer
29:  if  $tmp = q.Last$  then                                       ▷ Queue empty?
30:    return  $\perp$ 
31:  end if
32:   $q.Announce \leftarrow tmp$                                     ▷ Announce to prevent free
33:  if  $tmp \neq q.First$  then                                    ▷ Head changed (was dequeued)?
34:     $retval \leftarrow q.Help$                                     ▷ Use helped value
35:  else
36:     $retval \leftarrow tmp.val$                                     ▷ Read directly
37:  end if
38:  return  $retval$ 
39: end function
40:
41: function READFRONT_D( $q$ )                                     ▷ Called by dequeuer
42:   $tmp \leftarrow q.First$ 
43:  if  $tmp = q.Last$  then
44:    return  $\perp$ 
45:  end if
46:  return  $tmp.val$                                              ▷ Safe - no concurrent dequeue
47: end function

```

in lines 18 - 26 walks from leaf to root, calling `refresh` at each node. The double `refresh` pattern in lines 22 - 24 ensures correctness. if the first refresh fails, another process updated the node. if the second refresh also fails, that process must have read the updated children values and installed the correct minimum. The `refresh` function uses LL/SC in lines 28 - 33 to atomically update a node with the minimum of its children's timestamps. The consumer reads the root to find the producer with the earliest element in line 9 and then dequeues from

5. Analyzing existing Wait-Free Data Structures and Algorithms

that local queue in line 13 and propagates any changes in line 14. This design transforms the $O(n)$ scan of all queues into $O(\log n)$ tree traversals, while the space complexity remains $O(n + m)$ where m is the number of queued items. [44]

Algorithm 13 Jayanti's MPSC Queue Operations [44]

```

1: function ENQUEUE( $q, p, v$ )
2:    $tok \leftarrow LL(q.counter)$  ▷ Read timestamp
3:    $SC(q.counter, tok + 1)$  ▷ Try increment
4:    $enqueue2(q.Q[p], (v, (tok, p)))$  ▷ Add timestamp to local queue
5:    $PROPAGATE(q, q.Q[p])$ 
6: end function
7:
8: function DEQUEUE( $q, p$ )
9:    $[t, id] \leftarrow read(q.T.root)$  ▷ Get min producer
10:  if  $id = \perp$  then
11:    return  $\perp$ 
12:  end if
13:   $ret \leftarrow dequeue2(q.Q[id])$ 
14:   $PROPAGATE(q, q.Q[id])$ 
15:  return  $ret.val$ 
16: end function
17:
18: function PROPAGATE( $q, localQueue$ )
19:    $currentNode \leftarrow localQueue$ 
20:   repeat
21:      $currentNode \leftarrow parent(currentNode)$ 
22:     if  $\neg REFRESH(q, currentNode)$  then ▷ First try
23:        $REFRESH(q, currentNode)$  ▷ Second ensures correctness
24:     end if
25:   until  $currentNode = q.T.root$ 
26: end function
27:
28: function REFRESH( $q, node$ )
29:    $LL(node)$  ▷ Load-link node
30:    $stamps \leftarrow$  read timestamps from  $node$ 's children
31:    $minT \leftarrow$  minimum timestamp from  $stamps$ 
32:   return  $SC(node, minT)$  ▷ Store-conditional
33: end function

```

Drescher Queue

Uses a linked list with a dummy head node to eliminate producer contention, as shown in algorithm 14. Unlike traditional MPSC queues that require retry loops, producers complete enqueue in exactly three steps. First the producers clear the item's `next` pointer in line 6, then it atomically swaps the tail pointer via `FAS` in line 7 and further links the previous tail to the new item in line 8. The `FAS` operation ensures multiple producers can enqueue concurrently without interference. The consumer reads the head and its `next` pointer in lines 12 and 13 and afterwards advances the head in line 17 if the queue is non-empty. Subsequently the consumer handles the special case of the dummy node in lines 18-24. When the dummy is dequeued, it's immediately re-enqueued in line 19 to maintain the invariant that the queue always contains at least one element to prevent complex empty queue conditions. The guard integration

5. Analyzing existing Wait-Free Data Structures and Algorithms

through `VOUCH` and `CLEAR` ensures all orders are enqueued before guard acquisition in line 2 of `VOUCH`. The guard is released before checking for pending orders in line 11 of `CLEAR`, preventing lost updates. This ordering guarantees that either the current sequencer or a new thread will process all pending orders, achieves the wait-free progress guarantees with constant time enqueue operations. [28]

Algorithm 14 Drescher's Wait-Free MPSC Queue Operations

```

1: dummy.next ← 0
2: head ← &dummy
3: tail ← &dummy
4:
5: procedure ENQUEUE(guard, item)
6:   item.next ← 0                                ▷ Clear next pointer
7:   prev ← FAS(guard.tail, item)                ▷ Atomic swap tail
8:   prev.next ← item                             ▷ Link to new item
9: end procedure
10:
11: function DEQUEUE(guard)
12:   item ← guard.head
13:   next ← guard.head.next
14:   if next = 0 then                                ▷ Empty queue?
15:     return ⊥
16:   end if
17:   guard.head ← next
18:   if item = &dummy then                            ▷ Dequeued dummy?
19:     ENQUEUE(guard, item)                          ▷ Re-enqueue dummy
20:     if guard.head.next = 0 then                    ▷ Still empty?
21:       return ⊥
22:     end if
23:     guard.head ← guard.head.next
24:     return next
25:   end if
26:   return item
27: end function

```

Jiffy Queue

A queue that uses a linked list of fixed-size arrays (buffers), as shown in function `ENQUEUE(data)` in algorithm 15 and in `DEQUEUE` function in algorithm 16. Unlike other linked-list queues that allocate nodes per element, Jiffy amortizes allocation overhead by storing multiple elements in each buffer. Producers use `FAA` on a global tail counter to reserve slots in line 2 of `enqueue`, eliminating producer-producer synchronization except during buffer allocation. Each buffer contains an array of nodes with data and a 2-bit `isSet` flag indicating the node's state: `empty` (uninitialized), `set` (data written), or `handled` (already dequeued). When the current buffer fills, producers allocate new buffers and link them via `CAS` in lines 7 and 8. To reduce allocation contention, the producer obtaining the second slot in each buffer proactively allocates the next buffer in lines 21 - 26, ensuring smooth transitions between buffers. The consumer maintains a local head pointer and scans for the first non-handled element in lines 3 - 9 of `dequeue`. To ensure linearizability when producers stall: if

5. Analyzing existing Wait-Free Data Structures and Algorithms

the head element is still `empty`, the consumer scans forward to find a `set` element in line 20, then rescans backward in line 24 to ensure no earlier element became `set` during the scan. This prevents violating FIFO ordering when a slow producer completes after a faster one. The consumer can “fold” the queue by deleting fully-handled buffers in the middle of the list during scans, to not use too much memory even with stalled producers. This achieves wait-free progress guarantees with minimal synchronization. Producers only need one FAA per enqueue, while the consumer performs no atomic operations at all. [43]

Algorithm 15 Jiffy MPSC Queue Enqueue Operation [43]

```

1: function ENQUEUE(data)
2:   location  $\leftarrow$  FAA(tail, 1)                                ▷ Reserve global index
3:   tempTail  $\leftarrow$  tailOfQueue
4:   while location is in unallocated buffer do                    ▷ Beyond last buffer?
5:     if tempTail.next = NULL then
6:       newArr  $\leftarrow$  new BufferList()
7:       if CAS(tempTail.next, NULL, newArr) then
8:         CAS(tailOfQueue, tempTail, newArr)
9:       else
10:        delete newArr                                           ▷ Another thread succeeded
11:       end if
12:     end if
13:     tempTail  $\leftarrow$  tailOfQueue                                ▷ Move to new buffer
14:   end while
15:   while location not in tempTail's buffer do                    ▷ Location in earlier buffer?
16:     tempTail  $\leftarrow$  tempTail.prev                               ▷ Walk backward
17:   end while
18:   index  $\leftarrow$  location - tempTail.startIndex                  ▷ Buffer-local index
19:   tempTail.buffer[index].data  $\leftarrow$  data
20:   tempTail.buffer[index].isSet  $\leftarrow$  SET                      ▷ Mark as ready
21:   if index = 1 AND tempTail is last buffer then                ▷ Second slot?
22:     newArr  $\leftarrow$  new BufferList()                               ▷ Proactive allocation
23:     if NOT CAS(tempTail.next, NULL, newArr) then
24:       delete newArr
25:     end if
26:   end if
27: end function

```

DQueue

Combines local buffering with a segmented shared queue to minimize synchronization overhead, as shown in function `ENQUEUE(data)` in algorithm 17 and in `DEQUEUE` function in algorithm 18. DQueue reduces contention by having producers accumulate enqueue requests in thread-local ring buffers before writing them to the shared queue in batches. Producers reserve slots using FAA on a global tail counter in line 7 of `enqueue`, storing both the data and the reserved cell index (*cid*) in their local buffer. Each producer maintains a buffer of `Request` structures with capacity *L*, using `local_head` and `local_tail` pointers to track buffer state. When the buffer fills, detected in line 2, the producer calls `dump_local_buffer` to flush all buffered requests. During flushing, producers write values directly to their reserved cells in line 15 without synchronization, as each cell is exclusively owned by the reserving

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 16 Jiffy MPSC Queue Dequeue Operation [43]

```

1: function DEQUEUE
2:    $n \leftarrow \text{headOfQueue.buffer}[\text{head}]$ 
3:   while  $n.\text{isSet} = \text{HANDLED}$  do                                     ▷ Skip dequeued items
4:      $\text{head} \leftarrow \text{head} + 1$ 
5:     if end of buffer then
6:       move to next buffer and delete current
7:     end if
8:      $n \leftarrow \text{headOfQueue.buffer}[\text{head}]$ 
9:   end while
10:  if queue is empty then
11:    return  $\perp$ 
12:  end if
13:  if  $n.\text{isSet} = \text{SET}$  then                                           ▷ Ready to dequeue?
14:     $\text{data} \leftarrow n.\text{data}$ 
15:     $n.\text{isSet} \leftarrow \text{HANDLED}$ 
16:     $\text{head} \leftarrow \text{head} + 1$ 
17:    return  $\text{data}$ 
18:  end if
19:  if  $n.\text{isSet} = \text{EMPTY}$  then                                           ▷ Incomplete enqueue?
20:     $\text{tempN} \leftarrow \text{Scan}(\text{find first SET element})$ 
21:    if no SET element found then
22:      return  $\perp$ 
23:    end if
24:     $\text{Rescan}(n, \text{tempN})$                                                ▷ Check for newly set elements
25:     $\text{data} \leftarrow \text{tempN}.\text{data}$ 
26:     $\text{tempN}.\text{isSet} \leftarrow \text{HANDLED}$ 
27:    return  $\text{data}$ 
28:  end if
29: end function
30:
31: function SCAN                                                         ▷ Find first SET element
32:  for each element from current position do
33:    if  $\text{element.isSet} = \text{SET}$  then
34:      return element
35:    end if
36:    if entire buffer is HANDLED then
37:      fold queue (delete buffer)
38:    end if
39:  end for
40:  return NULL
41: end function
42:
43: function RESCAN( $\text{start}, \text{end}$ )                                         ▷ Check for ordering violations
44:  for each element from  $\text{start}$  to  $\text{end}$  do
45:    if  $\text{element.isSet} = \text{SET}$  then
46:       $\text{end} \leftarrow \text{element}$                                          ▷ Found earlier SET element
47:      restart scan from  $\text{start}$ 
48:    end if
49:  end for
50: end function

```

producer. Producers cache their current segment pointer (pseg) and update it when moving to newer segments in line 18. The `find_segment` function traverses the segment list and allocates new segments on-demand using CAS in line 29. To maintain wait-freedom when producers stall, the consumer encountering an empty cell that should contain data, checked

5. Analyzing existing Wait-Free Data Structures and Algorithms

in line 7 of `dequeue`, distinguishes between an empty queue in line 8 and a pending enqueue by checking if `head` equals `tail`. For pending enqueues, `help_enqueue` in line 11 iterates through all producers' local buffers from lines 19-31, writing any buffered values to their reserved cells in line 28. The helper skips producers that have already moved past the target segment in line 24, avoiding unnecessary work. This ensures minimal synchronization with only one FAA per enqueue and no atomics for dequeue and improves cache locality via batched writes that reduce false sharing and writes that directly write to known cell locations without searching. The consumer's dequeue operation has its linearization point at line 14 where it increments the head pointer. [41]

Algorithm 17 DQueue MPSC Queue Enqueue Operation [41]

```

1: function ENQUEUE(Producer p, data)
2:   if next(p.local_tail) = p.local_head then
3:     dump_local_buffer(p)                                     ▷ Flush when full
4:   end if
5:   tail ← p.local_tail
6:   p.local_buffer[tail].val ← data
7:   p.local_buffer[tail].cid ← FAA(q.tail, 1)                 ▷ Reserve slot
8:   p.local_tail ← next(p.local_tail)
9: end function
10:
11: function DUMP_LOCAL_BUFFER(Producer p)
12:   while p.local_head ≠ p.local_tail do
13:     r ← p.local_buffer[p.local_head]
14:     seg ← find_segment(p.pseg, r.cid)
15:     seg.cell[r.cid mod N] ← r.val                             ▷ Write in batch
16:     p.local_head ← next(p.local_head)
17:     if p.pseg ≠ seg then
18:       p.pseg ← seg                                           ▷ Update segment cache
19:     end if
20:   end while
21: end function
22:
23: function FIND_SEGMENT(Segment *sp, int cid)
24:   curr ← sp
25:   for i ← curr → id; i < cid/N; i++ do
26:     next ← curr → next
27:     if next = NULL then
28:       new ← new_segment(i + 1)
29:       if CAS(curr → next, NULL, new) then
30:         next ← new
31:       else
32:         delete new                                           ▷ Another thread succeeded
33:       end if
34:     end if
35:     curr ← next
36:   end for
37:   return curr
38: end function

```

Algorithm 18 DQueue MPSC Queue Dequeue Operation [41]

```

1: function DEQUEUE(Consumer c)
2:   seg  $\leftarrow$  find_segment(c.cseg, q.head)
3:   if c.cseg  $\neq$  seg then
4:     c.cseg  $\leftarrow$  seg ▷ Update segment cache
5:   end if
6:   cell  $\leftarrow$  seg.cell[q.head mod N]
7:   if cell =  $\perp$  then ▷ Empty cell?
8:     if q.head = q.tail then
9:       return EMPTY
10:    else
11:      help_enqueue() ▷ Help stalled producers
12:    end if
13:  end if
14:  q.head  $\leftarrow$  q.head + 1 ▷ Linearization point
15:  return cell
16: end function
17:
18: function HELP_ENQUEUE
19:   for each Producer p in system do
20:     for each Request r in p.local_buffer do
21:       pos  $\leftarrow$  r.cid
22:       val  $\leftarrow$  r.val
23:       seg  $\leftarrow$  find_segment(p.pseg, pos)
24:       if seg.id > pos/N then
25:         break ▷ Producer moved past
26:       end if
27:       if seg.cell[pos mod N] =  $\perp$  then
28:         seg.cell[pos mod N]  $\leftarrow$  val ▷ Help write
29:       end if
30:     end for
31:   end for
32: end function

```

5.2.3. Single Producer Multi Consumer (SPMC)

This case is trickier to implement, since now multiple reading workers have to be synchronized to read consistently without any unwanted behavior. Multiple producers was simpler, since making producers write specific data each is not so hard. In this case every consumer has to be synchronized so that when one item is consumed by a consumer, it cannot be consumed again from another and also the ordering has to be kept. That is most probably also the reason only one algorithm for this contention category was found. The approach to achieve this in a wait-free manner is the following:

David Queue

Uses a two-dimensional array of Swap objects to handle the race condition where consumers overtake the producer, as shown in algorithm 19. David's queue allows the producer to detect when it has been overtaken and adapt by jumping to a fresh row. The producer maintains two persistent local variables, a `enq_row` (current row) and `tail` (next column to write) variable. During enqueue, the producer swaps the value into `ITEMS[enq_row, tail]` in line 10

5. Analyzing existing Wait-Free Data Structures and Algorithms

and checks if the retrieved value is \top , indicating a consumer already accessed this cell. If so, the producer jumps to the next row in lines 12 - 15, writing the value to the new row and updating the shared `ROW` register. This jump mechanism ensures that enqueued values are never lost. Consumers read the active row from `ROW` in line 22 of `dequeue`, then increment using Fetch and Increment (Like `FAA`, but incrementing) on `HEAD[deq_row]` in line 23 to reserve a unique column index. They swap \top into the reserved cell in line 24, retrieving either the enqueued value or \perp (empty). The use of swap instead of plain registers is important, because it allows the producer to detect consumer interference (by finding \top) and consumers to mark cells as processed. Each cell in `ITEMS` is accessed at most once by an enqueue and once by a dequeue operation. The algorithm achieves 3-bounded wait-freedom with constant time operations. The producer completes in at most 3 steps (regular enqueue: 1 step, jump enqueue: 3 steps), while consumers always complete in exactly 3 steps. [27]

Algorithm 19 David's Queue Operations [27]

```

1: Shared variables:
2: HEAD: array of Fetch&Increment objects, initially 0
3: ITEMS: 2D array of Swap objects, initially  $\perp$ 
4: ROW: Register, initially 0
5:
6: Enqueuer's persistent local variables:
7: enq_row  $\leftarrow$  0, tail  $\leftarrow$  0
8:
9: procedure ENQUEUE(x)                                     ▷ For enqueuer E only
10:   val  $\leftarrow$  Swap(ITEMS[enq_row, tail], x)              ▷ Try to enqueue
11:   if val =  $\top$  then                                         ▷ Dequeuer overtook us?
12:     enq_row  $\leftarrow$  enq_row + 1                             ▷ Jump to next row
13:     tail  $\leftarrow$  0
14:     Swap(ITEMS[enq_row, tail], x)                         ▷ Write to new row
15:     Write(ROW, enq_row)                                    ▷ Publish new row
16:   end if
17:   tail  $\leftarrow$  tail + 1
18:   return OK
19: end procedure
20:
21: function DEQUEUE                                           ▷ For dequeuers D1, ..., Dn
22:   deq_row  $\leftarrow$  Read(ROW)                                ▷ Get active row
23:   head  $\leftarrow$  Fetch&Increment(HEAD[deq_row])             ▷ Reserve column
24:   val  $\leftarrow$  Swap(ITEMS[deq_row, head],  $\top$ )              ▷ Get value
25:   if val =  $\perp$  then                                         ▷ Empty cell?
26:     return  $\epsilon$                                               ▷ Queue was empty
27:   else
28:     return val                                              ▷ Return dequeued value
29:   end if
30: end function

```

5.2.4. Multi Producer Multi Consumer (MPMC)

Finally a look into the MPMC case can be made. Here we need to think about synchronize producer-producer contention, consumer-consumer contention and producer consumer

5. Analyzing existing Wait-Free Data Structures and Algorithms

contention. This includes helping methods for the producer and consumer and different atomic primitives. Multiple approaches are available to achieve this:

Kogan and Petranks queue

Uses a priority-based helping scheme with Michael and Scott's lock-free queue from algorithm 1 as the foundation to achieve wait-freedom, as shown in algorithm 20, algorithm 21 and algorithm 22. Threads complete operations in bounded steps by helping slower peers. Each thread chooses a monotonically increasing phase number in line 2 of `ENQUEUE` in algorithm 20 and line 2 of `DEQUEUE` of algorithm 21, then records operation details in a shared `state` array in line 3. The helping mechanism in `HELP` from lines 15 - 26 in algorithm 22 ensures all operations with phases \leq the current phase complete. Threads traverse the state array and invoke `HELP_ENQ` or `HELP_DEQ` based on pending operations in lines 19 - 23 of algorithm 22. For enqueue, threads utilize the tail update like in Michael and Scott by first appending the node via `CAS` in line 15 of `HELP_ENQ` in algorithm 20, then finally helping by updating the tail in line 36 of `HELP_FINISH_ENQ`. The three-step scheme ensures exactly-once execution by first appending a node to list in line 15 then clear the pending flag in line 35 of `HELP_FINISH_ENQ`, and finally update the tail pointer in line 36. For dequeue, threads write their ID to the `deqTid` field of the head node in line 41 of `HELP_DEQ` in algorithm 21 to "lock" it logically. The consumer then updates the pending flag in line 9 of `HELP_FINISH_DEQ` in algorithm 22 and advances head in line 10. Special handling for empty queues occurs in lines 20 - 25 of `HELP_DEQ` of algorithm 21, where threads update state with null to indicate emptiness. The phase selection using `MAXPHASE` in lines 41-50 in algorithm 20 ensures threads help all concurrent operations before returning, preventing starvation. This achieves wait-free progress with $O(n)$ steps per operation where n is the number of threads. [33]

Turn Queue

Uses a novel turn-based consensus mechanism to achieve wait-freedom without requiring `FAA` instructions. As shown in algorithm 23, algorithm 24 and algorithm 25, the queue maintains two arrays: `enqueueers` for enqueue requests and `deqself/deqhelp` for dequeue operations. Each thread has a unique index used as its thread ID (`enqTid` or `deqTid`). For the producers in algorithm 23, threads publish their intent by storing a node pointer in `enqueueers[myIdx]` in line 6 of the function `ENQUEUE`. The consensus mechanism uses the `enqTid` of the tail node to determine whose turn is next. Threads scan the `enqueueers` array starting from position $(tail \rightarrow enqTid + 1) \% maxThreads$ in line 20, helping the first non-null request they find. This creates a circular turn order ensuring fairness. The algorithm guarantees that after publishing a request, at most $maxThreads - 1$ other nodes will be enqueued first, achieving wait-free bounded progress. The enqueue operation protects the tail pointer using hazard pointers in line 12 of the `ENQUEUE` function, then clears any completed request from the tail's position in lines 15 - 18. It searches for the next request to help in lines 19 - 26, attempting to append the found node via `CAS` in line 23. Finally, it advances the tail pointer

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 20 Kogan and Petrank's Queue Enqueue Operation [33]

```

1: function ENQUEUE(value)
2:   phase ← MAXPHASE + 1                                ▷ Choose phase
3:   state[tid] ← OpDesc(phase, true, true, Node(value, tid))
4:   HELP(phase)                                           ▷ Help all ops ≤ phase
5:   HELP_FINISH_ENQ                                       ▷ Ensure tail updated
6: end function
7:
8: procedure HELP_ENQ(tid, phase)
9:   while ISSTILLPENDING(tid, phase) do
10:    last ← tail
11:    next ← last.next
12:    if last = tail then                                ▷ Validate read
13:      if next = null then                                ▷ Can append?
14:        if ISSTILLPENDING(tid, phase) then
15:          if CAS(last.next, null, state[tid].node) then
16:            HELP_FINISH_ENQ
17:            return
18:          end if
19:        end if
20:      else                                                ▷ Help pending enqueue
21:        HELP_FINISH_ENQ
22:      end if
23:    end if
24:  end while
25: end procedure
26:
27: procedure HELP_FINISH_ENQ
28:   last ← tail
29:   next ← last.next
30:   if next ≠ null then
31:     tid ← next.enqTid                                   ▷ Thread that owns node
32:     desc ← state[tid]
33:     if last = tail and state[tid].node = next then
34:       newDesc ← OpDesc(state[tid].phase, false, true, next)
35:       CAS(state[tid], desc, newDesc)                   ▷ Clear pending
36:       CAS(tail, last, next)                             ▷ Update tail
37:     end if
38:   end if
39: end procedure
40:
41: function MAXPHASE
42:   max ← -1
43:   for i ← 0 to NUM_THREADS - 1 do
44:     phase ← state[i].phase
45:     if phase > max then
46:       max ← phase
47:     end if
48:   end for
49:   return max
50: end function

```

if a node was successfully appended in line 29. The operation completes when the thread's own request has been processed (detected by checking if `enqueueers[myIdx]` is null in line 8). For consumers in algorithm 24, the algorithm uses a dual-array approach with `deqself` and `deqhelp` to avoid excessive hazard pointer usage. Threads open a request by making

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 21 Kogan and Petrank's Queue Dequeue Operation [33]

```

1: function DEQUEUE
2:    $phase \leftarrow \text{MAXPHASE} + 1$ 
3:    $state[tid] \leftarrow \text{OpDesc}(phase, \text{true}, \text{false}, \text{null})$ 
4:    $\text{HELP}(phase)$ 
5:    $\text{HELP\_FINISH\_DEQ}$ 
6:    $node \leftarrow state[tid].node$ 
7:   if  $node = \text{null}$  then
8:     throw  $\text{EmptyException}$ 
9:   end if
10:  return  $node.next.value$ 
11: end function
12:
13: procedure  $\text{HELP\_DEQ}(tid, phase)$ 
14:  while  $\text{ISSTILLPENDING}(tid, phase)$  do
15:     $first \leftarrow head$ 
16:     $last \leftarrow tail$ 
17:     $next \leftarrow first.next$ 
18:    if  $first = head$  then
19:      if  $first = last$  then
20:        if  $next = \text{null}$  then
21:           $desc \leftarrow state[tid]$ 
22:          if  $last = tail$  and  $\text{ISSTILLPENDING}(tid, phase)$  then
23:             $newDesc \leftarrow \text{OpDesc}(state[tid].phase, \text{false}, \text{false}, \text{null})$ 
24:             $\text{CAS}(state[tid], desc, newDesc)$ 
25:          end if
26:        else
27:           $\text{HELP\_FINISH\_ENQ}$ 
28:        end if
29:      else
30:         $desc \leftarrow state[tid]$ 
31:         $node \leftarrow desc.node$ 
32:        if not  $\text{ISSTILLPENDING}(tid, phase)$  then
33:          break
34:        end if
35:        if  $first = head$  and  $node \neq first$  then
36:           $newDesc \leftarrow \text{OpDesc}(state[tid].phase, \text{true}, \text{false}, first)$ 
37:          if not  $\text{CAS}(state[tid], desc, newDesc)$  then
38:            continue
39:          end if
40:        end if
41:         $\text{CAS}(first.deqTid, -1, tid)$ 
42:         $\text{HELP\_FINISH\_DEQ}$ 
43:      end if
44:    end if
45:  end while
46: end procedure

```

▷ Validate read
 ▷ Queue might be empty
 ▷ Confirmed empty

 ▷ Help enqueue

 ▷ Queue not empty

 ▷ Lock node

$deqself[myIdx]$ equal to $deqhelp[myIdx]$ in lines 4 and 5 of the DEQUEUE function. The turn order follows the $deqTid$ of the head node. When assigning nodes, threads use CAS to set the next node's $deqTid$ field in line 8 of SEARCHNEXT in algorithm 25. This assignment is permanent and indicates ownership. The dequeue handles empty queues through a "give-up" mechanism implemented in GIVEUP (lines 28-44 of algorithm 25). When detecting an empty queue (head equals tail) in line 12 of DEQUEUE in algorithm 24, threads rollback their request in line 13 but must ensure no concurrent thread assigned them a node. This

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 22 Kogan and Petrank's Queue Dequeue Helping Operations [33]

```

1: procedure HELP_FINISH_DEQ
2:   first  $\leftarrow$  head
3:   next  $\leftarrow$  first.next
4:   tid  $\leftarrow$  first.deqTid ▷ Thread that locked node
5:   if tid  $\neq$  -1 then
6:     desc  $\leftarrow$  state[tid]
7:     if first = head and next  $\neq$  null then
8:       newDesc  $\leftarrow$  OpDesc(state[tid].phase, false, false, state[tid].node)
9:       CAS(state[tid], desc, newDesc) ▷ Clear pending
10:      CAS(head, first, next) ▷ Advance head
11:    end if
12:  end if
13: end procedure
14:
15: procedure HELP(phase)
16:   for i  $\leftarrow$  0 to NUM_THREADS - 1 do
17:     desc  $\leftarrow$  state[i]
18:     if desc.pending and desc.phase  $\leq$  phase then
19:       if desc.enqueue then
20:         HELP_ENQ(i, phase)
21:       else
22:         HELP_DEQ(i, phase)
23:       end if
24:     end if
25:   end for
26: end procedure

```

involves re-checking the queue state and potentially self-assigning the first node if no other requests exist (line 41 of GIVEUP). The algorithm closes requests by updating `deqhelp[i]` in line 18 of CASDEQANDHEAD in algorithm 25, making it differ from `deqself[i]`. Memory reclamation uses wait-free bounded hazard pointers integrated into the algorithm. Nodes are retired in line 35 of DEQUEUE in algorithm 24 only after ensuring they're no longer accessible through shared variables. The algorithm requires only one allocation per enqueued item (the node itself), achieving minimal memory overhead of $O(N_{threads})$ compared to the $O(N_{threads}^2)$ of other wait-free queues. [37]

YMC queue

Uses FAA and CAS combined with Kogan's and Petrank's fast-path slow-path methodology mentioned in chapter 3 to use the advantage of lock-free algorithms if possible while still maintaining wait-freedom. As shown in algorithm 26, algorithm 27, algorithm 28, and algorithm 29, the queue represents cells as an infinite array emulated through linked segments. Each segment contains *N* cells and a pointer to the next segment. The queue maintains global indices *H* (head) and *T* (tail) that are accessed using FAA, ensuring atomic increments without retry loops. For producers in algorithm 26, threads obtain a unique cell index via FAA on *T* in line 11. They then locate the corresponding cell using `find_cell` which traverses segments and allocates new ones if needed. The fast-path attempts a simple CAS to deposit the value in line 13. If this fails, due to concurrent dequeue marking the cell unusable, the thread switches to

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 23 Turn Queue Enqueue Operation [37]

```

1: function ENQUEUE(item)
2:   if item = null then throw InvalidArgument
3:   end if
4:   myIdx ← GETINDEX
5:   myNode ← new Node(item, myIdx)
6:   enqueueers[myIdx] ← myNode
7:   for i ← 0 to maxThreads − 1 do
8:     if enqueueers[myIdx] = null then                                ▷ Request completed
9:       hp.CLEAR
10:      return
11:    end if
12:    ltail ← hp.PROTECTPTR(kHpTail, tail)
13:    if ltail ≠ tail then continue
14:    end if
15:    if enqueueers[ltail.enqTid] = ltail then                            ▷ Clear old request
16:      tmp ← ltail
17:      CAS(enqueueers[ltail.enqTid], tmp, null)
18:    end if
19:    for j ← 1 to maxThreads do                                          ▷ Find next request
20:      nodeHelp ← enqueueers[(j + ltail.enqTid) mod maxThreads]
21:      if nodeHelp ≠ null then
22:        nullnode ← null
23:        CAS(ltail.next, nullnode, nodeHelp)                            ▷ Try append
24:        break
25:      end if
26:    end for
27:    lnext ← ltail.next
28:    if lnext ≠ null then                                                ▷ Advance tail if needed
29:      CAS(tail, ltail, lnext)
30:    end if
31:  end for
32:  enqueueers[myIdx] ← null                                            ▷ Cleanup if not helped
33:  hp.CLEAR
34: end function

```

the slow-path starting at line 20. The slow-path employs a helping mechanism where threads publish enqueue requests in their handle structure (line 23). In algorithm 29 consumers help pending enqueues through `help_enq` in line 13 when they mark cells unusable. This creates a symbiotic relationship: producers get help depositing values, while consumers ensure values are available to dequeue. For consumers in algorithm 28, threads obtain cell indices via `FAA` on `H` in line 18. The algorithm uses `help_enq` to secure values, which may involve helping slow-path enqueues. If a value is found, the consumer claims it using CAS on the cell's `deq` field (line 23). The slow-path (line 30) publishes dequeue requests that helpers can satisfy by finding unclaimed values or determining the queue is empty. The algorithm maintains linearizability through careful ordering. Enqueues linearize when `T` moves past their cell index, while dequeues linearize when `H` moves past theirs. The helping mechanism ensures that after at most $O(n^2)$ failed attempts, all threads become helpers for a pending operation, guaranteeing completion. [40]

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 24 Turn Queue Dequeue Operation [37]

```

1: function DEQUEUE
2:    $myIdx \leftarrow \text{GETINDEX}$ 
3:    $prReq \leftarrow deqself[myIdx]$  ▷ Save previous request
4:    $myReq \leftarrow deqhelp[myIdx]$ 
5:    $deqself[myIdx] \leftarrow myReq$  ▷ Open request
6:   for  $i \leftarrow 0$  to  $maxThreads - 1$  do
7:     if  $deqhelp[myIdx] \neq myReq$  then break ▷ Request satisfied
8:     end if
9:      $lhead \leftarrow hp.PROTECTPTR(kHpHead, head)$ 
10:    if  $lhead \neq head$  then continue
11:    end if
12:    if  $lhead = tail$  then ▷ Queue empty
13:       $deqself[myIdx] \leftarrow prReq$  ▷ Rollback
14:       $GIVEUP(myReq, myIdx)$ 
15:      if  $deqhelp[myIdx] \neq myReq$  then ▷ Check if helped
16:         $deqself[myIdx] \leftarrow myReq$ 
17:        break
18:      end if
19:       $hp.CLEAR$ 
20:      return null
21:    end if
22:     $lnext \leftarrow hp.PROTECTPTR(kHpNext, lhead.next)$ 
23:    if  $lhead \neq head$  then continue
24:    end if
25:    if  $SEARCHNEXT(lhead, lnext) \neq NOIDX$  then
26:       $CASDEQANDHEAD(lhead, lnext, myIdx)$ 
27:    end if
28:  end for
29:   $myNode \leftarrow deqhelp[myIdx]$ 
30:   $lhead \leftarrow hp.PROTECTPTR(kHpHead, head)$ 
31:  if  $lhead = head$  and  $myNode = lhead.next$  then
32:     $CAS(head, lhead, myNode)$  ▷ Help advance head
33:  end if
34:   $hp.CLEAR$ 
35:   $hp.RETIRE(prReq)$  ▷ Retire previous node
36:  return  $myNode.item$ 
37: end function

```

Feldman-Dechev Queue

Uses a sequence number-based mechanism with bitmarking to achieve bounded completion. As shown in algorithm 30, algorithm 31, and algorithm 32, the ring buffer maintains two atomic counters accessed via `NextTailSeq` in line 7 of algorithm 30 and `NextHeadSeq` in line 7 of algorithm 31. Each position in the buffer array stores either an `ElemNode` containing an element and sequence ID, or an `EmptyNode` containing only a sequence ID. For producers in algorithm 30, threads acquire a sequence ID via `FAA` on the tail counter in line 7. The position is determined as `seqid mod capacity` in line 8. In the common case, threads replace an `EmptyNode` with matching or lower sequence ID with their prepared `ElemNode` via `CAS` in line 32. The algorithm handles thread delays through backoff and retry mechanisms. If a position contains an `ElemNode` or has a higher sequence ID than assigned, the thread breaks from the inner loop in line 36 to acquire a new sequence ID in the outer loop and

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 25 Turn Queue Dequeue Helper Functions [37]

```

1: function SEARCHNEXT(lhead, lnext)
2:   turn  $\leftarrow$  lhead.deqTid
3:   for idx  $\leftarrow$  turn + 1 to turn + maxThreads do
4:     idDeq  $\leftarrow$  idx mod maxThreads
5:     if deqself[idDeq]  $\neq$  deqhelp[idDeq] then continue
6:     end if
7:     if lnext.deqTid = NOIDX then
8:       CAS(lnext.deqTid, NOIDX, idDeq)
9:     end if
10:    break
11:  end for
12:  return lnext.deqTid
13: end function
14:
15: procedure CASDEQANDHEAD(lhead, lnext, myIdx)
16:   ldeqTid  $\leftarrow$  lnext.deqTid
17:   if ldeqTid = myIdx then
18:     deqhelp[ldeqTid]  $\leftarrow$  lnext
19:   else
20:     ldeqhelp  $\leftarrow$  hp.PROTECTPTR(kHpDeq, deqhelp[ldeqTid])
21:     if ldeqhelp  $\neq$  lnext and lhead = head then
22:       CAS(deqhelp[ldeqTid], ldeqhelp, lnext)
23:     end if
24:   end if
25:   CAS(head, lhead, lnext)
26: end procedure
27:
28: procedure GIVEUP(myReq, myIdx)
29:   lhead  $\leftarrow$  head
30:   if deqhelp[myIdx]  $\neq$  myReq then return
31: end if
32:   if lhead = tail then return
33: end if
34:   hp.PROTECTPTR(kHpHead, lhead)
35:   if lhead  $\neq$  head then return
36: end if
37:   lnext  $\leftarrow$  hp.PROTECTPTR(kHpNext, lhead.next)
38:   if lhead  $\neq$  head then return
39: end if
40:   if SEARCHNEXT(lhead, lnext) = NOIDX then
41:     CAS(lnext.deqTid, NOIDX, myIdx)
42:   end if
43:   CASDEQANDHEAD(lhead, lnext, myIdx)
44: end procedure

```

attempt insertion at a new position. Bitmarking, setting a flag on a node, is used to indicate positions needing correction by delayed threads in line 20. For consumers in algorithm 31, threads similarly acquire a sequence ID via FAA on the head counter in line 7. They prepare an `EmptyNode` with sequence ID incremented by the buffer capacity in line 9. The dequeue succeeds when replacing an `ElemNode` with matching sequence ID in line 42 via CAS. If encountering an `EmptyNode` or lower sequence ID, threads use backoff and may bitmark `ElemNodes` to maintain FIFO ordering in line 32. The algorithm achieves bounded completion through a progress assurance scheme. After `MAX_FAILS` attempts in line 11, threads post

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 26 YMC Queue Enqueue Operation [40]

```

1: function ENQUEUE( $q, h, v$ )
2:   for  $p \leftarrow \text{PATIENCE}$  downto 0 do                                ▷ Try fast-path first
3:     if ENQ_FAST( $q, h, v, \&\text{cell\_id}$ ) then
4:       return
5:     end if
6:   end for
7:   ENQ_SLOW( $q, h, v, \text{cell\_id}$ )                                       ▷ Fall back to slow-path
8: end function
9:
10: function ENQ_FAST( $q, h, v, \text{cid}$ )
11:    $i \leftarrow \text{FAA}(\&q \rightarrow T, 1)$                                 ▷ Get unique cell index
12:    $c \leftarrow \text{FIND\_CELL}(\&h \rightarrow \text{tail}, i)$                     ▷ Locate cell, allocate segment if needed
13:   if CAS( $c.\text{val}, \perp, v$ ) then                                       ▷ Try to deposit value
14:     return true
15:   end if
16:    $\ast \text{cid} \leftarrow i$                                              ▷ Return cell index for slow-path
17:   return false
18: end function
19:
20: function ENQ_SLOW( $q, h, v, \text{cell\_id}$ )
21:    $r \leftarrow \&h \rightarrow \text{enq.req}$ 
22:    $r \rightarrow \text{val} \leftarrow v$                                            ▷ Publish value
23:    $r \rightarrow \text{state} \leftarrow (1, \text{cell\_id})$                              ▷ Set pending=1, id=cell_id
24:    $\text{tmp\_tail} \leftarrow h \rightarrow \text{tail}$ 
25:   repeat
26:      $i \leftarrow \text{FAA}(\&q \rightarrow T, 1)$ 
27:      $c \leftarrow \text{FIND\_CELL}(\&\text{tmp\_tail}, i)$ 
28:     if CAS( $c \rightarrow \text{enq}, \perp_e, r$ ) and  $c.\text{val} = \perp$  then           ▷ Reserve cell
29:       TRY_TO_CLAIM_REQ( $\&r \rightarrow \text{state}, i, i$ )                     ▷ Claim request for this cell
30:       break
31:     end if
32:   until  $\neg r \rightarrow \text{state.pending}$                                 ▷ Until helped by dequeuer
33:    $\text{id} \leftarrow r \rightarrow \text{state.id}$                                    ▷ Get claimed cell index
34:    $c \leftarrow \text{FIND\_CELL}(\&h \rightarrow \text{tail}, \text{id})$ 
35:   ENQ_COMMIT( $q, c, v, \text{id}$ )                                       ▷ Write value to claimed cell
36: end function

```

their operation to an announcement table and execute a wait-free slow path in lines 12-14. The helping mechanism works as follows: TryHelpAnother in lines 33-45 of algorithm 32 checks one entry in the announcement table per call, cycling through all threads. When an announced operation is found, helpers attempt to complete it using the Associate functions. These functions either claim and complete the operation via CAS or clean up failed attempts by replacing nodes. This ensures every operation completes within $O(N_{\text{threads}}^2)$ steps, as all threads will eventually help any announced operation. [35]

Verma's Queue

Uses an external helper thread that works on a dedicated core to help other processes to finish their work in a finite number of steps. As shown in algorithm 33, the queue maintains a state array where each worker has a dedicated slot for operation requests. The queue uses a linked list with head and tail pointers managed exclusively by the helper thread. For producers in

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 27 YMC Queue Enqueue Help Operation [40]

```

1: function HELP_ENQ( $q, h, c, i$ )
2:   if  $\neg \text{CAS}(c \rightarrow val, \perp, \top)$  and  $c \rightarrow val \neq \top$  then                                ▷ Value already present
3:     return  $c \rightarrow val$ 
4:   end if
5:   if  $c \rightarrow enq = \perp_e$  then                                                        ▷ No request yet, find one to help
6:     repeat
7:        $p \leftarrow h \rightarrow enq.peer$ 
8:        $r \leftarrow \&p \rightarrow enq.req$ 
9:        $s \leftarrow r \rightarrow state$ 
10:      if  $h \rightarrow enq.id = 0$  or  $h \rightarrow enq.id = s.id$  then                                ▷ Haven't helped this request
11:        break
12:      end if
13:       $h \rightarrow enq.id \leftarrow 0$ 
14:       $h \rightarrow enq.peer \leftarrow p \rightarrow next$                                     ▷ Move to next peer
15:    until true
16:    if  $s.pending$  and  $s.id \leq i$  and  $\neg \text{CAS}(c \rightarrow enq, \perp_e, r)$  then                ▷ Try to reserve cell for peer
17:       $h \rightarrow enq.id \leftarrow s.id$                                                 ▷ Remember we tried to help
18:    else
19:       $h \rightarrow enq.peer \leftarrow p \rightarrow next$                                     ▷ Peer doesn't need help
20:    end if
21:    if  $c \rightarrow enq = \perp_e$  then
22:       $\text{CAS}(c \rightarrow enq, \perp_e, \top_e)$                                             ▷ Mark no enqueue will use this cell
23:    end if
24:  end if
25:  if  $c \rightarrow enq = \top_e$  then                                                        ▷ No enqueue will fill this cell
26:    return ( $q \rightarrow T \leq i$  ? EMPTY : ⊤)                                       ▷ Check if queue was empty
27:  end if
28:   $r \leftarrow c \rightarrow enq$                                                         ▷ Cell has enqueue request
29:   $s \leftarrow r \rightarrow state$ 
30:   $v \leftarrow r \rightarrow val$ 
31:  if  $s.id > i$  then                                                                ▷ Request unsuitable for this cell
32:    if  $c \rightarrow val = \top$  and  $q \rightarrow T \leq i$  then
33:      return EMPTY
34:    end if
35:  else if TRY_TO_CLAIM_REQ( $\&r \rightarrow state, s.id, i$ ) or ( $s = (0, i)$  and  $c \rightarrow val = \top$ ) then
36:    ENQ_COMMIT( $q, c, v, i$ )                                                    ▷ Help commit the value
37:  end if
38:  return  $c \rightarrow val$ 
39: end function

```

algorithm 33, threads create a request object containing the operation type and element in line 14, then place it in their designated position in the state array via direct assignment in line 15. They wait until the helper marks the operation as completed in line 16. The algorithm achieves simplicity by delegating all queue modifications to a single helper thread, eliminating the need for complex synchronization. For consumers in algorithm 33, threads similarly create a dequeue request in line 3 and place it in their state array slot in line 4. They wait for completion in line 5, after which the dequeued element is available in the request object in line 9. The helper thread in algorithm 33 continuously traverses the state array in round-robin fashion in lines 24-52. When encountering an enqueue request, it creates a new node in line 29, appends it to the tail in line 30, and updates the tail reference in line 31. For dequeue requests, the helper checks if the queue is empty in line 35 and removes the head element in lines 39 and 40. The helper then updates the request with the dequeued value in line 44. This achieves

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 28 YMC Queue Dequeue Operation [40]

```

1: function DEQUEUE( $q, h$ )
2:   for  $p \leftarrow \text{PATIENCE}$  downto 0 do                                     ▷ Try fast-path first
3:      $v \leftarrow \text{DEQ\_FAST}(q, h, \&\text{cell\_id})$ 
4:     if  $v \neq \top$  then break
5:     end if
6:   end for
7:   if  $v = \top$  then                                                         ▷ Fast-path failed
8:      $v \leftarrow \text{DEQ\_SLOW}(q, h, \text{cell\_id})$                                ▷ Use slow-path
9:   end if
10:  if  $v \neq \text{EMPTY}$  then                                                     ▷ Got value, help peer dequeue
11:     $\text{HELP\_DEQ}(q, h, h \rightarrow \text{deq.peer})$ 
12:     $h \rightarrow \text{deq.peer} \leftarrow h \rightarrow \text{deq.peer} \rightarrow \text{next}$ 
13:  end if
14:  return  $v$ 
15: end function
16:
17: function DEQ_FAST( $q, h, id$ )
18:   $i \leftarrow \text{FAA}(\&q \rightarrow H, 1)$                                            ▷ Get unique cell index
19:   $c \leftarrow \text{FIND\_CELL}(\&h \rightarrow \text{head}, i)$ 
20:   $v \leftarrow \text{HELP\_ENQ}(q, h, c, i)$                                        ▷ Try to get/help produce value
21:  if  $v = \text{EMPTY}$  then return  $\text{EMPTY}$ 
22:  end if
23:  if  $v \neq \top$  and  $\text{CAS}(c \rightarrow \text{deq}, \perp_d, \top_d)$  then             ▷ Claim the value
24:    return  $v$ 
25:  end if
26:   $\ast id \leftarrow i$                                                          ▷ Return cell index for slow-path
27:  return  $\top$ 
28: end function
29:
30: function DEQ_SLOW( $q, h, cid$ )
31:   $r \leftarrow \&h \rightarrow \text{deq.req}$ 
32:   $r \rightarrow id \leftarrow cid$                                                  ▷ Set request ID
33:   $r \rightarrow \text{state} \leftarrow (1, cid)$                                          ▷ Publish pending request
34:   $\text{HELP\_DEQ}(q, h, h)$                                                      ▷ Help complete own request
35:   $i \leftarrow r \rightarrow \text{state.idx}$                                        ▷ Get index where value found
36:   $c \leftarrow \text{FIND\_CELL}(\&h \rightarrow \text{head}, i)$ 
37:   $v \leftarrow c \rightarrow \text{val}$ 
38:   $\text{ADVANCE\_END\_FOR\_LINEARIZABILITY}(\&q \rightarrow H, i + 1)$                  ▷ Ensure linearizability
39:  return  $(v = \top ? \text{EMPTY} : v)$ 
40: end function

```

bounded completion of every process as each operation completes within $O(N)$ steps, where N is the number of workers, since the helper visits each state array position in fixed order. [39]

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 29 YMC Queue Dequeue Help Operation [40]

```

1: function HELP_DEQ( $q, h, \text{helped}$ )
2:    $r \leftarrow \text{helped} \rightarrow \text{deq.req}$ 
3:    $s \leftarrow r \rightarrow \text{state}$ 
4:    $id \leftarrow r \rightarrow id$ 
5:   if  $\neg s.\text{pending}$  or  $s.idx < id$  then return                                ▷ Request complete or invalid
6:   end if
7:    $ha \leftarrow \text{helped} \rightarrow \text{head}$                                           ▷ Segment pointer for announced cells
8:    $s \leftarrow r \rightarrow \text{state}$                                           ▷ Re-read after getting head
9:    $prior \leftarrow id; i \leftarrow id; cand \leftarrow 0$ 
10:  while true do
11:    for  $hc \leftarrow ha; \neg cand$  and  $s.idx = prior$ ; do                                ▷ Find candidate
12:       $c \leftarrow \text{FIND\_CELL}(\&hc, ++i)$ 
13:       $v \leftarrow \text{HELP\_ENQ}(q, hc, c, i)$ 
14:      if  $v = \text{EMPTY}$  or  $(v \neq \top \text{ and } c \rightarrow \text{deq} = \perp_d)$  then                                ▷ Found candidate
15:         $cand \leftarrow i$ 
16:      else
17:         $s \leftarrow r \rightarrow \text{state}$                                 ▷ Check if announced
18:      end if
19:    end for
20:    if  $cand$  then
21:       $\text{CAS}(\&r \rightarrow \text{state}, (1, prior), (1, cand))$                                 ▷ Try announce candidate
22:       $s \leftarrow r \rightarrow \text{state}$ 
23:    end if
24:    if  $\neg s.\text{pending}$  or  $r \rightarrow id \neq id$  then return                                ▷ Request completed
25:    end if
26:     $c \leftarrow \text{FIND\_CELL}(\&ha, s.idx)$                                 ▷ Get announced cell
27:    if  $c \rightarrow \text{val} = \top$  or  $\text{CAS}(c \rightarrow \text{deq}, \perp_d, r)$  or  $c \rightarrow \text{deq} = r$  then
28:       $\text{CAS}(\&r \rightarrow \text{state}, s, (0, s.idx))$                                 ▷ Complete request
29:      return
30:    end if
31:     $prior \leftarrow s.idx$ 
32:    if  $s.idx \geq i$  then                                ▷ Announced cell is ahead
33:       $cand \leftarrow 0; i \leftarrow s.idx$                                 ▷ Jump forward
34:    end if
35:  end while
36: end function

```

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 30 Feldman-Dechev Queue's Enqueue Operation [35]

```

1: function ENQUEUE(val)
2:   TRYHELPAOTHER
3:   fails  $\leftarrow$  0
4:   while true do
5:     if ISFULL then return false
6:     end if
7:     seqid  $\leftarrow$  NEXTTAILSEQ ▷ FAA on tail
8:     pos  $\leftarrow$  seqid mod capacity
9:     n_node  $\leftarrow$  new ElemNode(seqid, val)
10:    while true do
11:      if fails++ = MAX_FAILS then
12:        op  $\leftarrow$  new EnqueueOp(val)
13:        MAKEANNOUNCEMENT(op)
14:        return op.RESULT
15:      end if
16:      node  $\leftarrow$  buffer[pos].LOAD
17:      if node.op  $\neq$  null then ▷ Operation record
18:        node.op.ASSOCIATE(node, &buffer[pos])
19:        continue
20:      else if ISSKIPPED(node) then ▷ Bitmarked
21:        break ▷ Get new seqid
22:      else if node.seqid < seqid then
23:        BACKOFF
24:        if node = buffer[pos].LOAD then
25:          if ISEMPYNODE(node) then
26:            if buffer[pos].CAS(node, n_node) then
27:              return true
28:            end if
29:          end if
30:          end if
31:        else if node.seqid  $\leq$  seqid and ISEMPYNODE(node) then
32:          if buffer[pos].CAS(node, n_node) then
33:            return true
34:          end if
35:        else ▷ node.seqid > seqid or ElemNode
36:          break ▷ Get new seqid
37:        end if
38:      end while
39:    end while
40: end function

```

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 31 Feldman-Dechev Queue's Dequeue Operation [35]

```

1: function DEQUEUE(&result)
2:   TRYHELPAOTHER
3:   fails ← 0
4:   while true do
5:     if ISEMPY then return false
6:     end if
7:     seqid ← NEXTHEADSEQ ▷ FAA on head
8:     pos ← seqid mod capacity
9:     n_node ← new EmptyNode(seqid + capacity)
10:    while true do
11:      if fails++ = MAX_FAILS then
12:        op ← new DequeueOp
13:        MAKEANNOUNCEMENT(op)
14:        return op.RESULT(result)
15:      end if
16:      node ← buffer[pos].LOAD
17:      if node.op ≠ null then
18:        node.op.ASSOCIATE(node, &buffer[pos])
19:        continue
20:      else if ISSKIPPED(node) and ISEMPYNODE(node) then
21:        if buffer[pos].CAS(node, n_node) then
22:          break
23:        end if
24:      else if seqid > node.seqid then ▷ Delayed element
25:        BACKOFF
26:        if node = buffer[pos].LOAD then
27:          if ISEMPYNODE(node) then
28:            if buffer[pos].CAS(node, n_node) then
29:              break
30:            end if
31:          else
32:            SETSKIPPED(&buffer[pos]) ▷ Bitmark
33:          end if
34:          end if
35:        else if seqid < node.seqid then
36:          break ▷ Get new seqid
37:        else ▷ seqid = node.seqid
38:          if ISELEMNODE(node) then
39:            if ISSKIPPED(node) then
40:              n_node ← SETSKIPPED(n_node)
41:            end if
42:            if buffer[pos].CAS(node, n_node) then
43:              result ← node.value
44:              return true
45:            end if
46:          else ▷ EmptyNode with matching seqid
47:            BACKOFF
48:            if node = buffer[pos].LOAD then
49:              if buffer[pos].CAS(node, n_node) then
50:                break
51:              end if
52:            end if
53:          end if
54:        end if
55:      end while
56:    end while
57: end function

```

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 32 Feldman-Dechev Queue's Helper Functions [35]

```

1: function ENQUEUEOP::ASSOCIATE(node, address)
2:   success  $\leftarrow$  helper.CAS(null, node)
3:   if success or helper.LOAD = node then
4:     node.op.STORE(null) ▷ Remove op reference
5:   else
6:     n_node  $\leftarrow$  new EmptyNode(node.seqid)
7:     if not address.CAS(node, n_node) then
8:       node  $\leftarrow$  SETSKIPPED(node)
9:       if address.LOAD = node then
10:        n_node  $\leftarrow$  SETSKIPPED(n_node)
11:        address.CAS(node, n_node)
12:      end if
13:    end if
14:  end if
15: end function
16:
17: function DEQUEUEOP::ASSOCIATE(node, address)
18:   success  $\leftarrow$  helper.CAS(null, node)
19:   if success or helper.LOAD = node then
20:     n_node  $\leftarrow$  new EmptyNode(node.seqid + capacity)
21:     if not address.CAS(node, n_node) then
22:       node  $\leftarrow$  SETSKIPPED(node)
23:       if address.LOAD = node then
24:        n_node  $\leftarrow$  SETSKIPPED(n_node)
25:        address.CAS(node, n_node)
26:      end if
27:    end if
28:   else
29:     node.op.STORE(null)
30:   end if
31: end function
32:
33: function TRYHELPAOTHER
34:   ▷ Check announcement table and help one operation
35:   helpIdx  $\leftarrow$  thread-local helping index
36:   op  $\leftarrow$  announcementTable[helpIdx]
37:   if op  $\neq$  null and op.INPROGRESS then
38:     if op is EnqueueOp then
39:       WAITFREEENQUEUE(op)
40:     else
41:       WAITFREEDEQUEUE(op)
42:     end if
43:   end if
44:   helpIdx  $\leftarrow$  (helpIdx + 1) mod MAX_THREADS
45: end function

```

5. Analyzing existing Wait-Free Data Structures and Algorithms

Algorithm 33 Verma's Queue Operations [39]

```

1: function DEQUEUE
2:    $id \leftarrow \text{GETTHREADID}$                                 ▷ Get worker's unique ID
3:    $req \leftarrow \text{CREATEREQUEST}(\text{null}, \text{DEQUEUE})$         ▷ Create dequeue request
4:    $stateArr[id] \leftarrow req$                               ▷ Place request in dedicated slot
5:   while  $\neg req.isCompleted$  do                             ▷ Wait for helper to process
6:     wait
7:   end while
8:    $stateArr[id] \leftarrow \text{null}$                             ▷ Clear request from state array
9:   return  $req.e$                                            ▷ Return dequeued element
10: end function
11:
12: function ENQUEUE( $e$ )
13:    $id \leftarrow \text{GETTHREADID}$                                 ▷ Get worker's unique ID
14:    $req \leftarrow \text{CREATEREQUEST}(e, \text{ENQUEUE})$             ▷ Create enqueue request with element
15:    $stateArr[id] \leftarrow req$                               ▷ Place request in dedicated slot
16:   while  $\neg req.isCompleted$  do                             ▷ Wait for helper to process
17:     wait
18:   end while
19:    $stateArr[id] \leftarrow \text{null}$                             ▷ Clear request from state array
20:   return  $\text{true}$ 
21: end function
22:
23: function HELPER
24:    $id \leftarrow 0$                                            ▷ Start at first worker slot
25:   while  $\text{true}$  do                                           ▷ Continuous helper loop
26:      $req \leftarrow stateArr[id]$                              ▷ Check current slot for request
27:     if  $req \neq \text{null} \wedge \neg req.isCompleted$  then        ▷ Found pending request
28:       if  $req.operation = \text{ENQUEUE}$  then
29:          $n \leftarrow \text{new Node}(req.e)$                      ▷ Create new node
30:          $tail.next \leftarrow n$                              ▷ Append to tail
31:          $tail \leftarrow n$                                    ▷ Update tail reference
32:          $size \leftarrow size + 1$ 
33:          $req.isCompleted \leftarrow \text{true}$                   ▷ Mark request complete
34:       else if  $req.operation = \text{DEQUEUE}$  then
35:         if  $head.next = \text{null}$  then                          ▷ Queue is empty
36:            $req.e \leftarrow \text{null}$ 
37:            $req.isCompleted \leftarrow \text{true}$ 
38:         else
39:            $n \leftarrow head.next$                              ▷ Get first element
40:            $head.next \leftarrow n.next$                        ▷ Remove from queue
41:           if  $n.next = \text{null}$  then                             ▷ Queue now empty
42:              $tail \leftarrow head$                              ▷ Reset tail
43:           end if
44:            $req.e \leftarrow n.e$                                ▷ Store dequeued value
45:            $size \leftarrow size - 1$ 
46:            $req.isCompleted \leftarrow \text{true}$ 
47:         end if
48:       end if
49:     end if
50:      $id \leftarrow (id + 1) \bmod workers$                     ▷ Round-robin to next slot
51:   end while
52: end function

```

6. Implementation

7. Benchmarking and Results

8. Conclusion and Future Work

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List of Acronyms

IPC Inter-Process Communication
HRTS Hard Real-Time System
SRTS Soft Real-Time System
RTOS Real-Time Operating System
RTS Real-Time System
CAS Compare and Swap
FIFO First In First Out
LIFO Last In First Out
MPMC Multi Producer Multi Consumer
MPSC Multi Producer Single Consumer
SPMC Single Producer Multi Consumer
SPSC Single Producer Single Consumer
FAA Fetch and Add
FAS Fetch and Store
LL/SC Load-Linked and Store-Conditional
LL Load-Linked
SC Store-Conditional
VL Validate-Link
FFQ FastForward Queue
IFFQ Improved FastForward Queue
BIFFQ Batched Improved FastForward Queue
uSPSC Unbounded Single Producer Single Consumer
dSPSC Dyncamic Single Producer Single Consumer
mSPSC MultiPush Single Producer Single Consumer
BLQ Batched Lamport Queue
LLQ Lazy Lamport Queue
BLQ Batched Lamport Queue

List of Figures

2.1. Race condition between two threads, which write to the same shared variable.	5
2.2. Mutual exclusion between three tasks(processes), which access the same critical section. Multiple processes need to stop working and just wait for other processes to finish their work. See the waiting phase of the processes.	6
2.3. Deadlock between two processes, which wait for each other to release the needed resources.	6

List of Tables

List of Algorithms

1. Michael and Scott's Lock-Free Queue	9
2. Lamports Queue [48]	19
3. Lazy Lamport Queue Operations [48]	20
4. Batched Lamport Queue Operations [48]	21
5. FastForward Queue Operations [49]	22
6. Improved FastForward Queue Operations [48]	23
7. Batched Improved FastForward Queue Operations [48]	23
8. B-Queue with Self-Adaptive Backtracking[47]	25
9. Dynamic List-based SPSC Queue (dSPSC) Operations [45]	26
10. Unbounded Single Producer Single Consumer Operations[45]	27
11. MultiPush Single Producer Single Consumer Operations[45]	28
12. Jayanti's SPSC Queue Operations [44]	29
13. Jayanti's MPSC Queue Operations [44]	30
14. Drescher's Wait-Free MPSC Queue Operations	31
15. Jiffy MPSC Queue Enqueue Operation [43]	32
16. Jiffy MPSC Queue Dequeue Operation [43]	33
17. DQueue MPSC Queue Enqueue Operation [41]	34
18. DQueue MPSC Queue Dequeue Operation [41]	35
19. David's Queue Operations [27]	36
20. Kogan and Petrank's Queue Enqueue Operation [33]	38
21. Kogan and Petrank's Queue Dequeue Operation [33]	39
22. Kogan and Petrank's Queue Dequeue Helping Operations [33]	40
23. Turn Queue Enqueue Operation [37]	41
24. Turn Queue Dequeue Operation [37]	42
25. Turn Queue Dequeue Helper Functions [37]	43
26. YMC Queue Enqueue Operation [40]	44
27. YMC Queue Enqueue Help Operation [40]	45
28. YMC Queue Dequeue Operation [40]	46
29. YMC Queue Dequeue Help Operation [40]	47
30. Feldman-Dechev Queue's Enqueue Operation [35]	48
31. Feldman-Dechev Queue's Dequeue Operation [35]	49
32. Feldman-Dechev Queue's Helper Functions [35]	50
33. Verma's Queue Operations [39]	51

A. Appendix