



# Master's Thesis

# Wait-free synchronisation for inter-process communication in real-time systems

submitted by

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# **Declaration of Originality**

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English title Wait-free synchronisation for inter-process communication in real-time

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temen

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Stuttgart,	July	18,	2025

# Kurzfassung

Vorhersehbare und korrekte Interprozesskommunikation (IPC) ist für Echtzeitsysteme von entscheidender Bedeutung, da Verzögerungen, Unvorhersehbarkeit oder inkonsistente Datenstände zu Instabilität und Ausfällen führen können. Traditionelle Synchronisationsmechanismen verursachen Blockierungen, die zu Prioritätsinversionen und erhöhten Antwortzeiten führen. Um diese Herausforderungen zu bewältigen, bietet die wartefreie Synchronisation eine Alternative, die den Abschluss von, wie der Austausch von Daten zwischen mehreren Prozessen, in einer begrenzten Anzahl von Schritten garantiert und so die Systemreaktionsfähigkeit und -zuverlässigkeit sicherstellt.

Diese Arbeit untersucht die Nutzung von wait-free Datenstrukturen für IPC in Echtzeitsystemen mit Fokus auf deren Implementierung in Rust. Das Eigentumsmodell und die strengen Nebenläufigkeitsgarantien von Rust machen es besonders geeignet für die Entwicklung latenzarmer und hochzuverlässiger Synchronisationsmechanismen. Diese Arbeit analysiert bestehende wait-free Methoden für IPC in Echtzeitsystemen und bewertet ihre Leistung im Vergleich zu herkömmlichen Synchronisationsmethoden.

**Stichwörter:** Echtzeitsysteme, wait-free Sysnchronisation, lock-free Synchronisation, Interprozesskommunikation, rust

# **Abstract**

Predictable and correct Inter-Process Communication (IPC) is essential for Real-Time System (RTS), where delays, unpredictability or inconsistent data can lead to instability and failures. Traditional synchronization mechanisms introduce blocking, leading to priority inversion and increased response times. To overcome these challenges, wait-free synchronization provides an alternative that guarantees operation completion, such as the completion of data exchange between multiple processes, within a bounded number of steps, ensuring system responsiveness and reliability.

This thesis explores the use of wait-free data structures for IPC in RTS, focusing on their implementation in Rust. Rust's ownership model and strict concurrency guarantees make it well-suited for developing low-latency and high-reliability synchronization mechanisms. This work examines existing wait-free techniques for real-time IPC, and evaluates their performance against conventional synchronization methods.

**Keywords:** real-time systems, wait-free synchronization, lock-free synchronization, interprocess communication, rust

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# 1. Introduction

# 1.1. Motivation

In modern manufacturing and automation, control systems must operate under strict timing constraints to function reliably. If a system fails to meet these constraints, unexpected delays can disrupt processes, leading to instability or even hazardous failures in safety-critical environments. For this reason, RTS and low-level programming languages like C or Rust are widely used to ensure predictable execution times.

To achieve these strict timing requirements, many real-time applications involve multiple tasks that must run concurrently and share resources efficiently. Without proper synchronization, problems such as data corruption or race conditions can occur leading to unpredictable behavior. Traditional synchronization methods with locks are commonly used to manage access to shared resources by blocking processes so that only one process at time accesses the shared resource to exchange data in a proper way. However, these blocking mechanisms introduce significant challenges in real-time settings. Since Traditional synchronization methods require processes to wait for resource availability, they can lead to increased response times, potential deadlocks, potential process starvations, and potential priority inversions. These delays are unacceptable in systems that require strict timing guarantees. [1]–[3]

To overcome these limitations, there is an increasing interest in synchronization techniques without any blocking mechanisms. A lock-free algorithm for instance functions withouth any locking mechanism thus no blocking. This guarantees that at least one process completes in a finite number of steps, regardless of contention (multiple processes try to access the same shared resource). This property ensures that at least the system will still work eventhough one process might be lagging. The only problem is that this will not handele starvation since there is no guarantee that every process will finish its task. [4]

While lock-free algorithms represent a significant improvement, wait-free algorithm guarantees that every operation completes in a finite number of steps, regardless of contention. This property ensures system responsiveness and predictability, which are essential for real-time applications. By eliminating blocking and contention-based delays, wait-free synchronization prevents priority inversion and ensures that high-priority tasks execute without interference. [1], [2], [4]

These synchronization mechanisms are particularly important in the context of IPC, which plays a crucial role in RTS. IPC allows processes to exchange data efficiently, but its performance is heavily influenced by the synchronization techniques used. Traditional IPC mechanisms, which often rely on blocking some processes, can introduce significant latency and reduce throughput. Wait-free data structures offer a promising alternative by ensuring that communi-

#### 1. Introduction

cation operations complete within predictable time bounds. However, selecting appropriate wait-free data structures and evaluating their performance in real-time environments remains a challenge. [5]–[8]

To implement these advanced synchronization techniques safely, the choice of programming language is crucial. The Rust programming language provides useful features for implementing real-time synchronization mechanisms. Its ownership model and strict type system prevents data races and enforce safe concurrency. Additionally, Rust offers fine-grained control over system resources, making it a strong candidate for real-time applications that demand both low latency and high reliability. [9], [10]

The concepts and methods introduced here, including RTS, IPC, synchronization techniques and problems, wait-free synchronization, and the rust programming language are explored in greater depth in chapter 2.

# 1.2. Objective

The primary goal of this research is to find the best wait-free data structures that can be used to implement a wait-free synchronization for IPC though shared memory in RTS using Rust. To do so, this study aims to:

- Identify and analyze existing wait-free synchronization techniques for IPC through shared memory for RTS.
- Implement, validate and compare the performance of existing wait-free synchronization mechanisms for IPC through a shared memory for real-time scenarios with each other.
- Choose and analyze which wait-free data structure for IPC through shared memory in a real-time setting using Rust that is best suited.

By addressing these objectives, this work contributes to the field of wait-free synchronization for IPC in RTS by providing a practical solution with rust. The insights gained from this research can help improve the reliability and performance of real-time applications across various domains.

# 1.3. Structure of the Thesis

# 2. Background

To establish a clear foundation for the concepts and definitions introduced throughout this thesis, a fundamental overview of the key topics relevant to this research will be provided. This includes an introduction to RTS, Inter-Process Communication (IPC), and synchronization techniques, with a particular focus on wait-free synchronization. Additionally, the Rust programming language will be examined, as it serves as the primary development environment for this study. Furthermore, existing synchronization methods in RTS will be explored to contextualize the motivation and contributions of this work.

# 2.1. Real-Time Systems

In RTS the correctness of the system does not only depend on the logical results of computations, but also on timing constraints. These systems can be classified into Hard Real-Time System (HRTS) or Soft Real-Time System (SRTS). HRTS have strict timing constraints, and missing a constraint is considered a system failure and may lead to a catastrophic desaster. The system must guarantee that every timing constraint has to be met. An use case would be industrial automation where all the machines and robotic modules have to communicate with each other as quick as possible to ensure no blockage of the manufacturing line. [11]

On the other hand, SRTS try to stick to the timing constraints as much as possible, but missing some timing constraints is not considered a system failure. Infrastructure wise SRTS are similar to HRTS, since it is still considered important to meet these timing constraints. An example would be a multimedia system where it would be considered fine if sometimes frames are dropped to guarantee the video stream. [11]

Sometimes these two systems appear in combination, where some functions have hard real-time constraints and some have soft real-time constraints. Krishna K. gives a good example in his paper where he describes that for the apollo 11 mission some components for the landing processes had soft real-time behavior and the rest still functioned with hard real-time constraints. [11]

Since the workfield of this thesis is within HRTS, the term RTS will be used synonymously with the terminology HRTS.

# 2.2. Inter-Process Communication

Processes used in a RTS also have to share information with each other so the system can function. So some kind of IPC is needed. IPC allows processes to share information with each

other using different kind of methods like a shared memory region, which will be the method used and explained later in this thesis. In general, IPC is needed in all computing systems, because processes often need to work together (e.g. a producer process passes data to a consumer process). Lets take the brake-by-wire technology as example. Brake-by-wire is a technology for driverless cars where some mechanical and hydraulic components from the braking systems are replaced by wires to transmit braking signals, since there is no driver anymore to press on the braking pedal [12]. This of course requires different processes to share information together. In the context of this thesis this kind of communication requires strict timing constraints as stated as before, since any kind of delay or blockage would lead to fatal consequences. [13], [14]

# 2.2.1. Shared Memory

To achieve any kind of information sharing between processes, these processes will need to have access to the same data regularly. With a shared memory segment, multiple processes can have access to the same memory location. So all processes which are part of the IPC can read and write to this common memory space avoiding unnecessary data copys. With that, processes exchange information by directly manipulating memory. This kind of IPC is particular useful for real-time applications, which handle large volumes of data or are required to quickly transfer data between sensors and control tasks. What is also important to know is that the section of the code, that programs these data accesses by different processes is called critical section. The problem with this is that the system somehow has to manage how the processes access the shared memory segment. This is mostly done by using different kind of synchronization techniques. Without any synchronization mechanism race conditions or inconsistent data can occur. [15]

# 2.3. Synchronization

As observed, synchronization is a crucial part of IPC in RTS, especially when processes communicate via shared memory. Communication through shared memory always has a risk of race conditions and data inconsistency if the processes are not properly synchronized. Tratitional synchronization techniques ensure mutual exclusion (only one process at a time uses shared resource) thus avoiding race conditions and ensuring data consistency. Race conditions happen when for example two processes write to the same resource. Lets take a single counter instance with value 17 as a shared resource in a shared memory region. If one has process p1 and one process p2 increments that number, the end result should be 19. But what could happen is that p1 could read the value 17 before p2 increments it and then before p1 increments that value p2 could also read the value 17. Now internally both processes increment that number to 18 and both processes would write 18 to that shared resource. To understand this example more in detail fig. 2.1 visualizes a race condition with threads.

The difference between processes and threads is just, that threads are part of a process which can perform multiple tasks via threads simultaneously within that process. Another

difference that will later be important in this thesis is that processes have their own private memory space, while threads share the memory space of the process they are part of. So naturally a process can not access the memory of another process. Regardless the following concept in fig. 2.1 can be used for processes too. [16]

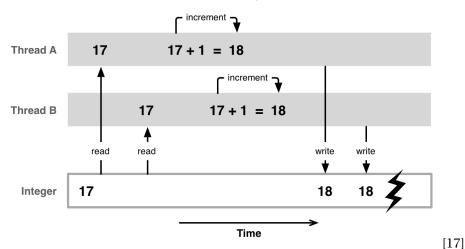


Figure 2.1.: Race condition between two threads, which write to the same shared variable.

#### 2.3.1. Mutual Exclusion

As discussed mutual exclusion does only allow one process or thread to access the shared resource at a time. This includes that if a process p1 already accessed the shared resource x and is still working on it, a second process p2, which trys to access that shared resource x has to wait untill the process p1 finishes its task, where it needs that shared resource x. To achieve this mostly synchronisation techniques based on locks or semaphores are used to block the entry of an process to an already accessed and in use shared resource of an other process. See fig. 2.2 to gain an deeper understanding on how this works. This paper will not go into detail how traditional synchronisation techniques like locks or semaphores work, since for this work it is only important that these kind of methods manage the access of processes to shared resources in shared memorys via some kind of locks. A process will aquire a lock to access a shared resource and will release it when its task is done. Another process trying to access the same resource while its in use has to wait untill the lock is released for that resource.

It is clear that this approach inherently relys on blocking a set of processes. This may lead to several issues, including deadlocks, process starvation, priority inversion, and increased response times. The sequence which process might aquire the lock first to enter the critical section, when multiple processes wait for the access is mostly set by a scheduler. Since wait-free methods explained later in section 2.5 are lock-free, a scheduler is not needed and as a result of that scheduling will not be explained more in detail in this work. [2], [19]

Figure 2.2.: Mutual exclusion between three tasks(processes), which access the same critical section. Multiple processes need to stop working and just wait for other processes to finish their work. See the waiting phase of the processes.

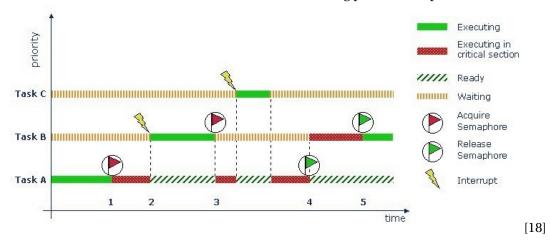
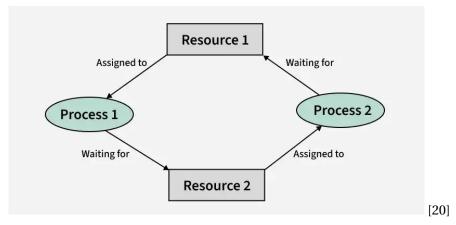


Figure 2.3.: Deadlock between two processes, which wait for each other to release the needed resources.



# **Process Starvation**

Another problem would be, what if when multiple processes try to enter the shared resource one after the other and one process keeps getting outperformed in aquiring a lock to enter the critical section. This process would wait for a indefinite time and will never enter the shared resource. A process that will never access a shared resource that it trys to enter starves out. This usually happens when a synchronization method allows one or more processes to make progress while ignoring a particular process or processes. This mostly happens in environments where some sort of process prioritization exists and processes are classified into low and high priority processes. When there are always high priority processes available and

some low priority processes, it might happen that these low priority processes will never be able to enter the critical section. This is a problem, since these low priority processes might be important for the system too. [21]

#### **Deadlock**

Even worse, what if two or more processes already accessed a resource and now each of them wait that the other process releases the lock for the resource each of them aquired? This results in a situation seen in fig. 2.3 where these processes now indefinetlywait for each other and never terminate. So the resources that these waiting processes hold are also never released and are also never available to other processes maybe needed by other systems. As one can see, this a system into a state which would make no progress any further and would also not respond to any command anymore. [20], [22]

For instance a driverless car with a brake-by-wire system, where processes responsible for braking are in a deadlock, could eventually not brake if needed and a fatal car crash would happen.

# **Priority Inversion**

Now lets say no process starvations or deadlocks happen. What could happen too is that a lower priority process already accessed a shared resource and after that a higher priority process needs to access that specific resource too. If the lower priority process now gets delayed, the higher priority process gets delayed too. This would be called priority inversion now; a low priority process delaying an high priority process. [23]

#### **Increased Response Times**

As demonstrated traditional synchronization is based on mutual exclusion via blocking processes. The result is processes that are waiting, which leads to increased response times of a system. This results in not meeting the timing constraints of a HRTS environment.

# 2.4. Lock-Free Synchronization

Therefore synchronization techniques are required that do not block processes with any kind of locking mechanism. One way could be the implementation of lock-free syschronization techniques. This would allow multiple processes to access the shared resource concurrently. Lock-free synchronization ensures that at least one process will make progress in a finite number of steps. However some processes may be unable to proceed, because lock-free synchronization does not guarantee that all processes will complete their operations in a finite number of steps. This means that starvation or even priority inversion is still possible, as some processes, even high priority processes may be indefinitely delayed by others. There are different kind of mechanisms to achieve this. One way to accomplish lock-freedom for

example is the lock-free technique introduced by Michael and Scott, which is also the basis for some other wait-free algorithms.

#### 2.4.1. Michael and Scott's Lock-Free Queue

Michael and Scott developed an algorithm seen in algorithm 1 using a linked-list as a shared data structure with a enqueue and a dequeue function to introduce lock-freedom. A linked-list is a list containing nodes containing data and a pointer called next which references the next node in the list, which can only be traversed in a single direction. There is also a pointer called head, which references the beginning node of the list and a pointer calles tail, which references the end node of the list. The core concept of the algorithm is the enqueue and dequeue functions beginning at line 7 and 26 in algorithm 1, which are used to add and remove nodes to the shared data structure. When a process trys to add a node to the list, it first creates a new node and sets its next pointer to NULL, see line 8 to 10 of the enque function. Beginning from line 11 to line 23 following happens: The process first checks if the pointer referencing to the next node after the tail node is NULL, see line 15. If it is null it tries to link the new node to the end of the list by using a CAS seen in line 16. This operation atomically compares the current value of the tail pointer with the expected value and, if they match, updates the tail pointer to point to the new node. The tail itself would be updated in line 24. [24]

So lets say 2 processes p1 and p2 untill line 16 executes one after the other. What could happen now is that if p1 executes line 16 before p2, p2 will fail the CAS from line 16. Now if p1 would not execute further thus not finalizing the enqueue with line 24 and p2 retrys the loop until line 15, the condition in line 15 would not be TRUE anymore for p1 and p1 would execute line 19 and 20 to help p2 to finalize its enqueue so other processes can work further with this algorithm. [24]

The dequeue function works analogously, but instead of adding a node to the end of the list it removes a node from the front of the list. And since another process which could not finish its enqueue would cause confusion for other processes in the dequeue function, the process which could not finish its enqueue will also be helped in the dequeue function. [24]

Initialization starts at line 1 in algorithm 1, which is just used to to create dummy nodes when there's no node in the list. This just simplifies the algorithm so that the head and tail pointers are not null. It can be observed that this approach does not need any locks explained in section 2.3. Still this approach has one major problem. If for instance process p1 is trying to enqueue, it can happen that the CAS loop might fail indefinetly if for an indefinite time other processes are always executing line 16 immediately befor p1 could execute line 16. This means that in very high contention scenarios, a process may be delayed indefinetly and starve out. In a HRTS this could lead to violating timing constraints, since the process would not finish his task in the defined timing window, which is unacceptable. This is why a slightly different approach which guerantees that every process will complete its operation in a finite number of steps is in need. [24]

# 2. Background

# Algorithm 1 Michael and Scott's Lock-Free Queue

```
1: function INITIALIZE(Q : pointer to queue_t)
      node = new node()
                                                                                                     ⊳ Allocate a dummy node
3:
      node.next.ptr = \texttt{NULL}
                                                                                             ▶ Make it the only node in the list
4:
      Q.Head = node
                                                                                                   ⊳ Both Head and Tail point
5:
      Q.Tail = node
                                                                                                        ⊳ to this dummy node
6: end function
7: function ENQUEUE(Q : pointer to queue_t, value : data_type)
8:
      node = new node()
                                                                                       > Allocate a new node from the free list
9:
      node.value = value
                                                                                              10:
       node.next.ptr = NULL
                                                                                           ▶ Set next pointer of node to NULL
11:
       loop
                                                                                          ▶ Keep trying until Enqueue is done
12:
          tail = Q.Tail
                                                                                         ▶ Read Tail (pointer + count) together
13:
          next = tail.ptr.next
                                                                                              ⊳ Read next ptr + count together
14:
          if tail == Q.Tail then
                                                                                                   ▶ Are tail & next consistent?
                                                                                                         ▶ Tail is the last node?
15:
             if \ next.ptr == \texttt{NULL} \ then
16:
                 if CAS(\& tail.ptr.next, next, \langle node, next.count + 1 \rangle) then
17:
                    break
                                                                                        ⊳ Link the new node; Enqueue is done
18:
                 end if
19:
                                                                                            > Tail not pointing to the last node
              else
20:
                 CAS(&Q.Tail, tail, (next.ptr, tail.count+1))
                                                                              ▶ Move Tail forward (helping another enqueuer)
21:
              end if
22:
          end if
23:
       end loop
24:
       CAS(\&Q.Tail,\ tail,\ \langle node,\ tail.count+1\rangle)
                                                                             > Final attempt to swing Tail to the inserted node
25: end function
26: function Dequeue(Q:pointer to queue_t, pvalue:pointer to data_type)
27:
                                                                                          ▶ Keep trying until Dequeue is done
28:
          head = Q.Head
29:
          tail = Q.Tail
30:
          next = head.ptr.next
                                                                                                            ▶ Read head->next
31:
          if head == Q.Head then
                                                                                                             ▶ Still consistent?
                                                                                                       ⊳ Empty or Tail behind?
32.
              if head.ptr == tail.ptr then
33:
                 if next.ptr == NULL then
                                                                                                             ▶ Queue is empty
34:
                    return FALSE
35:
                                                                                                 ⊳ Tail is behind, help move it
                 else
36:
                    CAS(\&Q.Tail,\ tail,\ \langle next.ptr,\ tail.count+1\rangle)
37:
                 end if
38:
              else
                                                                                                       ⊳ No need to adjust Tail
39:
                 *pvalue = next.ptr.value
                                                                                                      ▶ Read value before CAS
40:
                 if CAS(\&Q.Head, head, \langle next.ptr, head.count + 1 \rangle) then
41:
                    break
                                                                                                            ▶ Dequeue is done
42:
                 end if
43:
              end if
44:
          end if
45:
       end loop
       free(head.ptr)
                                                                                                > Safe to free old dummy node
       return TRUE
47:
48: end function
                                                             [24]
```

While Michael and Scott's algorithm relies on the CAS primitive, other atomic primitives provide alternative approaches that other algorithms shown later in this thesis use. A overview on the atomic primitives that are used in this thesis context is given in the following section.

#### 2.4.2. Atomic Primitives

Atomic primitives are hardware instructions that conduct a set of steps atomically, meaning with no interruption from other processes [25]. This will be important in the algorithms analyzed later in this thesis, since these primitives are used to implement wait-free synchronization. There are different kind of atomic primitives:

# Load-Linked and Store-Conditional (LL/SC)

Abbreviation of the instructions Load-Linked (LL) and Store-Conditional (SC), which is an operation available on ARM, MIPS and Alpha architecutures usually implied with a Validate-Link (VL) instruction.

- LL(R) returns value of register r
- "SC(R, v) changes the value in register R to v and returns true, if and only if no other process performed a successful SC since the most recent call of LL of the current process. So SC fails if the value of the register has changed since it has been read" [26]
- "VL(R) returns true if no other process performed a successful SC on register R, which allows to test a register value without changing it" [26]

[26]

## Compare and Swap (CAS)

Furthermore to the explanation in section 2.4.1 CAS is an atomic primitive that is supported on "intel x386, x64 and most general purpose architectures with operands that are restricted to pointer size" [26].

• "CAS(R,e,n) returns true and sets the value of R to n if the value in R is e. Otherwise, it returns false." [26]

The problem with CAS furthermore than the issue explained earlier in section 2.4.1 is that it can lead to the ABA problem, which can also occur in wait-free algorithms:

- Process 1 reads value A from a shared variable.
- Process 2 changes the value to B and then back to A.
- Process 1's CAS operation succeeds, because it compares the value A it read earlier with the current value A, even though the value was changed in between.

This is a fundemental limitation of CAS. One solution would be to replace CAS with LL/SC, but that is not possible on x86 processors. So other solutions are needed that are discussed in chapter 6. [26]

# **Double-With Compare and Swap (DWCAS)**

This is a CAS on two neighboring memory locations. [26]

# **Double Compare and Swap (DCAS)**

Sometimes also called CAS2, is a CAS on two independent memory locations. [26]

# **Swap**

Swap is an atomic read-modify-write operation that unconditionally exchanges a value in memory with a new value and returns the old value. Swap(R, v) atomically stores value v into location R and returns the previous value that was in R. This operation always succeeds. [27].

# Fetch and Add (FAA)

This primitive is used to increment "the value of a variable by a given offset and [return] the result. This instruction always succeeds." [26]

# Fetch and Store (FAS)

This atomically stores a value into a variable and returns the previous value. This is similar to CAS, but it does not require a comparison and a retry loop. This is faster then CAS, if conditions before updating do not need to be checked. [28]

# 2.5. Wait-Free Synchronization

Lock-freedom solves the problem off a system getting into a deadlock. But this is not enough, in a fully automated car for example it is undesirable that any process does not complete its task, since that could mean that some processes that are responsible for braking would not finish their work in a worst case scenario. And such an occasion where the car would need to brake a fatal car crash would be the outcome. Consequently a solution is necessary where every process finishes their task in a finite number of steps instead of just one process. So something is needed which builds upon such mechanisms and expand them. This is exactly what wait-free synchronization is. It guarantees that every process will complete its operation in a finite number of steps, regardless of contention. This means that even process starvation is by definition not possible anymore. So by definition starvation cannot happen anymore. Also priority inversion is eliminated too, because processes do not have to wait for other processes anymore. This ensures system responsiveness and predictability thus the ability to define strict timing constraints to meet these vital timing constraints, which are essential for HRTS applications. But even wait-free algorithms introduce one problem. Wait-free algorithms are in most cases slower than their lock-free counterpart in execution. A solution to this problem was the fast-path / slow path method by Kogan and Petrank, where operations on a data

structure is first done with a bounded lock-free operation, and when failed a slower wait-free operation will substitute the failed lock-free operation [4]. This will be analysed more in detail in chapter 5.

# 2.6. Rust Programming Language

The question now is which programming language suits best for this kind of research. Since a fast communication between the processes is compulsory to meet all HRTS timing constraints, the C programming language would be a good choice. C provides low-hardware control and therefore also allows the implementation of fast low-latency communication. What is also important and necessary for a RTS is, that C does not have an automatic garbage collecter, which gets active and stops all processes from working to clean up allocated but no longer used memory space. Because of that all Real-Time Operating System (RTOS) are written in C. The main problem with C is that it does not provide any kind of memory safety, since C implements memory operations that are prone to buffer overflows or control-flow attacks. In the industry around 70% of vulnarabilities happen because of memory safety issues. If the real-time application would run on an isolated system with no internet connection, this would not be a problem. But in modern automation, where systems need to be connected to the internet for data exchange, such systems would be prone to security attacks. RTS nowadays is an integral part in various connected devices, including critical fields such as health or transportation. Conclusively it is extremely important that the security of such devices is guaranteed. With the rust programming language the problems of memory safety features are gone. The difference to C is that it can be as fast as C with the possibility to support low-level control and high-level programming features, while providing memory safety features in a realtime setting. The memory safety aspect is achieved by an ownership concept that controls how memory is handled in programs. This is strictly checked and therefore the executable program has guaranteed memory safety. In the model every value has a single owner represented by a variable. The owner is in charge of the lifetime and deallocation of that value. Rust will automatically free the memory associated with that value, when the owner goes out of scope. This behaviour is automatically done by using the memory reference feature provided by rust. Creating such references is also called borrowing. This allows the usage of these values without transferring the ownership. These references have its own lifetime, which can be explicitly defined by the programmer or implicitly inferred by rusts compiler. This ensures that the references are valid and do not exist longer as needed. Hence this also can play a role in lock-freedom, which is needed for wait-free synchronization, since shared resources can be shared with this ownership concept. Additionally rust is a type-safe language, which can be helpfull during implementation to avoid bugs and errors, since this also needs to be avoided in a RTS. As seen rust is a good choice for implementing wait-free synchronization mechanisms for IPC in RTS. [9], [29].

Further mechanisms on how with rust different kind of common memory safety issues are solved will not be discussed in detail, as that would go beyond the scope of this thesis. It is

# 2. Background

only important to know the basics on how rust is a type-safe and memory-safe programming language, to understand why rust is used for this work.

# 3. Related Work

The early foundations regarding wait-freedom was done indirectly by Leslie Lamport in 1977 and 1983 [30], [31]. While these works did not directly address or formally define wait-freedom, they laid the groundwork for lock-freedom, which Maurice Herlihy later extended to wait-freedom [1].

In 1977, Lamport he showed how one writer and multiple readers can share data without the need of locks, eliminating writer delays due to reader interference. It works by using atomic byte-wise read and write operations. The writer will atomically write a value to a memory location from right to left, while the reader uses the same memory location to read the value from left to right. So even if the writer is still in the process of writing, the reader will not block the writer while reading (and vice versa) and still see a correct snapshot of the data. To prevent a reader process from saving inconsistent data (for example while the writer process writes), the writer process will tag each update by incrementing a start counter before an end counter after writing. Readers take the start counter, read the data, and compare if the start counter matches the end counter. If they do not match it means the data is inconsistent and the reader will retry reading the data until it gets a consistent value. To understand this better imagine a date with the format DD/MM/YYYY, where every digit is written as one byte from right to left and read from left to write. This solves the problem of contention between readers and a single writer. If multiple writers are involved, the writers still have to be mutually exclusive, which means that they have to use locks to block each other to prevent inconsistency (So with multiple writers this algorithm cannot be lock-free anymore). [30]

In 1983 Leslie Lamport then gave a formal method to write and prove the correctness of any concurrent module in a simple and modular way independent of the used data structure, which he refers to as modules. These modules consist of three components:

- state functions, which are abstract variables describing the module's state.
- initial conditions, which are predicates on the state functions.
- properties, which are a mix of safety and liveness requirements.

Safety requirements define what must never happen (e.g., a queue must never drop an element), while liveness requirements define what must eventually happen (e.g., a non-empty queue must eventually allow dequeueing). He also defines the usage of action sets and environment constraints, which seperate the module action from the environments (e.g., the program where the data structure runs in). For example, a First In First Out (FIFO) queue specification would include:

#### 3. Related Work

- State Functions: queue contents, operation parameters, return values.
- Initial Conditions: queue starts empty.
- Safety Condition: queue maintains FIFO ordering.
- Liveness Condition: dequeue operation will eventually return a value.

This systematic methodology to prove the correctness of concurrent data structures laid the necessary groundwork for later developments too. [31]

Building on methodologys to prove concurrent data structure correctness Herlihy and Wing provided linearizability as a correctness condition for concurrent objects, which is a guarantee that every operation performed appears to take effect instantaneously at some point between the call and return of the operation [32]. This correctness condition was then used to formalize wait-freedom in 1991 [1]. In the latter work Herlihy proved that any sequential data structure can be transformed into a wait-free concurrent data structure [1]. A wait-free data structure must satisfy following three constraints:

- Linearizability: operations take effect instantaneously at some point between the call and return of the operation.
- Bounded steps: operations end in a finite number of steps.
- Independence: operations finish regardless of other processes' exection (for later understrandin: a process waiting for another process for a maximum number of time and then returning an error if that time is exceeded would still be considered wait-free, since it will finish regardless of the other process).

From this perspective the algorithm provided by Lamport in 1977 is already wait-free, even though the term was not yet defined at that time. [1], [32]

Herlihys universal construction and principles (or work that builds upon his work) appear conceptually throughout all of these wait-free algorithms [4], [27], [28], [33]–[49]. [1]

Kogan and Petrank later invented a method called fast-path slow-path, were first usually a lock-free method (the fast-path) is used to try to complete an operation, since lock-free algorithms are usually faster than wait-free algorithms. These lock-free paths are bounded by a maximum number of steps and if the operation does not complete within that bound the algorithm tries to complete the operation using a wait-free method (the slow-path). So in cases where the fast-path succeeds often without switching to the slow path, the algorithm in general completes in a shorter time then a pure wait-free algorithm. This method is used by two algorithms with one of them having a great performance advantage, which will be demonstrated later in this thesis [38], [40]. [4]

# 4. Methodology

To achieve the goal that is defined in section 1.2, first all wait-free data structures that could be used for IPC through shared memory in HRTS need to be identified. To find all existing wait-free datastructure a method was used that is more known from mapping studys or literature reviews. Multiple python scripts were implemented to do this [50]. A web scraper script was written to scrape over google scholar with the following querys:

- · "wait-free queue"
- "wait-free" ("mpmc" OR "multi-producer multi-consumer" OR "multi-writer multi-reader" OR "many-to-many") "queue"
- "wait-free" ("mpsc" OR "multi-producer single-consumer" OR "single-writer multi-reader" OR "many-to-one") "queue"
- "wait-free" ("spsc" OR "single-producer single-consumer" OR "single-writer single-reader" OR "one-to-one") "queue"
- "wait-free" ("spmc" OR "single-producer multi-consumer" OR "multi-writer single-reader" OR "one-to-many") "queue"

In google scholar a whitespace is considered as an AND. The rest is interpreted as read. With this approach i got a list of 1324 papers. The papers were then written into a csv file split into query, rank (number of paper), title, year, authors, venue, citations, abstract snippet, full\_abstract and url with ";" as an delimiter. To extract all of this the information in google scholar was extracted and then for the full abstract the scraper went onto the source url and extracted the abstract there. If the url was a direct pdf link, a pdf reader was used to find the abstract. If an abstract was not extractable (some source site which was not considered or other problems), "ABSTRACT\_NOT\_FOUND" was written instead or if the paper was accessible the full paper was written instead into that cell. Because a lot of scientific web pages will put ceptchas if continuously requests are made undetected\_chromedriver was importet and used as the web driver. It is an enhanced version of chromedriver which bypasses anti bot detections. After that I also implemented a regex analyzer to analyze the abstracts of the found papers on the words "lockfree", "waitfree", and "obstructionfree" and also again without a hyphon inbetween these words. If these keywords were not found in the abstract or the abstract contained the flag "ABSTRACT\_NOT\_FOUND" the paper was removed from the csv. This left 475 papers that contained at least one of these words in their abstract. After that the duplicates were removed by the algorithm, which left 325 papers. The duplicates were

#### 4. Methodology

removed by checking the url of the paper. Now what was left had to be manually analyzed to see if the paper was relevant for the topic. Since libre office and microsoft excel has a limit of 32.767 charachters per cell a abstract splitter had to be build to split the abstract into multiple cells. Analyzing was done by reading the paper and checking if the paper was developing an wait-free fifo queue. While dooing that also backward and forward search was done to even find more papers. Papers where only included, if and only if:

- All three of Herlihys contraints were met, that we listed in chapter 3.
- The algorithms could be implemented on x86 architecture using rust, since this is the architecture and programming language that is used and available for this work.
- The algorithm runs in an acceptable time to even benchmark it for an IPC via a shared memory use-case.

In the end 17 papers were included from the 325 papers and 3 more paper were included by backward and forward search of the papers that were included. The papers were then split into 4 contention categories:

- MPMC queues [33], [35], [37]–[40]
- MPSC queues [28], [41], [43], [44]
- SPMC queues [27]
- SPSC queues [31], [45], [47]–[49]

Now the wait-free fifo queues had to be compared performance wise. Some papers were just improvements of other papers so only the improved version was used for the comparison. Some other papers showed multiple ways of implementing a wait-free fifo datastructure. In the end 6 MPMC queues, 4 MPSC queues, 1 SPMC queue and 11 SPSC queues were included into this work.

# 5. Analyzing existing Wait-Free Data Structures and Algorithms

After finding and identifying existing wait-free data structures and algorithms, they need to be analyzed like said in section 1.2 to meet the primary objective of this work. That is exactly what this chapter will be about.

# 5.1. Optimal Wait-Free Data Structure

Before analyzing the algorithms, first it needs to be set what data strucuture to use for the implementation of wait-free synchronization for IPC. M. Herlihy showed that every sequential data structure can be made wait-free [1]. So it is important to choose the optimal data structure for our use. Considering that the reason of this work is to optimize modern manufacturing and automation, some form of correct data flow order is as well necessary for correct work flow for instance in an modern manufacturing line or more critical in a driverless car. Hence an already natural fit like FIFO queues. Natural because in such queues a producer process can enqueue messages and the consumer process can dequeue messages sequentially. This models real-world data flows (sensor readings, commands, network packets), which are inherently sequential. Consequently with such queues the order of the data flow is preversed without the need of implementing additional functionalities. In contrast, data structures like stacks, sets, or maps do not maintain this kind of arrival order and moreover add semantics like Last In First Out (LIFO) order or key-value pairs, which are in most cases not desired or even unnecessary. This would bring in the need of additional functions to just get rid of undesired side effects. Furthermore in a queue only two operations exist, an enqueue and an dequeue operation. All the other data structures introduce more operations and therefore more complexity and therefore more performance overhead. The less operations exist, the less complex the implementation will be. Because of these advantages and also because of the fact that in most publications in the wait-free domain queues are beeing used, limiting this thesis to queues only is reasonable. [43]

# 5.2. Wait-Free Algorithms

With the appropriate data structure established, an important consideration is the selection of suitable algorithms. In chapter 4 4 different contention categories are defined. Which kind of algorithm going to be used will be decided contention based. Since all of them have different

complexity in runtime, it is important to choose the right contention category for the right use case to save resources and have faster execution times to meet the timing constraints of HRTS. In modern manufacturing and automation devices are used which can run multiple applications on a single device. This could mean that every application running on one device could be a producer and a consumer to each other (MPMC) and also maybe some single application of all applications running on one device produces data for just a single other consuming application (SPSC). And maybe some single application is a producer for multiple consuming applications (SPMC) and multiple applications are producers of a single consuming application (MPSC). So it can be that all cases can occur in just one device. This means that all the different cases of contention have to be considered. In the following the different cases and their algorithms will be discussed. Moreover they will be implemented and their performance tested via a benchmarked (how fast an algorithm can produce and consume items concurrently). Subsequently from each category the best algorithm will be chosen and their performance will be compared with each other to Identify, if 4 different categories are necessary. The reason for that is, that for instance the best performed MPMC algorithm could outperform all other algorithms even for their contention category, since a MPMC approach can cover all contention cases. The goal with this approach is to have as little overhead as possible, since an algorithm explicitly implemented for a MPMC use case could have extreme overhead for a SPSC case. The implementation will be discussed in chapter 6 and the results of the performance readings will be discussed in chapter 7. The following subsections will give an overview of the different contention categories and their algorithms found. The subsections will also shortly describe how the enqueue and dequeue in these algorithms work. Given that all algorithms found are about inter-thread communication and not IPC, the following explanation of the specific algorithms will include the terminology of threads to be precise about the papers. In chapter 6 it will be elaborated how these thread based algorithms are adapted to IPC in Rust. Other minor Rust-specific deviations from the following algorithms (different types required by Rust's safety model, additional memory fences, etc.) can be seen in the GitHub repository accompanying this thesis [50]. These are not detailed here as such explanations would provide limited value to the topic of this work, and while a comprehensive analysis would be relevant, it would require more extensive exploration than is feasible within the scope of this work.

# 5.2.1. Single Producer Single Consumer (SPSC)

This is the most simple form of IPC. In SPSC there is nearly no contention from other processes, because only one producer and one consumer is working. The only contention is between the consumer and producer. This leads to the producer and consumer finish in a bounded number of steps without special synchronisation techniques like helping or atomic primitives. The only concern is that the data the consumer reads is consistent. Different approaches were testet in different paper, that will be seen here. Since Batched Lamport Queue (BLQ), Lazy Lamport Queue (LLQ), Batched Improved FastForward Queue (BIFFQ) and Improved

FastForward Queue (IFFQ) are from the same paper, explanations and variables are shared between these algorithms to avoid redundancy:

# Lamport's Circular Buffer Queue

Uses a circular array with two shared indices for synchronization, based on the algorithm originally proposed by Leslie Lamport in 1983 [31] and shown here in algorithm 2 following Maffione et al.'s version [48]. The producer first checks if the queue is full (reached capacity N) in line 2, which requires reading the consumer's read index. If the queue is not full, it writes the input data to the slot at position write & mask in line 5, where the bitwise AND operation wraps the index around when it reaches the array end. The producer then increments write to signal that the written data is available in line 7. The consumer mirrors this behavior by checking if the queue is empty in line 12, which requires reading the producer's write index. If the queue is not empty, the consumer reads data from the slot at position read & mask in line 16, using the same modulo arithmetic through bitwise AND, and incrementing its read index to signal that the slot is available in line 17. This wraparound behavior creates the circular buffer structure, allowing the fixed-size array to be reused continuously. Unfortunately each operation requires accessing both shared indices plus the data slot, causing up to three cache misses per item when the queue moves between nearly empty and nearly full states. According to U. Drepper [51], cache misses occur when different processes access variables that reside on the same cache line. A cache miss is when the requested data is not in the local CPU core's cache and must be fetched from another core's cache or the main memory, with the cache coherence protocol ensuring memory consistency across all cores. Drepper showed that performance can degrade by 390%, 734%, and 1,147% for 2, 3, and 4 threads respectively. This happens because cache lines, the 64-byte blocks (on x86 architectures) that move between CPU caches, ping-pong between the producer's and consumer's cores as they take turns accessing the same memory locations.

# Lazy Lamport Queue (LLQ)

Reduces the described cache misses by postponing index reads until necessary, as shown in algorithm 3. Additionally to Lamports original enqueue function the producer maintains a local read\_shadow copy and only updates it when running out of known free slots in lines 2 to 6. Similarly, the consumer uses write\_shadow to avoid repeatedly checking for new items. Additionally, LLQ keeps K slots (where K is slots per cache line) permanently empty, preventing producer and consumer from touching the same cache line when the queue is full. This works well when one thread is faster than the other, reducing worst-case misses from 3 to about 2 per item. [48]

# **Batched Lamport Queue (BLQ)**

Extends LLQ with explicit batching to further reduce synchronization costs, as detailed in algorithm 4. The producer accumulates items using private write\_priv in line 11, filling

```
Algorithm 2 Lamports Queue [48]
1: function LQ_ENQUEUE(q, e)
2:
      if q.write - q.read = N then
                                                                                                              ⊳ Check if full
3:
         \boldsymbol{return} - 1
                                                                                                                 ⊳ No space
4:
      end if
5:
      q.slots[q.write \land q.mask] \leftarrow e
6:
      store_release_barrier()
7:
      q.write \leftarrow q.write + 1
8:
      return 0
9: end function
10.
11: function LQ_DEQUEUE(q)
12:
       if q.read = q.write then
                                                                                                           ▶ Check if empty
13:
          return NULL_ELEM
                                                                                                             ▶ Queue empty
14:
       end if
15:
       load_acquire_barrier()
       e \leftarrow q.slots[q.read \land q.mask]
17:
       q.read \leftarrow q.read + 1
18:
       return e
19: end function
                                                            [48]
```

# Algorithm 3 LLQ Operations [48]

```
1: function llq_enqueue(q, e)
      if q.write - q.read\_shadow = N - K then
                                                                                                              ▶ Lazy load check
3:
          q.read\_shadow \leftarrow q.read
                                                                                                              \triangleright Update shadow
4:
          if q.write - q.read\_shadow = N - K then
5:
             return -1
                                                                                                                     ⊳ No space
6:
          end if
7:
      end if
8:
      q.slots[q.write \land q.mask] \leftarrow e
9:
      store_release_barrier()
       q.write \leftarrow q.write + 1
10:
       return 0
12: end function
13:
14: function LLQ_DEQUEUE(q)
       if q.read = q.write\_shadow then
                                                                                                              ▶ Lazy load check
16:
           q.write\_shadow \leftarrow q.write
                                                                                                              ▶ Update shadow
17:
           if q.read = q.write\_shadow then
18:
             return NULL_ELEM
19:
          end if
20:
       end if
21:
       load_acquire_barrier()
22:
       e \leftarrow q.slots[q.read \land q.mask]
23:
       q.read \leftarrow q.read + 1
       \mathbf{return}\; e
25: end function
```

slots without updating the shared write index. Only the function blq\_enqueue\_publish in lines 15 to 18 makes the batch visible by advancing write in line 17. The consumer works symmetrically, using read\_priv in line 32 for local progress before updating read in line 40. With typical batch sizes like B=32, synchronization overhead is amortized across operations, reducing cache misses. However, the application using this queue design must explicitly

call the publish functions even with partial batches to avoid unbounded latency, because items remain invisible to the consumer until published. This design particularly benefits applications that naturally process data in batches, such as network packet processing, where batch boundaries are well-defined. [48]

```
Algorithm 4 BLQ Operations [48]
1: function BLO ENQUEUE SPACE(q, needed)
      space \leftarrow N - K - (q.write\_priv - q.read\_shadow)
3:
      if space < needed then
4:
         q.read\_shadow \leftarrow q.read
                                                                                                           ▶ Update shadow
5:
         space \leftarrow N - K - (q.write\_priv - q.read\_shadow)
      end if
7:
      return space
8: end function
10: function BLQ_ENQUEUE_LOCAL(q, e)
11:
       q.slots[q.write\_priv \land q.mask] \leftarrow e
12:
       q.write\_priv \leftarrow q.write\_priv + 1
13: end function
14:
15: function blq_enqueue_publish(q)
16:
     store_release_barrier()
17:
       q.write \leftarrow q.write\_priv
18:\ \mathbf{end}\ \mathbf{function}
19:
20: function blq_dequeue_space(q)
21:
       available \leftarrow q.write\_shadow - q.read\_priv
22:
       if available = 0 then
23:
          q.write\_shadow \leftarrow q.write
                                                                                                           ▶ Update shadow
24:
          available \leftarrow q.write\_shadow - q.read\_priv
25:
       end if
26:
       return available
27: end function
29: function blq_dequeue_local(q)
30:
      load_acquire_barrier()
31:
       e \leftarrow q.slots[q.read\_priv \land q.mask]
       q.read\_priv \leftarrow q.read\_priv + 1
33:
       return e
34: end function
35:
36: function BLQ_DEQUEUE_PUBLISH(q)
       q.read \leftarrow q.read\_priv
38: end function
```

# FastForward Queue (FFQ)

Synchronization by embedding control information directly within the data slots, eliminating separate shared indices shown in algorithm 5. Unlike Lamport's queue which requires checking both head and tail indices, FFQs producer simply examines if the next slot contains NULL in line 2 before writing. When the slot is empty (NULL), the producer writes the data directly and advances its private head index in lines 5 and 6. The consumer follows a similar pattern by reading from the current slot position in line 11 and then checks in line 12 data is present

(non-NULL). If not NULL it retrieves the value and writes NULL to mark the slot empty in line 15. Then it advances its private tail index in the line after that. This couples synchronization control and the actual data, reducing shared memory accesses from three (head, tail, buffer) to just one (buffer slot). Each thread maintains its own private index that never needs synchronization. The producer tracks where to write next through head, while the consumer tracks where to read next through tail. The NULL value serves dual purpose as both an empty indicator and the synchronization mechanism. While this approach reduces memory barriers and cache misses significantly, it still has the ping-pong effect when the queue has few elements, causing the producer and consumer to operate on the same cache line. [49]

```
Algorithm 5 FFQ Operations [49]
1: function FFQ_ENQUEUE(q, data)
     if q.buffer[q.head] \neq NULL then
        return EWOULDBLOCK
4:
      end if
5:
      q.buffer[q.head] \leftarrow data
6:
      q.head \leftarrow NEXT(q.head)
7:
      return 0
8: end function
10: function FFQ_DEQUEUE(q)
11:
     data \leftarrow q.buffer[q.tail]
      if data = NULL then
13:
          return EWOULDBLOCK
14:
       end if
      q.buffer[q.tail] \leftarrow \texttt{NULL}
15:
      q.tail \leftarrow NEXT(q.tail)
17:
      return data
18: end function
```

# Improved FastForward Queue (IFFQ)

Prevents cache conflicts through spatial separation using a look-ahead mechanism shown in algorithm 6. The producer checks if a slot H positions ahead (4 cache lines ahead) is empty before proceeding in line 4, ensuring it works far ahead of the consumer. This check happens only once every H items when write reaches limit in line 2. The consumer delays clearing slots through the function iffq\_dequeue\_publish seen in lines 23 to 28, maintaining separation between producer and consumer regions. With 2H permanently unused slots as a buffer zone, producer and consumer operate on different cache lines, reducing cache misses even more. [48]

# **Batched Improved FastForward Queue (BIFFQ)**

Addresses IFFQs weakness when the queue is nearly empty by adding producer-side buffering, as shown in algorithm 7. Items first accumulate in a thread-local buffer seen in line 10, then the function biffq\_enqueue\_publish beginning at line 15 writes them to the queue in

#### Algorithm 6 IFFQ Operations [48] 1: **function** IFFQ\_ENQUEUE(q, e) **if** q.write = q.limit **then** ⊳ Check limit 3: $next\_limit \leftarrow q.limit + H$ if $q.slots[next\_limit \land q.mask] \neq \texttt{NULL\_ELEM}$ then 4: 5: ▶ No space 6: end if 7: $q.limit \leftarrow next\_limit$ ▶ Free partition 8: end if 9: $q.slots[q.write \land q.mask] \leftarrow e$ 10. $q.write \leftarrow q.write + 1$ 11: return 0 12: end function 13: 14: **function** IFFQ\_DEQUEUE\_LOCAL(*q*) 15: $e \leftarrow q.slots[q.read \land q.mask]$ 16: if e = NULL ELEM then 17: return NULL ELEM 18: 19: $q.read \leftarrow q.read + 1$ return e21: end function 23: **function** IFFQ\_DEQUEUE\_PUBLISH(q) 24: **while** $q.clear \neq next\_clear(q.read)$ **do** 25: $q.slots[q.clear \land q.mask] \leftarrow \texttt{NULL\_ELEM}$ 26: $a.clear \leftarrow a.clear + 1$ 27: end while 28: end function

a rapid burst in lines 15 to 18. Also like in BLQ the application using this queue must call this function explicitly to avoid deadlocks. This behavior creates an intended race condition, which is beneficial if all writes complete before the consumer notices. The cache line stays with the producer to avoid ping-pong effects. The consumer side remains unchanged from IFFQ. While theoretical worst-case behavior is similar to IFFQ, practical measurements show significant improvement when the queue operates near empty, making BIFFQ effective across all operating conditions. [48]

#### **B-Queue**

Addresses the deadlock issues inherent in batching approaches through a self-adaptive backtracking mechanism that dynamically adjusts to production rates shown in algorithm 8. The producer maintains local head and batch\_head pointers, probing BATCH\_SIZE positions ahead when needed in line 3. The consumer's adaptive backtracking algorithm from lines 27 to 41 maintains a batch\_history variable that records successful batch sizes from previous operations. When searching for data, it starts from this historical value rather than always beginning at BATCH\_SIZE, significantly reducing latency when the producer operates slowly. If in line 29 to 31 the recorded size is below BATCH\_MAX, the algorithm optimistically increments batch\_size by INCREMENT (typically one cache line) to probe for higher throughput when the producer accelerates. The binary search then proceeds from this adaptive starting

#### **Algorithm 7** BIFFQ Operations [48] 1: **function** BIFFQ\_WSPACE(q, needed) 2: $space \leftarrow q.limit - q.write$ 3: if space < needed then 4: return space ⊳ Force limit update 5: end if 6: return space 7: end function 8: 9: **function** BIFFQ\_ENQUEUE\_LOCAL(q, e) 10. $q.buf[q.buffered] \leftarrow e$ 11: $q.buffered \leftarrow q.buffered + 1$ 12: end function 13: 14: **function** $BIFFQ_ENQUEUE_PUBLISH(q)$ for $i \leftarrow 0$ to q.buffered-1 do 15: 16: $q.slots[q.write \land q.mask] \leftarrow q.buf[i]$ ▶ Fast burst 17: $q.write \leftarrow q.write + 1$ 18: end for $q.buffered \leftarrow 0$ 19: $q.limit \leftarrow q.write + H$ ▶ Update limit 21: end function

point, halving the batch size until finding available data or reaching zero. In the dequeue function, the consumer uses this computed value to update batch\_tail in line 15. This eliminates the need for manual parameter adjustment or manual calling of a publish function while maintaining cache line separation and preventing deadlocks. [47]

# **Dyncamic Single Producer Single Consumer (dSPSC)**

A dynamically space allocating queue using a linked list with node caching to reduce memory allocation overhead, as shown in algorithm 9. Unlike bounded circular buffers like the Lamport Queue, dSPSC dynamically allocates nodes as needed, making it suitable for scenarios where queue size cannot be predetermined. The implementation maintains a dummy head node head to ensure producer and consumer always operate on different nodes to prevent cache line conflicts. The SPSC\_Buffer (line 4, which is just a Lamport Queue) serves as a node cache to recycle deallocated nodes to minimize malloc or free calls. When pushing, the producer first checks the cache for a recycled node in line 8, falling back to malloc only when the cache is empty in line 11. After setting the data and next pointer, a memory barrier ensures correct ordering before linking the new node into the list in lines 20 to 22. The consumer checks for available data by testing if the dummy head points to a data node in line 28. Upon a successful pop, the consumer advances the head pointer so the data node becomes the new dummy and then attempts to cache the old dummy for reuse in lines 30 to 33. While node caching improves performance, reading and referencing the pointer so often causes memory accesses spread over multiple cache lines. As shown earlier this leads to cache misses. [45]

# Algorithm 8 B-Queue with Self-Adaptive Backtracking [47]

```
1: function BQUEUE_ENQUEUE(q, e)
       if q.head = q.batch\_head then
                                                                                                                    ⊳ No empty slots
3:
          if q.buffer[(q.head + BATCH\_SIZE) \mod q.size] \neq \texttt{NULL} then
4:
              return -1
                                                                                                                        ⊳ Queue full
5:
          end if
6:
          q.batch\_head \leftarrow q.head + BATCH\_SIZE
7:
8:
       q.buffer[q.head \bmod q.size] \leftarrow e
9:
       q.head \leftarrow q.head + 1
10:
       return ()
11: end function
12:
13: function BQUEUE_DEQUEUE(q)
       if q.tail = q.batch\_tail then
                                                                                                                     ⊳ No filled slots
           batch\_tail \leftarrow ADAPTIVE\_BACKTRACK(q)
15:
16:
           if batch_tail = -1 then
              return NULL
17:
18:
           end if
19:
           q.batch\_tail \leftarrow batch\_tail
20:
21:
       e \leftarrow q.buffer[q.tail \bmod q.size]
22:
       q.buffer[q.tail \mod q.size] \leftarrow \texttt{NULL}
       q.tail \leftarrow q.tail + 1
23:
24:
       return e
25: end function
26:
27: function ADAPTIVE_BACKTRACK(q)
28:
       batch\_size \leftarrow q.batch\_history
                                                                                                        ⊳ Start from historical value
29:
       if batch_size < BATCH_MAX then
30:
          batch\_size \leftarrow batch\_size + \texttt{INCREMENT}
                                                                                                                   ▶ Try larger batch
31:
32.
       while batch\_size > 0 do
33:
           batch\_tail \leftarrow q.tail + batch\_size
34:
           if q.buffer[(batch\_tail-1) \mod q.size] \neq \text{NULL} then
35:
                                                                                                        > Remember successful size
               q.batch\_history \leftarrow batch\_size
36:
              {\bf return}\; batch\_tail
37:
           end if
38:
           batch\_size \leftarrow batch\_size/2
                                                                                                                     ⊳ Binary search
39:
       end while
40:
       return -1
41: end function
```

# **Unbounded Single Producer Single Consumer (uSPSC)**

An unbounded queue that links multiple Lamport Queues to combine the cache efficiency of Lamports circular buffer queues with unlimited capacity, as shown in algorithm 10. Unlike dSPSC which uses scattered linked list nodes, uSPSC maintains spatial locality by keeping data in contiguous circular buffers while only linking the buffers themselves. The implementation uses two pointers <code>buf\_w</code> pointing to the producer's current write buffer and <code>buf\_r</code> pointing to the consumer's current read buffer. When pushing, the producer checks if the current buffer is full in line 2, and if so, requests a new buffer from the pool via <code>next\_w()</code> in line 3 before writing the data to <code>buf\_w</code>. The consumer first checks if its current buffer is empty in line 10. If empty, it determines whether the queue is truly empty by comparing read and write

#### Algorithm 9 dSPSC Operations [45] 1: **struct** Node { void\* data; Node\* next; } 2: Node\* head; ⊳ Points to dummy node 3: Node\* tail; ⊳ Points to last data node 4: SPSC\_Buffer cache; > Bounded cache for node recycling 6: function ALLOCNODE 7: Node\* $n \leftarrow \text{NULL}$ 8: if cache.pop(&n) then ▶ Try cache first 9: return n10. end if 11: $n \leftarrow (\text{Node*}) \text{malloc(sizeof(Node))}$ 12: return n 13: end function 14: 15: function PUSH(void\* data) Node\* $n \leftarrow allocnode()$ ⊳ Get node from cache or malloc 17: *n*->data ← data 18: n->next $\leftarrow$ NULL 19: WMB() ▶ Write Memory Barrier 20: tail->next $\leftarrow n$ ▶ Link new node 21. ▶ Update tail pointer tail $\leftarrow n$ 22: return true 23: end function 24: 25: **function** POP(void\*\* data) 26: **if** head->next $\neq$ NULL **then** ⊳ Check if data available 27: Node\* $n \leftarrow \text{head}$ ⊳ Save current dummy 28: \*data ← (head->next)->data ▶ Extract data 29: $head \leftarrow head -> next$ ▶ Advance to next node 30: **if**!cache.push(n) **then** > Try to recycle old dummy 31: free(n)⊳ Free if cache full end if 32. 33: return true 34: end if 35: return false ▶ Queue empty 36: end function

buffer pointers in line 11. If they point to the same buffer, no more data exists. Otherwise, after rechecking emptiness to prevent race conditions in line 14, the consumer obtains the next buffer via next\_r() and releases the empty buffer back to the pool for recycling in lines 15 to 17. This double-check prevents data loss when the producer writes to the current buffer between the initial emptiness check and the buffer comparison. By reusing entire buffers rather than individual nodes, uSPSC matches bounded SPSC queues cache behavior while providing unbounded capacity. [45]

# MultiPush Single Producer Single Consumer (mSPSC)

Reduces the ping-pong effect in Lamport's circular buffer by batching multiple elements before insertion, as shown in algorithm 11. Instead of writing elements one by one directly to the shared buffer, mSPSC accumulates items in a thread-local array batch. The producer stores incoming data in the batch array in lines 2 and 3, and when the batch reaches BATCH\_SIZE in

#### **Algorithm 10** uSPSC Operations [45] 1: **function** USPSC\_PUSH(q, data) 2: if $q.buf_w.full()$ then ⊳ Current buffer full 3: $q.buf\_w \leftarrow q.pool.next\_w()$ ⊳ Get new buffer 4: end if 5: $q.buf\_w.push(data)$ 6: return tirue 7: end function 8: 9: **function** USPSC\_POP(q, data) 10: if $q.buf\_r.empty()$ then 11: **if** $q.buf_r = q.buf_w$ **then** ▶ Same buffer? 12: return false ▶ Queue truly empty 13: end if 14: if $q.buf\_r.empty()$ then ▶ Recheck after comparison 15: $tmp \leftarrow q.pool.next\_r()$ 16: $q.pool.release(q.buf\_r)$ ▶ Recycle buffer 17: $q.buf_r \leftarrow tmp$ 18: end if 19: end if $return \ q.buf\_r.pop(data)$ 21: end function

line 4, the producer calls multipush to insert all elements at once in line 5. The multipush function first calculates the final write position in line 11 and checks if sufficient space exists in line 12. As seen in lines 15 to 17 elements are written in reverse order, starting from the furthest position and working backwards. This backward insertion creates distance between the write pointer and where the consumer is reading, ensuring they operate on different cache lines. A write memory barrier in line 18 ensures all batch writes are visible before updating the write pointer in line 19. The batch counter resets in line 20, preparing for the next batch. The flush function in lines 24 to 29 allows forcing partial batch writes when needed. While adding an extra copy per element from batch to buffer, the improved cache behavior from reduced traffic from the coherence protocol compensates for this overhead. [45]

#### Jayanti SPSC Queue

A queue specifically for composability in larger MPSC structures, as shown in algorithm 12. Unlike traditional SPSC queues, this implementation includes readFront operations that enables observation of the queue's head element, crucial for the MPSC construction. The queue maintains a linked list where the tail always points to a dummy node. When enqueueing, the producer converts the current dummy node into a data node by writing the value in line 4. Then the producer links a new dummy node in line 5 and updates the tail pointer in line 6. This ensures the consumer never sees a partially constructed node. The Help variable in line 15 stores the dequeued value, allowing concurrent readFront\_e operations to obtain valid data even after the original node is removed. The announcement mechanism prevents use-after-free errors. When the producer calls readFront\_e, it writes the front node pointer to Announce in line 32, signaling the consumer not to immediately free that node. If the consumer encounters an announced node in line 17, it defers the node's deallocation to

# **Algorithm 11** mSPSC Operations[45]

```
1: function MSPSC_PUSH(q, data)
      q.batch[q.count] \leftarrow data
3:
      q.count \leftarrow q.count + 1
4:
      if q.count = BATCH_SIZE then
5:
         return MULTIPUSH(q, q.batch, q.count)
6:
      end if
7:
      return true
8: end function
10: function MULTIPUSH(q, batch, len)
       last \leftarrow q.write + len - 1
                                                                                                      ▶ Calculate end position
12:
       if q.slots[last \mod q.size] \neq NULL then
13:
          return false
                                                                                                          ▶ Not enough space
14:
       end if
15:
       for i \leftarrow len - 1 downto 0 do
                                                                                                               ▶ Reverse order
16:
          q.slots[(q.write+i) \mod q.size] \leftarrow batch[i]
17:
       end for
18:
                                                                                                     ⊳ Ensure all writes visible
       WMB()
19:
       q.write \leftarrow (last + 1) \mod q.size
       q.count \leftarrow 0
                                                                                                        ▶ Reset batch counter
21:
       return true
22: end function
23:
24: function FLUSH(q)
25:
       if q.count > 0 then
26:
          return MULTIPUSH(q, q.batch, q.count)
27:
       end if
28:
       return tirue
29: end function
```

FreeLater in lines 18 to 20, ensuring the producer can safely read the node's value. The separate readFront\_d operation in lines 41 to 47 is simpler since the consumer knows no concurrent dequeue can occur. This coordination enables wait-free progress while supporting the propagation mechanism, the process of pushing each local queue's minimum timestamp up through a binary tree to maintain a global minimum, needed for the logarithmic-time MPSC operations as seen in section 5.2.2. [44]

# **5.2.2. Multi Producer Single Consumer (MPSC)**

This is a bit more complex to implement than the SPSC case. Multiple producers can enqueue items at the same time while a single consumer dequeues items. This includes implementing other strategies then just adding some memory barriers, such as helping and atomic primitives to maintain wait-freedom and consistency between the producers. There are multiple approaches that are available from different papers to achieve this:

# Jayanti MPSC Queue

Achieves logarithmic time complexity by distributing the global queue across n local SPSC queues implemented like in section 5.2.1 and organized under a binary tree, as shown in

# Algorithm 12 Jayanti's SPSC Queue Operations [44]

```
1: function Enqueue(q, v)
      newNode \leftarrow new Node()
                                                                                                    ▶ Create new dummy node
3:
      tmp \leftarrow q.Last
                                                                                                     ⊳ Get current dummy tail
4:
      tmp.val \leftarrow v
                                                                                               > Convert dummy to data node
5:
      tmp.next \leftarrow newNode
                                                                                                           ▶ Link new dummy
6:
      q.Last \leftarrow newNode
                                                                                                          ▶ Update tail pointer
7: end function
8:
9: function DEQUEUE(q)
10:
       tmp \leftarrow q.First
                                                                                                               ⊳ Get head node
       if tmp = q.Last then
11:
                                                                                                      ▶ Only dummy remains?
12:
          return \perp
                                                                                                               ▶ Queue empty
13:
       end if
14:
       retval \leftarrow tmp.val
                                                                                                                  ⊳ Read value
15:
       q.Help \leftarrow retval
                                                                                                  ▶ Help concurrent readFront
16:
       q.First \leftarrow tmp.next
                                                                                                         ▶ Remove from queue
                                                                                               ▶ Was announced by readFront?
17:
       if tmp = q.Announce then
18:
          tmp' \leftarrow q.FreeLater
                                                                                                       ⊳ Get old deferred node
19:
          q.FreeLater \leftarrow tmp
                                                                                                          ▶ Defer current node
20:
          free(tmp')
                                                                                                      ⊳ Free old deferred node
21:
       else
22:
          free(tmp)
                                                                                                            ▶ Free immediately
23:
       end if
24:
       return retval
25: end function
26:
27: function READFRONT_E(q)
                                                                                                          ▶ Called by enqueuer
28:
       tmp \leftarrow q.First
                                                                                                           ▶ Read head pointer
29:
       if tmp = q.Last then
                                                                                                               ⊳ Queue empty?
30:
          return 🕹
31:
       end if
32.
       q.Announce \leftarrow tmp
                                                                                                    > Announce to prevent free
33:
       if tmp \neq q. First then
                                                                                             ► Head changed (was dequeued)?
34:
          retval \leftarrow q.Help
                                                                                                            ▶ Use helped value
35:
36:
                                                                                                                ⊳ Read directly
          retval \leftarrow tmp.val
37:
       end if
38:
       \mathbf{return}\ retval
39: end function
40:
41: function READFRONT_D(q)
                                                                                                          ▶ Called by dequeuer
42:
       tmp \leftarrow q.First
43:
       if tmp = q.Last then
44:
          return \perp
45:
       end if
       return tmp.val
                                                                                               ⊳ Safe - no concurrent dequeue
47: end function
```

algorithm 13. Each producer owns a dedicated local queue, eliminating producer-producer contention. When enqueueing, a producer obtains a global timestamp via LL/SC on a shared counter in lines 2 and 3, creating a unique ordering even if the SC fails, since some other producer must have incremented it. If LL/SC is not supported on system architecture it can be replaced with versioned CAS. The producer then inserts a timestamped pair into its local queue in line 4 and propagates this timestamp up the tree in line 5. The tree maintains the invariant

that each internal node holds the minimum timestamp of its subtree. The propagate function in lines 18 to 26 walks from leaf to root, calling refresh at each node. The double refresh pattern in lines 22 to 24 ensures correctness. if the first refresh fails, another process updated the node. if the second refresh also fails, that process must have read the updated children values and installed the correct minimum. The refresh function uses LL/SC in lines 28 to 33 to atomically update a node with the minimum of its children's timestamps. The consumer reads the root to find the producer with the earliest element in line 9 and then dequeues from that local queue in line 13 and propagates any changes in line 14. This design transforms the O(n) scan of all queues into  $O(\log n)$  tree traversals, while the space complexity remains O(n+m) where m is the number of queued items. [44]

```
Algorithm 13 Jayanti's MPSC Queue Operations [44]
1: function ENQUEUE(q, p, v)
      tok \leftarrow LL(q.counter)
                                                                                                         ▶ Read timestamp
3:
     SC(q.counter, tok + 1)
                                                                                                           ▶ Try increment
     enqueue2(q.Q[p], (v, (tok, p)))

ightharpoonup Add timestamp to local queue
     PROPAGATE(q, q.Q[p])
5:
6: end function
8: function DEQUEUE(q, p)
9:
      [t, id] \leftarrow \text{read}(q.T.root)
                                                                                                       ▶ Get min producer
10:
       if id = \bot then
11:
          return \perp
12:
       end if
13:
       ret \leftarrow \text{dequeue2}(q.Q[id])
14:
       PROPAGATE(q, q.Q[id])
15:
       return ret.val
16: end function
17:
18: function PROPAGATE(q, localQueue)
19:
       currentNode \leftarrow localQueue
20:
       repeat
21:
          currentNode \leftarrow parent(currentNode)
22:
          if \negREFRESH(q, currentNode) then
                                                                                                                 ▶ First try
23:
             REFRESH(q, currentNode)
                                                                                              ▶ Second ensures correctness
24:
          end if
25:
       until currentNode = q.T.root
26: end function
27:
28: function refresh(q, node)
29:
                                                                                                          ▶ Load-link node
      LL(node)
       stamps \leftarrow \text{read timestamps from } node's children
30:
31.
       minT \leftarrow minimum timestamp from stamps
                                                                                                        return SC(node, minT)
33: end function
```

#### **Drescher Queue**

Uses a linked list with a dummy head node to eliminate producer contention, as shown in algorithm 14. Unlike traditional MPSC queues that require retry loops, producers complete enqueue in exactly three steps. First the producers clear the item's next pointer in line 6, then

it atomically swaps the tail pointer via FAS in line 7 and further links the previous tail to the new item in line 8. The FAS operation ensures multiple producers can enqueue concurrently without interference. The consumer reads the head and its next pointer in lines 12 and 13 and afterwards advances the head in line 17 if the queue is non-empty. Subsequently the consumer handles the special case of the dummy node in lines 18 to 24. When the dummy is dequeued, it's immediately re-enqueued in line 19 to maintain the invariant that the queue always contains at least one element to prevent complex empty queue conditions. The guard integration through VOUCH and CLEAR ensures all orders are enqueued before guard acquisition in line 2 of VOUCH. The guard is released before checking for pending orders in line 11 of CLEAR, preventing lost updates. This ordering guarantees that either the current sequencer or a new thread will process all pending orders, achieves the wait-free progress guarantees with constant time enqueue operations. [28]

```
Algorithm 14 Drescher's Wait-Free MPSC Queue Operations
1: dummy.next \leftarrow 0
2: head \leftarrow \&dummy
3: tail \leftarrow \&dummy
5: procedure Enqueue(guard, item)
6:
     item.next \leftarrow 0
                                                                                                     ▶ Clear next pointer
      prev \leftarrow FAS(guard.tail, item)
                                                                                                       ▶ Atomic swap tail
8:
      prev.next \leftarrow item
                                                                                                      ▶ Link to new item
9: end procedure
10:
11: function Dequeue(guard)
12:
      item ← guard.head
       next \leftarrow guard.head.next
14:
      if next = 0 then
                                                                                                         ▶ Empty queue?
15:
          return \perp
16:
       end if
17:
       guard.head \leftarrow next
18:
       if item = \&dummy then
                                                                                                   ▶ Dequeued dummy?
19:
          ENQUEUE(guard, item)
                                                                                                   ▶ Re-enqueue dummy
20:
          if guard.head.next = 0 then
                                                                                                            ⊳ Still empty?
21:
             return 1
22:
23:
          guard.head \leftarrow guard.head.next
24:
          return next
25:
       end if
       return item
27: end function
```

#### **Jiffy Queue**

A queue that uses a linked list of fixed-size arrays (buffers), as shown in function <code>ENQUEUE</code> (data) in algorithm 15 and in <code>DEQUEUE</code> function in algorithm 16. Unlike other linked-list queues that allocate nodes per element, Jiffy amortizes allocation overhead by storing multiple elements in each buffer. Producers use <code>FAA</code> on a global tail counter to reserve slots in line 2 of <code>enqueue</code>, eliminating producer-producer synchronization except during

buffer allocation. Each buffer contains an array of nodes with data and a 2-bit isSet flag indicating the node's state: empty (uninitialized), set (data written), or handled (already dequeued). When the current buffer fills, producers allocate new buffers and link them via CAS in lines 7 and 8. To reduce allocation contention, the producer obtaining the second slot in each buffer proactively allocates the next buffer in lines 21 to 26, ensuring smooth transitions between buffers. The consumer maintains a local head pointer and scans for the first non-handled element in lines 3 to 9 of dequeue. To ensure linearizability when producers stall: if the head element is still empty, the consumer scans forward to find a set element in line 20, then rescans backward in line 24 to ensure no earlier element became set during the scan. This prevents violating FIFO ordering when a slow producer completes after a faster one. The consumer can "fold" the queue by deleting fully-handled buffers in the middle of the list during scans, to not use to much memory even with stalled producers. This achieves wait-free progress guarantees with minimal synchronization. Producers only need one FAA per enqueue, while the consumer performs no atomic operations at all. [43]

```
Algorithm 15 Jiffy MPSC Queue Enqueue Operation [43]
1: function ENQUEUE(data)
      location \leftarrow FAA(tail, 1)
                                                                                                    ⊳ Reserve global index
      tempTail \leftarrow tailOfQueue
3:
4:
      while location is in unallocated buffer do
                                                                                                      ▶ Beyond last buffer?
5:
         if tempTail.next = NULL then
6:
             newArr \leftarrow new BufferList()
7:
             if CAS(tempTail.next, NULL, newArr) then
8:
               CAS(tailOf Queue, tempTail, newArr)
9:
10:
                                                                                              > Another thread succeeded
                delete newArr
11:
             end if
          end if
12:
13:
          tempTail \leftarrow tailOfQueue
                                                                                                     ⊳ Move to new buffer
14:
       end while
15:
       while location not in tempTail's buffer do
                                                                                               ▶ Location in earlier buffer?
16:
          tempTail \leftarrow tempTail.prev
                                                                                                         ▶ Walk backward
17:
       end while
18:
       index \leftarrow location - tempTail.startIndex
                                                                                                      ▶ Buffer-local index
19:
       tempTail.buffer[index].data \leftarrow data
20:
       tempTail.buffer[index].isSet \leftarrow SET
                                                                                                          ▶ Mark as ready
21:
       if index = 1 AND tempTail is last buffer then
                                                                                                           ▶ Second slot?
22:
                                                                                                     ▶ Proactive allocation
          newArr \leftarrow new BufferList()
23.
          if NOT CAS(tempTail.next, NULL, newArr) then
24:
25:
          end if
       end if
27: end function
```

#### **DQueue**

Combines local buffering with a segmented shared queue to minimize synchronization overhead, as shown in function <code>ENQUEUE</code> (data) in algorithm 17 and in <code>DEQUEUE</code> function in algorithm 18. DQueue reduces contention by having producers accumulate enqueue requests

#### Algorithm 16 Jiffy MPSC Queue Dequeue Operation [43]

```
1: function DEQUEUE
      n \leftarrow headOfQueue.buffer[head]
3:
      while n.isSet = HANDLED do
                                                                                                         ▶ Skip dequeued items
4:
         head \leftarrow head + 1
5:
         if end of buffer then
6:
             move to next buffer and delete current
7:
8:
         n \leftarrow headOfQueue.buffer[head]
9:
      end while
10:
       if queue is empty then
11:
          return \perp
12:
       end if
13:
       if n.isSet = SET then
                                                                                                           ▶ Ready to dequeue?
14:
          data \leftarrow n.data
15:
          n.isSet \leftarrow \text{HANDLED}
16:
          head \leftarrow head + 1
17:
          return data
       end if
18:
19:
       if n.isSet = EMPTY then
                                                                                                        ▶ Incomplete enqueue?
20:
          tempN \leftarrow Scan(find first SET element)
21:
          if no SET element found then
22:
             return \perp
23:
          end if
24:
          Rescan(n, tempN)
                                                                                                ⊳ Check for newly set elements
25:
          data \leftarrow tempN.data
26:
          tempN.isSet \leftarrow \texttt{HANDLED}
27:
          return data
28:
       end if
29: end function
30:
31: function SCAN
                                                                                                       ⊳ Find first SET element
32.
       for each element from current position do
33:
          if element.isSet = SET then
34:
             return element
35:
          end if
36:
          if entire buffer is HANDLED then
37:
              fold queue (delete buffer)
38:
          end if
39:
       end for
40:
       return NULL
41: end function
42:
43: function RESCAN(start, end)
                                                                                                > Check for ordering violations
44:
       for each element from start to end do
45:
          if element.isSet = SET then
46:
              end \leftarrow \text{element}
                                                                                                   ⊳ Found earlier SET element
47:
              restart scan from start
48:
          end if
49:
       end for
50: end function
```

in thread-local ring buffers before writing them to the shared queue in batches. Producers reserve slots using FAA on a global tail counter in line 7 of enqueue, storing both the data and the reserved cell index (cid) in their local buffer. Each producer maintains a buffer of Request structures with capacity L, using local\_head and local\_tail pointers to track buffer

state. When the buffer fills, detected in line 2, the producer calls dump\_local\_buffer to flush all buffered requests. During flushing, producers write values directly to their reserved cells in line 15 without synchronization, as each cell is exclusively owned by the reserving producer. Producers cache their current segment pointer (pseq) and update it when moving to newer segments in line 18. The find segment function traverses the segment list and allocates new segments on-demand using CAS in line 29. To maintain wait-freedom when producers stall, the consumer encountering an empty cell that should contain data, checked in line 7 of dequeue, distinguishes between an empty queue in line 8 and a pending enqueue by checking if head equals tail. For pending enqueues, help\_enqueue in line 11 iterates through all producers' local buffers from lines 19 to 31, writing any buffered values to their reserved cells in line 28. The helper skips producers that have already moved past the target segment in line 24, avoiding unnecessary work. This ensures minimal synchronization with only one FAA per enqueue and no atomics for dequeue and improves cache locality via batched writes that reduce false sharing and writes that directly write to known cell locations without searching. The consumer's dequeue operation has its linearization point at line 14 where it increments the head pointer. [41]

# **5.2.3. Single Producer Multi Consumer (SPMC)**

This case is trickier to implement, since now multiple reading workers have to be synchronized to read consistently without any unwanted behavior. Multiple producers was simpler, since making producers write specific data each is not so hard. In this case every consumer has to be synchronized so that when one item is consumed by a consumer, it cannot be consumed again from another and also the ordering has to be kept. That is most probably also the reason only one algorithm for this contention category was found. The approach to achieve this in a wait-free manner is the following:

#### **David Queue**

Uses a two-dimensional array of Swap objects to handle the race condition where consumers overtake the producer, as shown in algorithm 19. David's queue allows the producer to detect when it has been overtaken and adapt by jumping to a fresh row. The producer maintains two persistent local variables, a enq\_row (current row) and tail (next column to write) variable. During enqueue, the producer swaps the value into ITEMS [enq\_row, tail] in line 10 and checks if the retrieved value is  $\top$ , indicating a consumer already accessed this cell. If so, the producer jumps to the next row in lines 12 to 15, writing the value to the new row and updating the shared ROW register. This jump mechanism ensures that enqueued values are never lost. Consumers read the active row from ROW in line 22 of dequeue, then increment using Fetch and Increment (Like FAA, but incrementing) on HEAD [deq\_row] in line 23 to reserve a unique column index. They swap  $\top$  into the reserved cell in line 24, retrieving either the enqueued value or  $\bot$  (empty). The use of swap instead of plain registers is important, because it allows the producer to detect consumer interference (by finding  $\top$ ) and consumers

#### **Algorithm 17** DQueue MPSC Queue Enqueue Operation [41]

```
1: function ENQUEUE(Producer p, data)
       if next(p.local\_tail) = p.local\_head then
3:
           dump_local_buffer(p)
                                                                                                                       ⊳ Flush when full
4:
       end if
5:
       tail \leftarrow p.local\_tail
6:
       p.local\_buffer[tail].val \leftarrow data
       p.local\_buffer[tail].cid \leftarrow FAA(q.tail, 1)
                                                                                                                           ▶ Reserve slot
8:
       p.local\_tail \leftarrow next(p.local\_tail)
9: end function
10.
11: function DUMP_LOCAL_BUFFER(Producer p)
        while p.local\_head \neq p.local\_tail do
13:
           r \leftarrow p.local\_buffer[p.local\_head]
14:
           seg \leftarrow \text{find\_segment}(p.pseg, r.cid)
15:
           seg.cell[r.cid \mod N] \leftarrow r.val
                                                                                                                         ▶ Write in batch
16:
            p.local\_head \leftarrow \text{next}(p.local\_head)
17:
           if p.pseg \neq seg then
18:
                                                                                                               > Update segment cache
               p.pseg \leftarrow seg
19:
           end if
        end while
21: end function
23: function FIND_SEGMENT(Segment * sp, int cid)
24:
        curr \leftarrow sp
25:
        for i \leftarrow curr \rightarrow id; i < cid/N; i++ do
26:
           next \leftarrow curr \rightarrow next
27:
           if next = NULL then
28:
               new \leftarrow \mathsf{new\_segment}(i+1)
29:
               if CAS(curr \rightarrow next, NULL, new) then
30:
                  next \leftarrow new
31:
                                                                                                           > Another thread succeeded
32.
                  delete new
33:
               end if
34:
            end if
35:
            curr \leftarrow next
36:
        end for
37:
        return curr
38: end function
```

to mark cells as processed. Each cell in ITEMS is accessed at most once by an enqueue and once by a dequeue operation. The algorithm achieves 3-bounded wait-freedom with constant time operations. The producer completes in at most 3 steps (regular enqueue: 1 step, jump enqueue: 3 steps), while consumers always complete in exactly 3 steps. [27]

#### 5.2.4. Multi Producer Multi Consumer (MPMC)

Finally a look into the MPMC case can be made. Here we need to think about synchronize producer-producer contention, consumer-consumer contention and producer consumer contention. This includes helping methods for the producer and consumer and different atomic primitives. Multiple approaches are available to achieve this:

#### Algorithm 18 DQueue MPSC Queue Dequeue Operation [41]

```
1: function DEQUEUE(Consumer c)
       seg \leftarrow \text{find\_segment}(c.cseg, q.head)
3:
       if c.cseg \neq seg then
4:
                                                                                                            > Update segment cache
          c.cseg \leftarrow seg
5:
       end if
6:
       cell \leftarrow seg.cell[q.head \mod N]
       if cell = \bot then
7:
                                                                                                                         ⊳ Empty cell?
8:
          \textbf{if } q.head = q.tail \textbf{ then}
9:
              return EMPTY
10:
           else
11:
              help_enqueue()
                                                                                                            ▶ Help stalled producers
12:
           end if
13:
        end if
14:
        q.head \leftarrow q.head + 1
                                                                                                                ▶ Linearization point
15:
        return cell
16: end function
17:
18: function HELP_ENQUEUE
19:
       for each Producer p in system do
           for each Request r in p.local_buffer do
               pos \leftarrow r.cid
21:
22:
               val \leftarrow r.val
23:
               seg \leftarrow find\_segment(p.pseg, pos)
24:
              if seg.id > pos/N then
25:
                  break
                                                                                                              > Producer moved past
26:
               end if
27:
               if seg.cell[pos \mod N] = \bot then
28:
                  seg.cell[pos \mod N] \leftarrow val
                                                                                                                          ⊳ Help write
29:
30:
           end for
        end for
32: end function
```

#### Kogan and Petranks queue

Uses a priority-based helping scheme with Michael and Scott's lock-free queue from algorithm 1 as the foundation to achieve wait-freedom, as shown in algorithms 20 to 22. Threads complete operations in bounded steps by helping slower peers. Each thread chooses a monotonically increasing phase number in line 2 of ENQUEUE in algorithm 20 and line 2 of DEQUEUE of algorithm 21, then records operation details in a shared state array in line 3. The helping mechanism in HELP from lines 15 to 26 in algorithm 22 ensures all operations with phases ≤ the current phase complete. Threads traverse the state array and invoke HELP\_ENQ or HELP\_DEQ based on pending operations in lines 19 to 23 of algorithm 22. For enqueue, threads utilize the tail update like in Michael and Scott by first appending the node via CAS in line 15 of HELP\_ENQ in algorithm 20, then finally helping by updating the tail in line 36 of HELP\_FINISH\_ENQ. The three-step scheme ensures exactly-once execution by first appending a node to list in line 15 then clear the pending flag in line 35 of HELP\_FINISH\_ENQ, and finally update the tail pointer in line 36. For dequeue, threads write their ID to the deqTid field of the head node in line 41 of HELP\_DEQ in algorithm 21 to "lock" it logically. The consumer then updates the pending flag in line 9 of HELP\_FINISH\_DEQ in algorithm 22

#### Algorithm 19 David's Queue Operations [27]

```
1: Shared variables:
2: HEAD: array of Fetch&Increment objects, initially 0
3: ITEMS: 2D array of Swap objects, initially \perp
4: ROW: Register, initially 0
6: Enqueuer's persistent local variables:
7: enq_row \leftarrow 0, tail \leftarrow 0
8:
9: procedure ENQUEUE(x)
                                                                                                               ⊳ For enqueuer E only
       val \leftarrow \text{Swap}(ITEMS[enq\_row, tail], x)
10.
                                                                                                                    ▶ Try to enqueue
       if val = \top then
                                                                                                            ▶ Dequeuer overtook us?
12:
           enq\_row \leftarrow enq\_row + 1
                                                                                                                  ▶ Jump to next row
13:
           tail \leftarrow 0
14:
           Swap(ITEMS[enq\_row, tail], x)
                                                                                                                   ▶ Write to new row
15:
           Write(ROW, enq_row)
                                                                                                                   ⊳ Publish new row
16:
        end if
17:
       tail \leftarrow tail + 1
18:
       return OK
19: end procedure
21: function Dequeue
                                                                                                          \triangleright For dequeuers D_1, ..., D_n
22:
       deq\_row \leftarrow Read(ROW)
                                                                                                                     ▶ Get active row
       head \leftarrow \text{Fetch} \& \text{Increment}(HEAD[deq\_row])
23:
                                                                                                                   ▶ Reserve column
24:
       val \leftarrow \text{Swap}(ITEMS[deq\_row, head], \top)
                                                                                                                          ⊳ Get value
25:
       if val = \bot then
                                                                                                                        ⊳ Empty cell?
26:
           return \varepsilon
                                                                                                                 ▶ Queue was empty
27:
28:
                                                                                                           ▶ Return dequeued value
           return val
29:
        end if
30: end function
```

and advances head in line 10. Special handling for empty queues occurs in lines 20 to 25 of HELP\_DEQ of algorithm 21, where threads update state with null to indicate emptiness. The phase selection using MAXPHASE in lines 41 to 50 in algorithm 20 ensures threads help all concurrent operations before returning, preventing starvation. This achieves wait-free progress with O(n) steps per operation where n is the number of threads. [33]

#### **Turn Queue**

Uses a novel turn-based consensus mechanism to achieve wait-freedom without requiring FAA instructions. As shown in algorithms 23 to 25, the queue maintains two arrays: enqueuers for enqueue requests and deqself/deqhelp for dequeue operations. Each thread has a unique index used as its thread ID (enqTid or deqTid). For the producers in algorithm 23, threads publish their intent by storing a node pointer in enqueuers [myIdx] in line 6 of the function ENQUEUE. The consensus mechanism uses the enqTid of the tail node to determine whose turn is next. Threads scan the enqueuers array starting from position (tail->enqTid + 1) % maxThreads in line 20, helping the first non-null request they find. This creates a circular turn order ensuring fairness. The algorithm guarantees that after publishing a request, at most maxThreads-1 other nodes will be enqueued first, achieving

# Algorithm 20 Kogan and Petrank's Queue Enqueue Operation [33]

```
1: function Enqueue(value)
      phase \leftarrow MaxPhase + 1
                                                                                                                ⊳ Choose phase
3:
      state[tid] \leftarrow \texttt{OpDesc}(phase, true, true, \texttt{Node}(value, tid))
      HELP(phase)
                                                                                                          ⊳ Help all ops ≤ phase
      HELP_FINISH_ENQ
                                                                                                          ⊳ Ensure tail updated
6: end function
7:
8: procedure Help\_Enq(tid, phase)
      while IsStillPending(tid, phase) do
          last \leftarrow tail
10:
          next \leftarrow last.next
11:
                                                                                                                 ⊳ Validate read
12:
          if last = tail then
13:
             if next = null then
                                                                                                                 ⊳ Can append?
14:
                 if IsStillPending(tid, phase) then
15:
                    if CAS(last.next, null, state[tid].node) then
16:
                       Help_Finish_Enq
17:
                       return
18:
                    end if
19:
                 end if
20:
                                                                                                       ▶ Help pending enqueue
21:
                 HELP_FINISH_ENQ
22:
              end if
23:
          end if
24:
       end while
25: end procedure
26:
27: procedure Help_Finish_Enq
28:
       last \leftarrow tail
29:
       next \leftarrow last.next
30:
      if next \neq null then
31:
          tid \leftarrow next.enqTid
                                                                                                       > Thread that owns node
32.
          desc \leftarrow state[tid]
33:
          if last = tail and state[tid].node = next then
34:
              newDesc \leftarrow \texttt{OpDesc}(state[tid].phase, false, true, next)
35:
              CAS(state[tid], desc, newDesc)
                                                                                                                ▶ Clear pending
36:
                                                                                                                    ⊳ Update tail
              CAS(tail, last, next)
37:
          end if
38:
       end if
39: end procedure
40:
41: function MaxPhase
42:
       max \leftarrow -1
43:
       for i \leftarrow 0 to NUM\_THREADS-1 do
44:
          phase \leftarrow state[i].phase
45:
          if phase > max then
46:
             max \leftarrow phase
          end if
47:
48:
       end for
49:
       return max
50: end function
```

wait-free bounded progress. The enqueue operation protects the tail pointer using hazard pointers in line 12 of the ENQUEUE function, then clears any completed request from the tail's position in lines 15 to 18. It searches for the next request to help in lines 19 to 26, attempting to append the found node via CAS in line 23. Finally, it advances the tail pointer if a

#### Algorithm 21 Kogan and Petrank's Queue Dequeue Operation [33]

```
1: function Dequeue
      phase \leftarrow MaxPhase + 1
3:
      state[tid] \leftarrow \texttt{OpDesc}(phase, true, false, null)
4:
      HELP(phase)
5:
      HELP_FINISH_DEQ
      node \leftarrow state[tid].node
6:
7:
      if node = null then
8:
         throw EmptyException
9:
      end if
10:
      return node.next.value
11: end function
12:
13: procedure HELP_DEQ(tid, phase)
       while IsStillPending(tid, phase) do
          first \leftarrow head
15:
16:
           last \leftarrow tail
17:
          next \leftarrow first.next
18:
          if first = head then
                                                                                                                 ⊳ Validate read
19:
              if first = last then
                                                                                                       ▶ Queue might be empty
20:
                 if next = null then
                                                                                                            ➤ Confirmed empty
21:
                    desc \leftarrow state[tid]
22:
                    if last = tail and IsStillPending(tid, phase) then
23:
                       newDesc \leftarrow \texttt{OpDesc}(state[tid].phase, false, false, null)
24:
                       CAS(state[tid], desc, newDesc)
25:
                    end if
26:
                 else
                    HELP_FINISH_ENQ
27:
                                                                                                                ▶ Help enqueue
28:
                 end if
29:
              else
                                                                                                            ▶ Queue not empty
30:
                 desc \leftarrow state[tid]
31:
                 node \leftarrow desc.node
32.
                 if not IsStillPending(tid, phase) then
33:
                    break
34:
                 end if
                 if first = head and node \neq first then
35:
                     newDesc \leftarrow \texttt{OpDesc}(state[tid].phase, true, false, first)
36:
37:
                    if not CAS(state[tid], desc, newDesc) then
38:
                       continue
39:
                    end if
40:
                 end if
                 CAS(first.degTid, -1, tid)
                                                                                                                    ⊳ Lock node
41:
42:
                 HELP_FINISH_DEQ
43:
              end if
44:
           end if
       end while
45:
46: end procedure
```

node was successfully appended in line 29. The operation completes when the thread's own request has been processed (detected by checking if enqueuers [myIdx] is null in line 8). For commsumers in algorithm 24, the algorithm uses a dual-array approach with deqself and deqhelp to avoid excessive hazard pointer usage. Threads open a request by making deqself [myIdx] equal to deqhelp [myIdx] in lines 4 and 5 of the DEQUEUE function. The turn order follows the deqTid of the head node. When assigning nodes, threads use CAS to set the next node's deqTid field in line 8 of SEARCHNEXT in algorithm 25. This assignment

#### Algorithm 22 Kogan and Petrank's Queue Dequeue Helping Operations [33]

```
1: procedure Help_Finish_Deq
      first \leftarrow head
3:
      next \leftarrow first.next
4:
      tid \leftarrow first.deqTid
                                                                                                      > Thread that locked node
5:
      if tid \neq -1 then
6:
          desc \leftarrow state[tid]
7:
          if first = head and next \neq null then
8:
             newDesc \leftarrow \texttt{OpDesc}(state[tid].phase, false, false, state[tid].node)
9:
             CAS(state[tid], desc, newDesc)
                                                                                                                 ▶ Clear pending
10:
              CAS(head, first, next)
                                                                                                                 > Advance head
11:
           end if
12:
       end if
13: end procedure
14:
15: procedure HELP(phase)
       for i \leftarrow 0 to NUM\_THREADS-1 do
17:
           desc \leftarrow state[i]
18:
           if desc.pending and desc.phase \le phase then
19:
              if desc.enaueue then
20:
                 HELP\_ENQ(i, phase)
21.
              else
22:
                HELP_DEQ(i, phase)
23:
              end if
24:
           end if
25:
       end for
26: end procedure
```

is permanent and indicates ownership. The dequeue handles empty queues through a "give-up" mechanism implemented in GIVEUP (lines 28 to 44 of algorithm 25). When detecting an empty queue (head equals tail) in line 12 of DEQUEUE in algorithm 24, threads rollback their request in line 13 but must ensure no concurrent thread assigned them a node. This involves re-checking the queue state and potentially self-assigning the first node if no other requests exist (line 41 of GIVEUP). The algorithm closes requests by updating deqhelp[i] in line 18 of CASDEQANDHEAD in algorithm 25, making it differ from deqself[i]. Memory reclamation uses wait-free bounded hazard pointers integrated into the algorithm. Nodes are retired in line 35 of DEQUEUE in algorithm 24 only after ensuring they're no longer accessible through shared variables. The algorithm requires only one allocation per enqueued item (the node itself), achieving minimal memory overhead of  $O(N_{threads})$  compared to the  $O(N_{threads}^2)$  of other wait-free queues. [37]

#### Yang Mellor-Crummey (YMC) queue

Uses FAA and CAS combined with Kogan's and Petrank's fast-path slow-path methodology mentioned in chapter 3 to use the advantage of lock-free algorithms if possible while still maintaining wait-freedom. As shown in algorithms 26 to 29, the queue represents cells as an infinite array emulated through linked segments. Each segment contains N cells and a pointer to the next segment. The queue maintains global indices  ${\tt H}$  (head) and  ${\tt T}$  (tail) that are accessed using FAA, ensuring atomic increments without retry loops. For producers in

#### Algorithm 23 Turn Queue Enqueue Operation [37]

```
1: function Enqueue(item)
2:
      if item = null then throw InvalidArgument
3:
       end if
4:
       mvIdx \leftarrow GETINDEX
5:
       myNode \leftarrow \mathbf{new} \, \text{Node}(item, myIdx)
6:
       engueuers[mvIdx] \leftarrow mvNode
7:
       for i \leftarrow 0 to maxThreads - 1 do
8:
          if enqueuers[myIdx] = null then
                                                                                                            ▶ Request completed
9:
             hp.CLEAR
10:
              return
11:
           end if
12:
           ltail \leftarrow hp.ProtectPtr(kHpTail, tail)
13:
           if ltail \neq tail then continue
14:
           end if
15:
           if enqueuers[ltail.enqTid] = ltail then
                                                                                                              ▶ Clear old request
16:
              tmp \leftarrow ltail
17:
              CAS(enqueuers[ltail.enqTid], tmp, null)
18:
19:
           for i \leftarrow 1 to maxThreads do
                                                                                                              ▶ Find next request
20:
              nodeHelp \leftarrow enqueuers[(j+ltail.enqTid) \mod maxThreads]
21:
              if nodeHelp \neq null then
22:
                 nullnode \leftarrow null
23:
                 CAS(ltail.next, nullnode, nodeHelp)
                                                                                                                    ▶ Try append
24:
                 break
25:
              end if
26:
           end for
27:
           lnext \leftarrow ltail.next
28:
           if lnext \neq null then
                                                                                                         > Advance tail if needed
29:
              CAS(tail, ltail, lnext)
30:
           end if
31:
                                                                                                          ➤ Cleanup if not helped
32.
       enqueuers[myIdx] \leftarrow null
       hp.CLEAR
34: end function
```

algorithm 26, threads obtain a unique cell index via FAA on T in line 11. They then locate the corresponding cell using find\_cell which traverses segments and allocates new ones if needed. The fast-path attempts a simple CAS to deposit the value in line 13. If this fails, due to concurrent dequeue marking the cell unusable, the thread switches to the slow-path starting at line 20. The slow-path employs a helping mechanism where threads publish enqueue requests in their handle structure in line 23. In algorithm 29 consumers help pending enqueues through  $help\_enq$  in line 13 when they mark cells unusable. This creates a symbiotic relationship: producers get help depositing values, while consumers ensure values are available to dequeue. For consumers in algorithm 28, threads obtain cell indices via FAA on H in line 18. The algorithm uses  $help\_enq$  to secure values, which may involve helping slow-path enqueues. If a value is found, the consumer claims it using CAS on the cell's deq field in line 23. The slow-path beginning at line 30 publishes dequeue requests that helpers can satisfy by finding unclaimed values or determining the queue is empty. The algorithm maintains linearizability through careful ordering. Enqueues linearize when T moves past their cell index, while dequeues linearize when H moves past theirs. The helping mechanism ensures that after at most  $O(n^2)$ 

# Algorithm 24 Turn Queue Dequeue Operation [37]

```
1: function Dequeue
      myIdx \leftarrow GETINDEX
3:
      prReq \leftarrow deqself[myIdx]
                                                                                                   ▶ Save previous request
4:
      myReq \leftarrow deqhelp[myIdx]
5:
      deqself[myIdx] \leftarrow myReq
                                                                                                           ▶ Open request
6:
      for i \leftarrow 0 to maxThreads - 1 do
7:
         if deqhelp[myIdx] \neq myReq then break
                                                                                                        ▶ Request satisfied
8:
         end if
9:
         lhead \leftarrow hp.ProtectPtr(kHpHead, head)
10:
          if lhead \neq head then continue
11:
12:
          if lhead = tail then
                                                                                                           ▶ Queue empty
13:
             deqself[myIdx] \leftarrow prReq
                                                                                                                ⊳ Rollback
14:
             GIVEUP(myReq, myIdx)
15:
                                                                                                         ⊳ Check if helped
             if deqhelp[myIdx] \neq myReq then
16:
                deqself[myIdx] \leftarrow myReq
17:
                break
18:
             end if
19:
             hp.Clear
20:
             return null
21:
          end if
22:
          lnext \leftarrow hp.ProtectPtr(kHpNext, lhead.next)
23:
          if lhead \neq head then continue
24:
25:
          if SearchNext(lhead, lnext) \neq NOIDX then
26:
             CASDEQANDHEAD(lhead, lnext, myIdx)
27:
          end if
28:
       end for
29:
       myNode \leftarrow deqhelp[myIdx]
30:
       lhead \leftarrow hp.ProtectPtr(kHpHead, head)
31:
       if lhead = head and myNode = lhead.next then
32.
          CAS(head, lhead, myNode)
                                                                                                     ▶ Help advance head
33:
       end if
34:
       hp.CLEAR
                                                                                                    ▶ Retire previous node
35:
       hp.Retire(prReq)
36:
       return myNode.item
37: end function
```

failed attempts, all threads become helpers for a pending operation, guaranteeing completion. [40]

#### Feldman-Dechev Queue

Uses a sequence number-based mechanism with bitmarking to achieve bounded completion. As shown in algorithms 30 to 32, the ring buffer maintains two atomic counters accessed via NextTailSeq in line 7 of algorithm 30 and NextHeadSeq in line 7 of algorithm 31. Each position in the buffer array stores either an ElemNode containing an element and sequence ID, or an EmptyNode containing only a sequence ID. For producers in algorithm 30, threads acquire a sequence ID via FAA on the tail counter in line 7. The position is determined as seqid mod capacity in line 8. In the common case, threads replace an EmptyNode with matching or lower sequence ID with their prepared ElemNode via CAS in line 32. The

#### **Algorithm 25** Turn Queue Dequeue Helper Functions [37]

```
1: function SEARCHNEXT(lhead, lnext)
      turn \leftarrow lhead.deqTid
3:
      for idx \leftarrow turn + 1 to turn + maxThreads do
         idDeq \leftarrow idx \mod maxThreads
4:
5:
         if deqself[idDeq] \neq deqhelp[idDeq] then continue
6:
         end if
7:
         if lnext.deqTid = NOIDX then
8:
            {\tt CAS}(lnext.deqTid, NOIDX, idDeq)
                                                                                                        ⊳ Assign node
9:
         end if
10.
         break
11:
      end for
12:
      return lnext.deqTid
13: end function
14:
15: procedure CasDeqAndHead(lhead, lnext, myIdx)
      ldeqTid \leftarrow lnext.deqTid
17:
      if ldeqTid = mvIdx then
                                                                                                           ▶ My node
18:
          deqhelp[ldeqTid] \leftarrow lnext
                                                                                                      19:
          ldeqhelp \leftarrow hp.ProtectPtr(kHpDeq, deqhelp[ldeqTid])
20:
21:
         if ldeghelp \neq lnext and lhead = head then
22:
            CAS(deghelp[ldegTid], ldeghelp, lnext)
                                                                                                          ⊳ Help close
23:
          end if
24:
      end if
25:
      CAS(head, lhead, lnext)
                                                                                                      ▶ Advance head
26: end procedure
27:
28: procedure GIVEUP(myReq, myIdx)
29:
       lhead ← head
30:
      if deqhelp[myIdx] \neq myReq then return
                                                                                                     > Already helped
31:
      end if
32.
      if lhead = tail then return
                                                                                                         ▶ Still empty
      end if
34:
      hp.PROTECTPTR(kHpHead, lhead)
35:
      if lhead \neq head then return
36:
37:
      lnext \leftarrow hp.ProtectPtr(kHpNext, lhead.next)
38:
      if lhead \neq head then return
39:
      end if
40:
      if SearchNext(lhead, lnext) = NOIDX then
41:
          CAS(lnext.deqTid, NOIDX, myIdx)
                                                                                                         ⊳ Self-assign
42:
43:
      CASDEQANDHEAD(lhead, lnext, myIdx)
44: end procedure
```

algorithm handles thread delays through backoff and retry mechanisms. If a position contains an ElemNode or has a higher sequence ID than assigned, the thread breaks from the inner loop in line 36 to acquire a new sequence ID in the outer loop and attempt insertion at a new position. Bitmarking, setting a flag on a node, is used to indicate positions needing correction by delayed threads in line 20. For consumers in algorithm 31, threads similarly acquire a sequence ID via FAA on the head counter in line 7. They prepare an EmptyNode with sequence ID incremented by the buffer capacity in line 9. The dequeue succeeds when replacing an ElemNode with matching sequence ID in line 42 via CAS. If encountering an

#### Algorithm 26 YMC Queue Enqueue Operation [40]

```
1: function Enqueue(q, h, v)
        for p \leftarrow PATIENCE downto 0 do
                                                                                                                                   ▶ Try fast-path first
3:
            if ENQ_FAST(q, h, v, &cell_id) then
4:
               return
5:
            end if
6:
        end for
 7:
        ENQ\_SLOW(q, h, v, cell\_id)
                                                                                                                             ⊳ Fall back to slow-path
8: end function
10: function ENQ_FAST(q, h, v, cid)
        i \leftarrow \text{FAA}(\&q \rightarrow T, 1)
                                                                                                                              ⊳ Get unique cell index
12:
         c \leftarrow \text{FIND\_Cell}(\&h \rightarrow tail, i)
                                                                                                         ▶ Locate cell, allocate segment if needed
13:
        if CAS(c.val, \perp, v) then
                                                                                                                                ▶ Try to deposit value
14:
            return true
15:
         end if
16:
         *cid \leftarrow i
                                                                                                                  ⊳ Return cell index for slow-path
         return false
17:
18: end function
19:
20: function ENQ\_SLOW(q, h, v, cell\_id)
21:
        r \leftarrow \&h \rightarrow eng.reg
22:
        r \rightarrow val \leftarrow v
                                                                                                                                       ⊳ Publish value
23:
                                                                                                                         ⊳ Set pending=1, id=cell_id
        r \rightarrow state \leftarrow (1, cell\_id)
        tmp\_tail \leftarrow h \rightarrow tail
24:
25:
         repeat
26:
            i \leftarrow \text{FAA}(\&q \rightarrow T, 1)
27:
             c \leftarrow \text{FIND\_CELL}(\&tmp\_tail, i)
            if CAS(c \rightarrow enq, \perp_e, r) and c.val = \perp then
28:
                                                                                                                                         ▶ Reserve cell
29:
                 TRY_TO_CLAIM_REQ(&r \rightarrow state, id, i)
                                                                                                                         ⊳ Claim request for this cell
30:
                 break
31:
             end if
32.
         until \neg r \rightarrow state.pending
                                                                                                                         ▶ Until helped by dequeuer
33:
         id \leftarrow r \rightarrow state.id
                                                                                                                             ⊳ Get claimed cell index
34:
         c \leftarrow \text{FIND\_Cell}(\&h \rightarrow tail, id)
                                                                                                                        ⊳ Write value to claimed cell
         ENQ\_COMMIT(q, c, v, id)
36: end function
```

EmptyNode or lower sequence ID, threads use backoff and may bitmark ElemNodes to maintain FIFO ordering in line 32. The algorithm achieves bounded completion through a progress assurance scheme. After MAX\_FAILS attempts in line 11, threads post their operation to an announcement table and execute a wait-free slow path in lines 12 to 14. The helping mechanism works as follows: TryHelpAnother in lines 33 to 45 of algorithm 32 checks one entry in the announcement table per call, cycling through all threads. When an announced operation is found, helpers attempt to complete it using the Associate functions. These functions either claim and complete the operation via CAS or clean up failed attempts by replacing nodes. This ensures every operation completes within  $O(N_{threads}^2)$  steps, as all threads will eventually help any announced operation. [35]

#### **Algorithm 27** YMC Queue Enqueue Help Operation [40]

```
1: function Help_Enq(q, h, c, i)
2:
        if \neg CAS(c \rightarrow val, \bot, \top) and c \rightarrow val \neq \top then
                                                                                                                                     ▶ Value already present
3:
            return c \rightarrow val
4:
        end if
5:
        if c \rightarrow enq = \perp_e then
                                                                                                                        ⊳ No request yet, find one to help
6:
            repeat
7:
                 p \leftarrow h \rightarrow enq.peer
8:
                 r \leftarrow \&p \rightarrow enq.req
9:
                 s \leftarrow r \rightarrow state
10.
                 if h \rightarrow enq.id = 0 or h \rightarrow enq.id = s.id then
                                                                                                                             ▶ Haven't helped this request
11:
                     break
12:
                  end if
13:
                 h \rightarrow enq.id \leftarrow 0
14:
                 h \rightarrow enq.peer \leftarrow p \rightarrow next
                                                                                                                                         ▶ Move to next peer
15:
             until true
16:
              if s.pending and s.id \le i and \neg CAS(c \rightarrow enq, \bot_e, r) then
                                                                                                                               ▶ Try to reserve cell for peer
17:
                  h \rightarrow enq.id \leftarrow s.id
                                                                                                                             ▶ Remember we tried to help
18:
             else
19:
                 h \rightarrow enq.peer \leftarrow p \rightarrow next
                                                                                                                                   ▶ Peer doesn't need help
20:
             end if
21:
             if c \rightarrow enq = \perp_e then
22:
                 CAS(c \rightarrow enq, \perp_e, \top_e)
                                                                                                                    ▶ Mark no enqueue will use this cell
23:
             end if
24:
         end if
25:
         if c \rightarrow enq = \top_e then
                                                                                                                            ⊳ No enqueue will fill this cell
26:
             return (q \rightarrow T \le i ? EMPTY : T)
                                                                                                                              ▶ Check if queue was empty
27:
         end if
28:
         r \leftarrow c \rightarrow eng
                                                                                                                                29:
         s \leftarrow r \rightarrow state
30:
         v \leftarrow r \rightarrow val
31:
         if s.id > i then
                                                                                                                         ⊳ Request unsuitable for this cell
             if c \rightarrow val = \top and q \rightarrow T \le i then
32.
33:
                 return EMPTY
34:
             end if
35:
         else if Try_To_Claim_Req(&r \rightarrow state, s.id, i) or (s = (0, i) \text{ and } c \rightarrow val = \top) then
                                                                                                                                   ▶ Help commit the value
36:
              ENQ\_COMMIT(q, c, v, i)
37:
         end if
38:
         return c \rightarrow val
39: end function
```

#### Verma's Queue

Uses an external helper thread that works on a dedicated core to help other processes to finish their work in a finite number of steps. As shown in algorithm 33, the queue maintains a state array where each worker has a dedicated slot for operation requests. The queue uses a linked list with head and tail pointers managed exclusively by the helper thread. For producers in algorithm 33, threads create a request object containing the operation type and element in line 14, then place it in their designated position in the state array via direct assignment in line 15. They wait until the helper marks the operation as completed in line 16. The algorithm achieves simplicity by delegating all queue modifications to a single helper thread, eliminating the need for complex synchronization. For consumers in algorithm 33, threads similarly create a dequeue request in line 3 and place it in their state array slot in line 4. They wait for completion

#### Algorithm 28 YMC Queue Dequeue Operation [40]

```
1: function Dequeue(q, h)
        for p \leftarrow PATIENCE downto 0 do
                                                                                                                                    ▶ Try fast-path first
3:
            v \leftarrow \text{DEQ\_FAST}(q, h, \&cell\_id)
4:
            if v \neq T then break
5:
            end if
6:
        end for
7:
                                                                                                                                      ⊳ Fast-path failed
        if v = \top then
8:
           v \leftarrow \text{DEQ\_SLow}(q, h, cell\_id)
                                                                                                                                       ▶ Use slow-path
9:
        end if
10:
        if v \neq \text{EMPTY} then
                                                                                                                     ⊳ Got value, help peer dequeue
11:
             \text{HELP\_DEQ}(q, h, h \rightarrow deq.peer)
12:
             h \rightarrow deq.peer \leftarrow h \rightarrow deq.peer \rightarrow next
13:
         end if
14:
         return \nu
15: end function
16:
17: function Deq_Fast(q, h, id)
18:
         i \leftarrow \text{FAA}(\&q \rightarrow H, 1)
                                                                                                                               ⊳ Get unique cell index
19:
         c \leftarrow \text{FIND\_Cell}(\&h \rightarrow head, i)
20:
                                                                                                                     ▶ Try to get/help produce value
         v \leftarrow \text{HELP\_ENQ}(q, h, c, i)
21:
         if v = EMPTY then return EMPTY
22:
23:
         if v \neq \top and CAS(c \rightarrow deq, \bot_d, \top_d) then
                                                                                                                                      ▶ Claim the value
24:
            return v
25:
         end if
26:
         *id \leftarrow i
                                                                                                                   ▶ Return cell index for slow-path
27:
         return T
28: end function
29:
30: function Deq_Slow(q, h, cid)
31:
        r \leftarrow \&h \rightarrow deq.req
        r \rightarrow id \leftarrow cid
32.
                                                                                                                                        ⊳ Set request ID
        r \rightarrow state \leftarrow (1, cid)
                                                                                                                           ▶ Publish pending request
33:
34:
        HELP_DEQ(q, h, h)
                                                                                                                       ⊳ Help complete own request
                                                                                                                      ⊳ Get index where value found
35:
        i \leftarrow r \rightarrow state.idx
36:
         c \leftarrow \text{FIND\_Cell}(\&h \rightarrow head, i)
37:
         v \leftarrow c \rightarrow val
38:
         ADVANCE_END_FOR_LINEARIZABILITY(&q \rightarrow H, i+1)

    ► Ensure linearizability

         return (v = \top? EMPTY : v)
40: end function
```

in line 5, after which the dequeued element is available in the request object in line 9. The helper thread in algorithm 33 continuously traverses the state array in round-robin fashion in lines 24 to 52. When encountering an enqueue request, it creates a new node in line 29, appends it to the tail in line 30, and updates the tail reference in line 31. For dequeue requests, the helper checks if the queue is empty in line 35 and removes the head element in lines 39 and 40. The helper then updates the request with the dequeued value in line 44. This achieves bounded completion of every process as each operation completes within O(N) steps, where N is the number of workers, since the helper visits each state array position in fixed order. [39]

#### **Algorithm 29** YMC Queue Dequeue Help Operation [40]

```
1: function HELP_DEQ(q, h, helpee)
2: r \leftarrow helpee \rightarrow deq.req
3:
       s \leftarrow r \rightarrow state
4:
       id \leftarrow r \rightarrow id
5:
        if \neg s.pending or s.idx < id then return
                                                                                                                            ▶ Request complete or invalid
6:
        end if
7:
        ha \leftarrow helpee \rightarrow head
                                                                                                                > Segment pointer for announced cells
8:
                                                                                                                               ▶ Re-read after getting head
        s \leftarrow r \rightarrow state
        prior \leftarrow id; i \leftarrow id; cand \leftarrow 0
9:
10.
         while true do
11:
             for hc \leftarrow ha; \neg cand and s.idx = prior; do
                                                                                                                                             > Find candidate
12:
                 c \leftarrow \text{FIND\_CELL}(\&hc, + + i)
13:
                  v \leftarrow \text{Help\_Enq}(q, hc, c, i)
14:
                 if v = \text{EMPTY} or (v \neq \top \text{ and } c \rightarrow deq = \bot_d) then
                                                                                                                                          ⊳ Found candidate
15:
                     cand \leftarrow i
16:
                  else
17:
                     s \leftarrow r \rightarrow state
                                                                                                                                      ▶ Check if announced
18:
                 end if
19:
             end for
20:
             if cand then
21:
                                                                                                                                 ▶ Try announce candidate
                 CAS(\&r \rightarrow state, (1, prior), (1, cand))
22:
                 s \leftarrow r \rightarrow state
23:
             end if
24:
             if \neg s.pending or r \rightarrow id \neq id then return
                                                                                                                                       ▶ Request completed
25:
             end if
26:
             c \leftarrow \text{FIND\_Cell}(\&ha, s.idx)
                                                                                                                                       ⊳ Get announced cell
27:
             if c \rightarrow val = \top or CAS(c \rightarrow deq, \bot_d, r) or c \rightarrow deq = r then
28:
                 CAS(\&r \rightarrow state, s, (0, s.idx))
                                                                                                                                         ➤ Complete request
29:
                 return
30:
             end if
31:
              prior \leftarrow s.idx
32.
                                                                                                                                > Announced cell is ahead
             if s.idx \ge i then
                 cand \leftarrow 0; \ i \leftarrow s.idx
33:
                                                                                                                                              ▶ Jump forward
34:
             end if
35:
         end while
36: end function
```

#### Wait-Free Circular Queue (wCQ)

The wCQ also uses the fast-path-slow-path by Kogan and Petrank methodology where threads first attempt lock-free operations and fall back to a slow path with helping mechanisms to achieve bounded completion of threads. As shown in algorithms 34 to 36, wCQ extends the lock-free Scalable Circular Queue (sCQ) shown in algorithms 37 and 38 with a variation of Kogan and Petrank's fast-path-slow-path methodology to guarantee wait-freedom. Like sCQ, wCQ uses a ring buffer of size 2n while only using n entries at any time, with Head and Tail counters initialized to 2n (as in line 32 of algorithm 36). For producers in algorithm 34, threads first help others via HELP\_THREADS in line 37. The fast path from lines 38 to 44 attempts sCQs TRY\_ENQ function of algorithm 37 up to MAX\_PATIENCE times. If unsuccessful, the slow path begins in line 45. The thread records its request in a per-thread descriptor containing the tail value, index, and sequence numbers for integrity checks in lines 46 to 53. It then calls ENQUEUE\_SLOW in line 54, which repeatedly attempts to insert the element using collabora-

#### Algorithm 30 Feldman-Dechev Queue's Enqueue Operation [35]

```
1: function ENQUEUE(val)
      TRYHELPANOTHER
3:
      fails \leftarrow 0
4:
      while true do
5:
          if IsFull then return false
6:
         end if
7:
          segid \leftarrow NEXTTAILSEQ
                                                                                                                   ⊳ FAA on tail
8:
          pos \leftarrow seqid \mod capacity
9:
          n\_node \leftarrow \mathbf{new} \, \texttt{ElemNode}(seqid, val)
10.
          while true do
              if fails++=MAX\_FAILS then
11:
12:
                 op \leftarrow \mathbf{new} \, \text{EnqueueOp}(val)
13:
                 MAKEANNOUNCEMENT(op)
14:
                 return op.Result
15:
              end if
16:
              node \leftarrow buffer[pos].LOAD
17:
              if node.op \neq null then
                                                                                                             > Operation record
18:
                 node.op. Associate(node, \&buffer[pos])
19:
                 continue
20:
                                                                                                                    ▶ Bitmarked
              else if IsSkipped(node) then
21:
                 hreak
                                                                                                                ▶ Get new segid
22:
              else if node.seqid < seqid then
23:
                 BACKOFF
24:
                 if node = buffer[pos].LOAD then
25:
                    if IsEmptyNode(node) then
26:
                       if buffer[pos].CAS(node, n\_node) then
27:
                           return true
28:
                        end if
29:
                    end if
30:
                 end if
31:
              else if node.seqid \le seqid and ISEMPTYNODE(node) then
32.
                 if buffer[pos].CAS(node, n_node) then
33:
                    return true
34:
                 end if
35:
                                                                                           \triangleright node.seqid > seqid or ElemNode
              else
36:
                 break
                                                                                                                ⊳ Get new seqid
37:
              end if
38:
          end while
39:
       end while
40: end function
```

tive synchronization until successful. For consumers in algorithm 34, after checking for empty queue at lines 2 to 4 and helping others at line 5, threads attempt the fast path using TRY\_DEQ defined in lines 6 to 13 in algorithm 38. On failure, they record their dequeue request in lines 14 to 21 and call DEQUEUE\_SLOW in line 22, which similarly uses collaborative synchronization to ensure the dequeue completes. Results are gathered from the slow path in lines 25 in 33. The difference to the other queues is the SLOW\_F&A operation in algorithm 35 at lines 17 to 39, which ensures all cooperative threads (helpee and helpers) increment global counters only once per iteration. The operation works in two phases as seen in line 32 where it atomically updates the global counter with a phase2 pointer using DWCAS (the paper mistakenly calls this DCAS (CAS2)), and line 35 where it clears the INC flag. If the system does not support DWCAS, algorithm 39 shows how to substitute it with LL/SC, which can than again be substi-

tuted with versioned CAS shown in section 5.2.2. This mechanism allows <code>ENQUEUE\_SLOW</code> and <code>DEQUEUE\_SLOW</code> to coordinate multiple threads working on the same operation, ensuring exactly one succeeds while others detect the completion and terminate. Progress is guaranteed through the helping mechanism. <code>HELP\_THREADS</code> in lines 1 to 15 of algorithm 35 checks one thread per call, cycling through all threads. When finding a pending request, it calls <code>HELP\_ENQUEUE</code> or <code>HELP\_DEQUEUE</code> in lines 8 and 10. After <code>MAX\_PATIENCE</code> failed attempts, all threads eventually converge to help stuck threads, ensuring wait-freedom with  $O(N_{threads}^2)$  complexity. [38]

### **Excluded but valuable queues**

The following two queues were not included because they rely on theoretical hardware primitives that are not available in current hardware. However, they are valuable to know about, since they show how the performance of wait-free queues could be improved with special hardware.

- The queue Khanchandani and Wattenhofer [52] created uses theoretical atomic primitives called half-increment and half-max. Half-increment would be an operation on a theoretical register with two values, first half and second half, that increments the first half if <= second half. Half-max(x) updates the second half to the maximum of its current value and x. The reason this was even introduced was to show that, when combined with CAS, the time complexity of CAS with O(n) would be reduced to  $O(\sqrt{n})$ , if such hardware would exist.
- Bédin et al. [53] who created a queue using a theoretical atomic primitive called memory-to-memory swap, which changes to memory locations atomically with each other (so a DCAS without the compare part), to show that it would be possible to create wait-free queues as fast as lock-free queues, if the hardware would exist. While thiss is valubale to know how special hardware could improve the performance of wait-free queues, it is not relevant for this thesis, since it is not possible to implement these algorithms on current hardware.

This algorithm was not included in the thesis, because it was running too slow to create valuable benchmark resutls, but still is important to mention, since they show an interesting improvement for time complexity of wait-free queues:

• Naderibeni and Ruppert [54] showed that it is possible to create a wait-free queue using CAS and still achieve a polylogarithmic time complexity by integrating a binary tree structure like Jayanti and Petrovic.

#### Algorithm 31 Feldman-Dechev Queue's Dequeue Operation [35]

```
1: function DEQUEUE(&result)
2:
      TRYHELPANOTHER
3:
      fails \leftarrow 0
4:
      while true do
5:
         if ISEMPTY then return false
6:
7:
         seqid \leftarrow NextHeadSeQ
                                                                                                                 > FAA on head
8:
          pos \leftarrow seqid \mod capacity
9:
          n\_node \leftarrow \mathbf{new} \; \texttt{EmptyNode}(seqid + capacity)
10:
          while true do
11:
              if fails++=MAX\_FAILS then
12:
                 op \leftarrow \mathbf{new} DequeueOp
13:
                 MAKEANNOUNCEMENT(op)
14:
                 return op.Result(result)
15:
16:
              node \leftarrow buffer[pos].LOAD
17:
              if node.op \neq null then
18:
                 node.op. Associate(node, \&buffer[pos])
19:
                 continue
20:
              else if IsSkipped(node) and IsEmptyNode(node) then
21:
                 if buffer[pos].CAS(node, n\_node) then
22:
                    break
23:
                 end if
24:
              else if seqid > node.seqid then
                                                                                                            ▶ Delayed element
25:
                 BACKOFF
26:
                 if node = buffer[pos].Load then
                    if ISEMPTYNODE(node) then
27:
28:
                       if buffer[pos].CAS(node, n_node) then
29:
                          break
30:
                       end if
31:
                    else
32:
                                                                                                                     ⊳ Bitmark
                       SetSkipped(&buffer[pos])
33:
                    end if
34:
                 end if
              \textbf{else if } seqid < node.seqid \textbf{ then}
35:
36:
                 break
                                                                                                               ⊳ Get new seqid
37:
              else
                                                                                                        \triangleright seqid = node.seqid
38:
                 if IsElemNode(node) then
39:
                    if IsSkipped(node) then
                       n\_node \leftarrow SetSkipped(n\_node)
40:
41:
42:
                    \textbf{if} \ buffer [pos]. {\sf CAS} (node, n\_node) \ \textbf{then}
43:
                       result \leftarrow node.value
                       return true
44:
45:
                    end if
46:
                 else
                                                                                            > EmptyNode with matching seqid
47:
                    BACKOFF
48:
                    if node = buffer[pos].Load then
49:
                       if buffer[pos].CAS(node, n\_node) then
50:
                          break
51:
                       end if
52:
                    end if
53:
                 end if
54:
              end if
           end while
55:
       end while
57: end function
```

#### Algorithm 32 Feldman-Dechev Queue's Helper Functions [35]

```
1: function ENQUEUEOP::ASSOCIATE(node, address)
      success \leftarrow helper.CAS(null, node)
3:
      if success or helper.Load = node then
4:
          node.op.Store(null)
                                                                                                         ⊳ Remove op reference
5:
      else
6:
          n\_node \leftarrow \mathbf{new} \; \texttt{EmptyNode}(node.seqid)
7:
          if not address.CAS(node, n\_node) then
8:
             node \leftarrow SetSkipped(node)
9:
             if address.Load = node then
10:
                 n\_node \leftarrow SetSkipped(n\_node)
11:
                 address.CAS(node, n\_node)
              end if
12:
13:
          end if
14:
       end if
15: end function
16:
17: function DEQUEUEOP::ASSOCIATE(node, address)
       success \leftarrow helper.CAS(null, node)
19:
       if success or helper.LOAD = node then
20:
           n\_node \leftarrow \mathbf{new} \; \texttt{EmptyNode}(node.seqid + capacity)
21:
          if not address.CAS(node, n_node) then
22:
              node \leftarrow SetSkipped(node)
23:
              \textbf{if} \ address. \texttt{LOAD} = node \ \textbf{then}
24:
                 n\_node \leftarrow SetSkipped(n\_node)
25:
                 address. {\it CAS}(node, n\_node)
26:
              end if
27:
          end if
28:
       else
           node.op. Store(null)
29:
30:
       end if
31: end function
32:
33: function TryHelpAnother
34:
                                                                          > Check announcement table and help one operation
35:
       helpIdx \leftarrow thread-local helping index
36:
       op \leftarrow announcementTable[helpIdx]
37:
       if op \neq null and op.InProgress then
38:
          if op is EnqueueOp then
39:
              WAITFREEENQUEUE(op)
40:
          else
41:
              WAITFREEDEQUEUE(op)
42:
           end if
43:
       end if
44:
       helpIdx \leftarrow (helpIdx + 1) \mod MAX\_THREADS
45: end function
```

#### Algorithm 33 Verma's Queue Operations [39]

```
1: function Dequeue
       id \leftarrow \mathsf{GETTHREADID}

ightharpoonup Get worker's unique ID
       req \leftarrow CREATEREQUEST(null, DEQUEUE)
                                                                                                               ▶ Create dequeue request
4:
       stateArr[id] \leftarrow req
                                                                                                       > Place request in dedicated slot
5:
       while \neg req.isCompleted do
                                                                                                             ▶ Wait for helper to process
6:
          wait
7:
       end while
8:
       stateArr[id] \leftarrow null
                                                                                                        ▶ Clear request from state array
9:
                                                                                                            > Return dequeued element
       return req.e
10: end function
11:
12: function ENQUEUE(e)
                                                                                                                ⊳ Get worker's unique ID
13:
        id \leftarrow \text{GetThreadId}
        req \leftarrow \text{CreateRequest}(e, \text{ENQUEUE})
14:
                                                                                                > Create enqueue request with element
15:
        stateArr[id] \leftarrow req
                                                                                                       > Place request in dedicated slot
16:
        while \neg req.isCompleted do
                                                                                                             ▶ Wait for helper to process
17:
           wait
18:
        end while
19:
        stateArr[id] \leftarrow null
                                                                                                        ▶ Clear request from state array
20:
        return true
21: end function
22:
23: function Helper
        id \leftarrow 0
24:

⊳ Start at first worker slot

25:
        while true do
                                                                                                               ▶ Continuous helper loop
26:

ightharpoonup Check current slot for request
           req \leftarrow stateArr[id]
27:
           if req \neq null \land \neg req.isCompleted then
                                                                                                               > Found pending request
28:
               if req.operation = ENQUEUE then
                  n \leftarrow \mathbf{new} \operatorname{Node}(req.e)
29:
                                                                                                                       ▶ Create new node
30:
                   tail.next \leftarrow n
                                                                                                                          ⊳ Append to tail
31:
                  tail \leftarrow n
                                                                                                                  ▶ Update tail reference
32:
                  size \leftarrow size + 1
33:
                  req. is Completed \leftarrow true
                                                                                                                ▶ Mark request complete
34:
               else if req.operation = DEQUEUE then
35:
                  if head.next = null then
                                                                                                                        ▶ Queue is empty
36:
                      req.e \leftarrow null
37:
                      req. is Completed \leftarrow true
38:
                  else
39:
                      n \leftarrow head.next

ightharpoonup Get first element
40:
                      head.next \leftarrow n.next
                                                                                                                   ▶ Remove from queue
41:
                      if n.next = null then
                                                                                                                     ▶ Queue now empty
42:
                         tail \leftarrow head
                                                                                                                               ⊳ Reset tail
43:
                      end if
44:
                                                                                                                 ⊳ Store dequeued value
                      req.e \leftarrow n.e
45:
                      size \leftarrow size - 1
46:
                      req. is Completed \leftarrow true
47:
                  end if
48:
               end if
49:
           end if
50:
           id \leftarrow (id + 1) \mod workers
                                                                                                              ⊳ Round-robin to next slot
        end while
51:
52: end function
```

#### Algorithm 34 wCQ's Operations [38] 1: function Dequeue\_wCQ if LOAD(&Threshold) < 0 then 3: return Ø ▶ Empty 4: end if 5: HELP\_THREADS 6: ⊳ Fast path (SCQ) 7: $count \leftarrow MAX\_PATIENCE$ 8: while $--count \neq 0$ do 9: idx10: $head \leftarrow TRY_DEQ(\&idx)$ 11: **if** head = OK **then return** idx12: end if 13: end while 14: ⊳ Slow path (wCQ) 15: $r \leftarrow \&Record[TID]$ 16: $seq \leftarrow r.seq1$ 17: $r.localHead \leftarrow head$ $r.initHead \leftarrow head$ 18: 19: $r.enqueue \leftarrow \mathbf{false}$ 20: $r.seq2 \leftarrow seq$ $r.pending \leftarrow \mathbf{true}$ 21: 22: ${\tt DEQUEUE\_SLOW}(head,r)$ $r.pending \leftarrow \mathbf{false}$ 23: 24: $r.seq1 \leftarrow seq + 1$ 25: ⊳ Get slow-path results 26: $h \leftarrow \text{COUNTER}(r.localHead)$ 27: $i \leftarrow \text{CACHE\_REMAP}(h \mod 2n)$ 28: $Ent \leftarrow LOAD(\&Entry[j].Value)$ 29: if Ent.Cycle = Cycle(h) and $Ent.Index \neq \bot$ then 30: CONSUME(h, j, Ent)31: $\mathbf{return}\ Ent. Index$ 32: end if 33: return Ø 34: end function 35: 36: **function** Enqueue\_wCQ(*index*) 37: HELP\_THREADS 38: ⊳ Fast path (SCQ) 39: $count \leftarrow MAX\_PATIENCE$ 40: **while** $--count \neq 0$ **do** 41: $tail \leftarrow TRY\_ENQ(index)$ 42: if tail = OK then return true 43: end if 44: end while 45: ⊳ Slow path (wCQ) 46: $r \leftarrow \&Record[TID]$ 47: $seq \leftarrow r.seq1$ $r.localTail \leftarrow tail$ 48: $r.initTail \leftarrow tail$ 49: 50: $r.index \leftarrow index$ 51: $r.enqueue \leftarrow \mathbf{true}$ 52: $r.seq2 \leftarrow seq$ 53: $r.pending \leftarrow \mathbf{true}$ $ENQUEUE\_SLOW(tail, index, r)$ 55: $r.pending \leftarrow \mathbf{false}$ $r.seq1 \leftarrow seq + 1$

57: end function

#### Algorithm 35 wCQ's Helper Functions [38]

```
1: function HELP_THREADS
      r \leftarrow \&Record[TID]
3:
       if -r.nextCheck \neq 0 then return
4:
       end if
5:
      thr \leftarrow \&Record[r.nextTid]
6:
       if thr.pending then
7:
          if thr.enqueue then
8:
              HELP_ENQUEUE(thr)
9:
          else
10:
              {\tt HELP\_DEQUEUE}(thr)
11:
           end if
12:
        end if
        r.nextCheck \leftarrow HELP\_DELAY
13:
       r.nextTid \leftarrow (r.nextTid + 1) \mod NUM\_THRDS
14:
15: \ \textbf{end function}
16:
17: function SLOW_F&A(globalp, local, v, thld)
       phase2 \leftarrow \&Record[TID].phase2
18:
19:
        repeat
20:
           cnt \leftarrow \texttt{LOAD\_GLOBAL\_HELP\_PHASE2}(globalp, local)
21:
           if cnt = \emptyset or !CAS(local, *v, cnt | INC) then
22:
               *v \leftarrow *local
23:
               if v\&FIN then return false
               end if
24:
               if !(*v\&INC) then return true
25:
26:
               end if
27:
               cnt \leftarrow \text{COUNTER}(*v)
28:
           else
29:
               *v \leftarrow cnt|INC
30:
31:
           {\tt PREPARE\_PHASE2}(phase2, local, cnt)
        \textbf{until} \ \mathsf{CAS2}(globalp, \{cnt, \textbf{null}\}, \{cnt+1, phase2\})
33:
        if thld then F&A(thld,-1)
34:
        end if
35:
        \mathsf{CAS}(local,cnt|INC,cnt)
36:
        {\it CAS2}(globalp, \{cnt+1, phase2\}, \{cnt+1, {\bf null}\})
37:
        *v \leftarrow cnt
38:
        return true
39: end function
```

#### Algorithm 36 wCQ's Data Structures [38]

```
1: \textbf{struct} \ phase2rec\_t \ \{
2: seq1: int = 1
3:
     *local:int
4:
     cnt: int
5:
     seq2: int = 0
6: }
7:
8: struct entpair_t {
9: Note : int = -1
10: Value : entry_t = \{ .Cycle=0, .IsSafe=1, .Enq=1, .Index=\bot \}
11: }
12:
13: Entry[2n] : entpair_t
14:
15: struct thrdrec_t {
                                                                                              ⊳ === Private Fields ===
16:
17:
      nextCheck: int = HELP\_DELAY
18:
                                                                                                         ⊳ Thread ID
      nextTid:int
19:
                                                                                              ⊳ === Shared Fields ===
20:
     phase2: phase2rec_t
                                                                                                           ⊳ Phase 2
21:
      seq1: int = 1
22:
      enqueue: bool
      pending: bool = false
24:
      localTail, initTail: int
25:
      localHead, initHead: int
26:
      index: int
27:
     seq2: int = 0
28: }
29:
30: Record[NUM\_THRDS]: thrdrec\_t
31: Threshold: int = -1
                                                                                                       ⊳ Empty wCQ
32: Tail: int = 2n, Head: int = 2n
```

Algorithm 37 Lock-free Circular Queue (SCQ): Enqueue Operations [38]

3:

5:

7:

8:

9:

11:

14:

15:

16:

17:

18:

19: 20:

21:

22:

23:

24:

25:

end if

end if

end if  $\mathbf{return}\ T$ 

27: end function

return OK

if LOAD(&Threshold)  $\neq 3n-1$  then

STORE(&Threshold, 3n-1)

#### 1: *Threshold*: int = -1 ⊳ Empty SCQ 2: Tail: int = 2n, Head: int = 2n ${\color{red} \rhd \ Init\ entries:\ \{.Cycle=0,\ .IsSafe=1,\ .Index=\bot\}}$ 4: $Entry[2n] : entry_t$ 6: **function** ENQUEUE\_SCQ(*index*) **while** TRY\_ENQ(index) $\neq$ OK **do** ▶ Try again end while 10: end function 12: **function** TRY\_ENQ(*index*) $T \leftarrow F&A(&Tail, 1)$ $j \leftarrow \mathsf{CACHE}_\mathsf{REMAP}(T \bmod 2n)$ $E \leftarrow \texttt{LOAD}(\&Entry[j])$ $\textbf{if} \ E.Cycle < \texttt{CYCLE}(T) \ \textbf{and} \ (E.IsSafe \ \textbf{or} \ \texttt{Load}(\&Head) \leq T) \ \textbf{and} \ (E.Index = \bot \ \textbf{or} \ \bot_{\mathcal{C}}) \ \textbf{then}$ $New \leftarrow \{ \texttt{CYCLE}(T), 1, index \}$ $\textbf{if} \, ! \mathsf{CAS}(\&Entry[j], E, New) \textbf{ then}$ goto 22

▶ Try again

#### Algorithm 38 Lock-free Circular Queue (SCQ): Dequeue Operations [38]

```
1: function TRY_DEQ(*index)
      H \leftarrow F&A(\&Head, 1)
3:
      j \leftarrow \text{Cache}\_\text{Remap}(H \text{ mod } 2n)
      E \leftarrow \text{LOAD}(\&Entry[j])
4:
5:
      if E.Cycle = Cycle(H) then
6:
          CONSUME(H, j, E)
7:
          *index \leftarrow E.Index
8:
          return OK
                                                                                                                         9:
      end if
10:
       New \leftarrow \{E.Cycle, 0, E.Index\}
11:
       if E.Index = \bot or \bot_c then
12:
          New \leftarrow \{ \texttt{CYCLE}(H), E.IsSafe, \bot \}
13:
14:
       if E.Cycle < Cycle(H) then
15:
          if !CAS(\&Entry[j], E, New) then
16:
              goto 33
17:
          end if
           T \leftarrow \texttt{LOAD}(\& Tail)
18:
                                                                                                                           ⊳ Exit if
19:
          if T \le H + 1 then
                                                                                                                           ⊳ empty
20:
              CATCHUP(T, H + 1)
21:
           end if
22:
           F&A(&Threshold,-1)
23:
          *index \leftarrow \emptyset
                                                                                                                          ⊳ Empty
24:
           return OK
                                                                                                                         25:
       end if
26:
       if F&A(&Threshold, -1) \le 0 then
27:
           *index \leftarrow \emptyset
                                                                                                                          ▶ Empty
28:
           return OK
                                                                                                                         29:
       end if
30:
       return H
                                                                                                                        ⊳ Try again
31: end function
32:
33: function DEQUEUE_SCQ
       if LOAD(&Threshold) < 0 then
34:
          return Ø
                                                                                                                           ⊳ Empty
36:
       end if
37:
       while TRY_DEQ(&idx) \neq OK do
38:

ightharpoonup Try again
39:
       end while
40:
       return idx
41: end function
42:
43: function Consume(h, j, e)
       OR(\&Entry[j], \{0, 0, \bot_c\})
45: end function
```

# Algorithm 39 CAS2 implementation for wCQ using LL/SC [38]

```
1: \textbf{ function } CAS2\_Value(Var: entpair\_t^*, Expect: entpair\_t, New: entpair\_t)
      Prev.Value \leftarrow \text{LL}(\&Var \rightarrow Value)
       Prev.Note \leftarrow Load(\&Var \rightarrow Note)
4:
       if Prev \neq Expect then
5:
          return false
6:
       end if
7:
      return SC(\&Var \rightarrow Value, New.Value)
8: end function
9:
10: function CAS2_Note(Var: entpair\_t^*, Expect: entpair\_t, New: entpair\_t)
11:
      Prev.Note \leftarrow LL(\&Var \rightarrow Note)
12:
        Prev.Value \leftarrow Load(\&Var \rightarrow Value)
13:
       if Prev \neq Expect then
14:
           return false
15:
        end if
16:
       return SC(\&Var \rightarrow Note, New.Note)
17: end function
```

After the wait-free algorithms got identified and analyzed the next sub-goal to find the best wait-free algorithms is to implement them like already said in section 1.2. The algorithms got implemented and published in the accompanying GitHub repository in [50], where complete implementation of the algorithms can be found. This chapter will present the implementation details of the concurrent queue algorithms seen in chapter 5 in Rust, focusing on the adaptations necessary for IPC over shared memory. While the algorithmic logic of each queue has been discussed already in chapter 5, the implementation required slight deviations to support IPC over shared memory. This includes ensuring correct cache allignment, correctly implementing various atomic primitives, and correctly implementing the logic for shared memory support based on short example snippets of the actual rust implementation from the GitHub repository or some general examples. This does not include showing again the same algorithmic logic just in a actual programming language instead of pseudocode, since that would be redundant. This chapter will give the necessary details to understand how to implement the algorithms in Rust and how to adapt them for IPC over shared memory.

# 6.1. Shared Memory Management for Inter-Process Communication

IPC through shared memory requires slightly different approaches compared to multi-threaded heap-based communication. The primary constraint is that shared memory regions may be mapped at different virtual addresses in different processes, requiring all data structures to be completely position-independent. Additionally, dynamic memory allocation is not possible within shared memory regions, necessitating buffer allocation from a pre-allocated memory pool for all dynamic data structures. Threads on the other hand can use the process-private heap for dynamic memory allocation, which' memory layout is shared between threads on the same process, but not processes.

# 6.1.1. Shared Memory Size Calculation

Each queue provides a method to calculate the exact shared memory size required. This calculation determines how much memory to allocate from the operating system. The following examples from BQueue and wCQ demonstrate both simple and complex size calculations as needed:

Listing 6.1: Shared memory size calculation methods

```
1 // From BQueue - simple calculation
pub const fn shared_size(capacity: usize) -> usize {
      mem::size_of::<Self>()
                                                           // Queue structure
          + capacity * mem::size_of::<MaybeUninit<T>>() // Data storage
4
          + capacity * mem::size_of::<AtomicBool>()
                                                           // Validity flags
5
6 }
8 // From WCQueue - complex layout calculation
9 fn layout(num_threads: usize, num_indices: usize) -> (Layout, [usize; 4])
      let ring_size = num_indices.next_power_of_two();
10
11
      let capacity = ring_size * 2;
12
13
      let root = Layout::new::<Self>();
      let (l_aq_entries, o_aq_entries) = root
14
           .extend(Layout::array::<EntryPair>(capacity).unwrap())
15
16
          .unwrap();
17
      let (l_fq_entries, o_fq_entries) = l_aq_entries
18
          .extend(Layout::array::<EntryPair>(capacity).unwrap())
19
          .unwrap();
      let (l_records, o_records) = l_fq_entries
20
          .extend(Layout::array::<ThreadRecord>(num_threads).unwrap())
21
22
           .unwrap();
      let (l_final, o_data) = l_records
23
           .extend(Layout::array::<DataEntry<T>>(num_indices).unwrap())
24
25
           .unwrap();
26
      (l_final.pad_to_align(), [o_aq_entries, o_fq_entries, o_records,
27
      → o_data])
28 }
29
30 pub fn shared_size(num_threads: usize) -> usize {
      let (_layout, _offsets) = Self::layout(num_threads, num_indices);
      _layout.size() // Total bytes needed for mmap
32
33 }
```

The size calculation accounts for all components including alignment padding. Some queues like wCQ use Rust's Layout API shown in lines 9 to 26 to ensure proper alignment and correctly calculated offsets. For simple queues like BQueue, manual calculation like in lines 2 to 6 suffices.

#### 6.1.2. Shared Memory Allocation

Once the required size is calculated, the following functions in listing 6.2 used in all benchmarks demonstrates how to allocate and deallocate the needed shared memory regions using mmap:

Listing 6.2: Shared memory allocation using mmap

```
unsafe fn map_shared(bytes: usize) -> *mut u8 {
let ptr = libc::mmap(
```

```
ptr::null_mut(),
          bytes,
                                                      // Size from
      → shared_size()
          libc::PROT_READ | libc::PROT_WRITE,
5
          libc::MAP_SHARED | libc::MAP_ANONYMOUS, // Shared between
6
      → processes
          -1,
7
8
           0,
9
      );
      if ptr == libc::MAP_FAILED {
10
          panic!("mmap_failed:__{}", std::io::Error::last_os_error());
11
12
      ptr.cast()
13
14 }
15
16 // Cleanup function
unsafe fn unmap_shared(ptr: *mut u8, len: usize) {
      if libc::munmap(ptr.cast(), len) == -1 {
19
          panic!("munmap_failed:_{{}}", std::io::Error::last_os_error());
20
21 }
```

The MAP\_SHARED flag ensures that modifications to the memory region are visible to all processes that map it. The MAP\_ANONYMOUS flag creates memory not backed by a file. The bytes parameter on line 4 comes directly from the shared\_size() calculation earlier.

#### 6.1.3. Memory Layout and Initialization

After allocating the shared memory region the components needed by the queue's implementations need to be initialized. All queue implementations follow a consistent pattern for shared memory initialization. The initialization function receives the pre-allocated memory pointer and organizes components within that memory region. The most complex example, the WCQueue from section 5.2.4, demonstrates how multiple components are laid out in shared memory with proper alignment:

Listing 6.3: Memory layout initialization in WCQueue

```
let aq_entries = mem.add(current_offset) as *mut EntryPair;
12
      current_offset += capacity * mem::size_of::<EntryPair>();
13
14
      // Initialize structures in-place
      ptr::write(q_ptr, Self {
15
           aq_entries_offset: current_offset,
16
          base_ptr: mem, // Store base pointer for offset calculations
17
18
           // Store offsets instead of pointers
19
      });
20
21
      &mut *q_ptr
22 }
```

The alignment calculation in line 5 ensures that each component starts at a properly aligned address. This is crucial for atomic operations, which often require natural alignment. The queue structure stores offsets relative to the base pointer rather than absolute pointers in line 16, ensuring position independence. When accessing these components later, the offset is added to the base pointer, as demonstrated in listing 6.4.

Listing 6.4: Position-independent component access

# 6.1.4. Node Allocation from Pre-allocated Memory Pools

Some queues as seen in chapter 5 use dynamic memory allocation within the process-private heap. For the IPC over shared memory use-case of this thesis that is not possible, because in shared memory dynamic memory allocations or deallocations with malloc or free are not possible, since that allocates from process-private heaps that are not available for other processes. Therefore, all queues that would normally allocate memory dynamically have been adapted to allocate from the initialized pre-allocated memory pool. As an example the Jiffy Queue algorithm from section 5.2.2 shows a dynamic heap allocation method to allocate new buffers to insert them into the linked-list. This was adapted to IPC over shared memory in rust by a pool allocation system with free lists that is similarly impülemented for all other queues needing dynamic memory allocation, as shown in listing 6.5.

Listing 6.5: Lock-free memory pool allocation

```
let next_free = (*(free_head as *mut AtomicPtr<Node<T>>))
               .load(Ordering::Acquire);
10
11
           if self.node_array_slice_free_list_head.compare_exchange(
12
13
               free_head,
               next_free,
14
15
               Ordering::AcqRel,
               Ordering::Acquire
16
17
           ).is_ok() {
               return free_head;
18
19
      }
20
21
      // Allocate from pre-allocated pool
22
23
      let nodes_needed = self.buffer_capacity_per_array;
24
      let start_idx = self.node_arrays_next_free_node_idx
25
           .fetch_add(nodes_needed, Ordering::AcqRel);
26
      if start_idx + nodes_needed > self.node_arrays_pool_total_nodes {
27
28
          self.node_arrays_next_free_node_idx
               .fetch_sub(nodes_needed, Ordering::Relaxed);
29
          return ptr::null_mut(); // Pool exhausted
30
      }
31
32
      self.node_arrays_pool_start.add(start_idx)
33
```

This implementation maintains a free list using CAS operations in lines 12 to 16. When the free list is empty, it falls back to allocate from the pre-allocated pool seen in lines 23 and 24. The fetch\_add operation atomically increments the allocation index, ensuring process-safe allocation. If the pool is exhausted, the operation fails by returning a null pointer in line 30.

# 6.2. Cache Line Optimization

Processors transfer data between cores in cache line units explained in section 5.2.1. When multiple processes access data on the same cache line, even if different variables, the cache coherence protocol causes the cache line to bounce between cores, degrading execution times.

# 6.2.1. Explicit Cache Line Padding

In chapter 5 multiple queues were shown that describe seperating the cache line. To show how this is done in rust the BLQ explained in section 5.2.1 will be taken to show how to explicitly seperate the cache lines, as shown in listing 6.6.

Listing 6.6: Cache line separation in BlqQueue

```
const CACHE_LINE_SIZE: usize = 64;
```

```
3 #[repr(C)]
4 #[cfq_attr(any(target_arch = "x86_64", target_arch = "aarch64"),
     → repr(align(64)))]
5 pub struct SharedIndices {
     pub write: AtomicUsize, // Producer's cache line
     pub read: AtomicUsize, // Consumer's cache line
7
8 }
10 #[repr(C, align(64))]
11 struct ProducerPrivate {
     12
     write_priv: usize,
                           // Producer-only write position
13
14 }
15
16 #[repr(C, align(64))]
17 struct ConsumerPrivate {
     write_shadow: usize,
                          // Local copy to avoid false sharing
19
     read_priv: usize,
                           // Consumer-only read position
```

The # [repr(C)] attribute ensures C-compatible memory layout, while

#[repr(align(64))] forces the structure to start at a cache line boundary shown in lines 4 and 10. Although SharedIndices contains only two usize values with 16 bytes total, the alignment ensures they reside in separate cache lines. The producer updates write while the consumer updates read, preventing false sharing. The shadow copies read\_shadow in line 12 and write\_shadow in line 18 ensures that producer and consumer work on different cache lines, preventing the cache lines to bounce between the producer process and consumer process.

Similarly all queues that need this kind of cache line separation use this pattern to ensure that the producer and consumer do not share cache lines, preventing false sharing leading to cache lines bouncing between cores.

# 6.2.2. Manual Padding Arrays

For structures where alignment alone is insufficient, manual padding arrays provide a solution, as demonstrated in listing 6.7. This is used in all queues needing manual padding. As an example the implementation of the David queue explained in section 5.2.3 uses manual padding.

Listing 6.7: Manual padding for exact cache line control

```
1 #[repr(C, align(64))]
2 struct FetchIncrement {
3    value: AtomicUsize,
4    _padding: [u8; CACHE_LINE_SIZE - std::mem::size_of::<AtomicUsize>()],
5 }
6
7 #[repr(C, align(64))]
```

```
8 struct Node<T> {
9     val: Option<T>,
10     next: AtomicPtr<Node<T>>,
11     _padding: [u8; CACHE_LINE_SIZE - 24], // Fill remaining cache line
12 }
```

The padding array size is calculated to fill the remainder of the cache line seen in lines 4 and 11. For FetchIncrement, the AtomicUsize occupies 8 bytes, so 56 bytes of padding complete the 64-byte cache line. This ensures each FetchIncrement instance occupies exactly one cache line, preventing false sharing in arrays of such structures, as required by the DavidQueue implementation from section 5.2.3.

# 6.3. Atomic Primitives Implementation

The algorithms in chapter 5 all use different kind of atomic primitives. To implement them rust provides a set of atomic operations with explicit memory ordering semantics, allowing control over synchronization order. This section shows how in general the atomic operations from chapter 5 are implemented in Rust across all queues, explained with specific examples. In rust atomic primitives can only be called on atomic types. Hence variables that are used in atomic operations must be defined as atomic types.

# 6.3.1. Fetch and Add (FAA)

The rust implementations of DQueue, BQueue and wCQ explained in chapter 5 are a good example, to understand how to implement FAA called fetch\_add (v, ordering) in rust.

Listing 6.8: Fetch-and-add with different memory orderings

In rust FAA is a method call on atomic types as seen in line 4. In listing 6.8 the memory ordering parameter added as the second argument after the value to add determines the synchronization order of FAA. Ordering::Relaxed in line 6 provides no synchronization, suitable for private counters. Ordering::AcqRel in line 3 ensures acquire semantics for the read and release semantics for the write, establishing happens-before relationships as required by the DQueue algorithm. Ordering::SeqCst in line 9 provides the strongest guarantees, ensuring a total order across all sequentially consistent operations, necessary for the complex wCQ. One simple solution would be to always use Ordering::SeqCst for all

operations, but that would reduce the execution times of the algorithms in a significant way. Consequently it is important to analyze the algorithms from chapter 5 to understand which memory ordering is needed for which operation.

# 6.3.2. Compare and Swap (CAS)

The implementation of wCQ shows how to implement CAS, called compare\_exchange(old\_value, new\_value, ordering\_on\_success, ordering\_on\_failure) in rust, as shown in listing 6.9.

Listing 6.9: Compare-and-swap variants and usage patterns

```
1 // Strong CAS with sequential consistency (from wcqueue)
2 match entry.value.compare_exchange(
3
      packed,
4
      new_packed,
      Ordering::SeqCst, // Success ordering
5
      Ordering::SeqCst,
                          // Failure ordering
6
7 ) {
8
      Ok (_) => {
          fence(Ordering::SeqCst); // Additional synchronization
9
10
          Ok(())
11
      }
     Err(current) => {
12
          // Retry with current value
13
14
15 }
16
17 // Weak CAS for performance (general example)
18 match entry.value.compare_exchange_weak(
     old_value,
19
20
     new_value,
21
      Ordering::AcqRel,
22
      Ordering::Acquire,
23 ) {
24
      Ok (_) => {
         // do something on success
25
26
      Err(current) => {
27
      // do something on failure
28
29
      }
```

The weak variant <code>compare\_exchange\_weak</code> in beginning at 17 may fail spuriously even when the values match, but can be more efficient on some architectures. The strong variant guarantees success when values match. The two ordering parameters in line 5 and 6 and 21 and 22 specify synchronization order for success and failure cases respectively at lines 8 and 12. This directly implements the CAS operations described in multiple algorithms.

#### 6.3.3. Swap Operations

Swap unconditionally replaces a value and returns the previous value, implemented as swap (new\_value, ordering), as shown in listing 6.10. As an example the David Queue and Drescher Queue is used.

Listing 6.10: Unconditional atomic swap operations

```
1  // From David Queue - unconditional slot update
2  unsafe fn swap(&self, new_val: usize) -> usize {
3    self.value.swap(new_val, Ordering::AcqRel)
4  }
5  
6  // From Drescher Queue - atomic pointer swap
7  let prev_tail = self.tail.swap(new_node_ptr, Ordering::AcqRel);
8  
9  // From DrescherQueue - simpler FAS primitive
10  let prev_tail_ptr = self.tail.swap(new_node_ptr, Ordering::AcqRel);
11  (*prev_tail_ptr).next.store(new_node_ptr, Ordering::Release);
```

Swap operations are useful when the previous value is needed but the update is unconditional. The DrescherQueue uses swap to implement its simple enqueue operation (line 10), atomically updating the tail pointer and then linking the previous tail to the new node, exactly as specified in the Drescher algorithm in section 5.2.2.

# 6.3.4. Load and Store with Memory Ordering

Simple loads and stores also require consideration of memory ordering to ensure correct synchronization according to the algorithms in chapter 5, as demonstrated in the general example of listing 6.11.

Listing 6.11: Memory ordering for loads and stores

The acquire-release pattern is particularly important. A release store in line 9 synchronizes with an acquire load in line 2 of the same location, ensuring that all writes before the release store are visible to any thread that sees the acquire load. This pattern is used in all queues to

ensure correct ordering to the producer-consumer relationship, implementing the memory barriers described in algorithms like Lamport Queue (section 5.2.1) and others.

## 6.3.5. Memory Fences

To still ensure correct data ordering without any memory operation rust provide memory fencec seen in the wCQ rust implementation, as shown in listing 6.12.

Listing 6.12: Explicit memory fence usage

```
1 // From WCQueue - ensuring visibility across operations
2 fence(Ordering::SeqCst);
3 let packed = entry.value.load(Ordering::SeqCst);
4 let e = EntryPair::unpack_entry(packed);
6 if condition {
     fence(Ordering::SeqCst); // Ensure all prior operations complete
      match entry.value.compare_exchange_weak(
10
       packed,
11
        new_packed,
         Ordering::SeqCst,
        Ordering::SeqCst,
15
        Ok (_) => {
           fence(Ordering::SegCst); // Ensure visibility before
16
      → proceeding
17
        }
18
      }
19 }
```

Fences ensure ordering between operations that might not otherwise synchronize. The wCQ implementation uses sequential consistency fences (lines 2, 7, 16) to ensure correctness in its complex algorithm. These kind of fences are used in all queue implementations since for IPC this was necessary for correctness.

# 6.3.6. Versioned Compare and Swap (CAS) (Simulating Load-Linked and Store-Conditional (LL/SC))

Some algorithms assume LL/SC primitives, which x86-64 does not provide. The Jayanti-Petrovic queue from section 5.2.2 simulates LL/SC using versioned CAS, as shown in listing 6.13.

Listing 6.13: Versioned CAS for LL/SC simulation

```
impl CompactMinInfo {
      fn to_u64(self) -> u64 {
10
           ((self.version as u64) << 32)
11
               | ((self.ts_val as u64) << 16)
12
               | ((self.ts_pid as u64) << 8)
13
               | (self.leaf_idx as u64)
14
15
16 }
17
unsafe fn cas_min_info(&self, old_compact: CompactMinInfo,
19
                          new_min_info: MinInfo) -> bool {
      // Increment version on every update
20
      let new_compact = CompactMinInfo::from_min_info(
21
22
          new_min_info,
23
          old_compact.version + 1
24
      );
25
      self.compact_min_info.compare_exchange(
26
27
          old_compact.to_u64(),
28
          new_compact.to_u64(),
          Ordering::AcqRel,
29
          Ordering::Acquire
30
31
      ).is ok()
32 }
```

The version counter in line 3 prevents the ABA problem where a value changes from A to B and back to A between observations. By incrementing the version on every update seen in line 23, even if the logical value returns to a previous state, the version ensures the CAS will fail, simulating LL/SC semantics as required by the Jayanti-Petrovic algorithm. This is done in every queue rust implementation that requires LL/SC semantics.

#### 6.3.7. Unsafe Blocks

Rust's memory safety guarantees to prevent data races by ensuring that either multiple readers or a single writer can access data at any time. However, the wait-free algorithms in chapter 5 require to bypass these restrictions. With the use of unsafe blocks the Rust compiler gets indicated that the blocks memory safety is handled by the implementation itself. The try\_enq\_inner function of wCQs Rust implementation in listing 6.14 demonstrates why unsafe blocks are necessary.

Listing 6.14: Wait-free synchronization requiring unsafe

```
// Multiple threads may execute this concurrently
unsafe fn try_enq_inner(&self, wq: &InnerWCQ, entries_offset: usize,
index: usize) -> Result<(), u64> {

let tail = wq.tail.cnt.fetch_add(1, Ordering::AcqRel);

let j = Self::cache_remap(tail as usize, wq.capacity);
```

```
let entry = self.get_entry(wq, entries_offset, j);
               let packed = entry.value.load(Ordering::Acquire);
               let e = EntryPair::unpack_entry(packed);
10
11
               // Check if slot is available
12
               if e.cycle < Self::cycle(tail, wq.ring_size) &&</pre>
13
14
                   (e.is_safe || wq.head.cnt.load(Ordering::Acquire) <= tail)
      ∽ &&
                   (e.index == IDX_EMPTY || e.index == IDX_BOTTOM) {
15
16
17
                    // Attempt to claim slot with CAS
                   match entry.value.compare_exchange_weak(
18
                        packed,
19
                        new_packed,
20
                        Ordering::SeqCst,
21
22
                        Ordering::SeqCst,
23
24
                        Ok (_) => return Ok (()),
25
                        Err(_) => continue, // Retry
26
                    }
27
           }
28
29
30
       // get_entry uses raw pointer arithmetic
31
       unsafe fn get_entry(&self, _wq: &InnerWCQ, entries_offset: usize,
32
33
                           idx: usize) -> &EntryPair {
           let entries = self.base_ptr.add(entries_offset) as *const

→ EntryPair;

           &*entries.add(idx) // Dereference raw pointer
35
36
```

One reason for an unsafe block is raw pointer dereferencing seen in lines 32 to 34. The get\_entry function performs pointer arithmetic on base\_ptr and dereferences the result which is needed for shared memory. The compiler cannot verify that the calculated address is valid or that no data races occur. The Rust compiler also does not allow concurrent access of multiple writer threads or processes. try\_enq\_inner beginning at line 2 is implementated so that multiple processes can simultaneously call it. Each process, atomically increments the tail to get a unique position in line 4, then accesses potentially the same entry due to cache remapping in lines 5 and 7, and finally attempts to modify the entry in line 18. The Rust compiler cannot verify too that this access is safe, so the developer of this implementation has to indicate to the compiler that this is safe by using an unsafe block.

#### 6.4. Validation

Part of the objective is also to ensure the correctness of the implemented algorithms, unit and miri tests were performed. The unit tests validate the basic functionality of each queue,

ensuring that operations like enqueue and dequeue work as expected. Miri tests were used to check for undefined behavior in concurrent scenarios, ensuring that the algorithms behave correctly under extreme contention. This section will generally describe how the tests were implemented and what they validate, without going into the details of each test case.

## 6.4.1. Basic Operations

Every queue implementation was validated for fundamental operations including initialization, push, pop, and state queries (is\_empty, is\_full). For example, the basic operation test pattern was implemented as shown in listing 6.15:

Listing 6.15: Basic operation test pattern

```
1 // Test empty queue state
2 assert!(queue.is_empty());
assert!(queue.pop().is_err());
5 // Test single element operations
6 queue.push(42).unwrap();
7 assert!(!queue.is_empty());
8 assert_eq! (queue.pop().unwrap(), 42);
9 assert!(queue.is_empty());
11 // Test multiple elements
12 for i in 0..10 {
     queue.push(i).unwrap();
13
14 }
15 for i in 0..10 {
      assert_eq! (queue.pop().unwrap(), i);
16
```

Lines 2 to 3 in listing 6.15 test the initial empty state and check that pop operations fail correctly on empty queues. The single element test in lines 6 to 9 tests the state change from empty to non-empty and back, with line 8 testing that the pushed value is correctly retrieved. Lines 12 to 17 test that FIFO ordering is maintained for multiple elements.

#### 6.4.2. Capacity and Boundary Tests

Capacity limits also had to be testet, so it can be ensured, that the capacities work correctly. Special attention was given to queues with buffering mechanisms like BIFFQ and MultiPush queue, which required explicit flushing operations.

Listing 6.16: Capacity limit test pattern

```
1 // Test pushing up to capacity
2 let mut pushed = 0;
3 for i in 0..capacity {
4  match queue.push(i) {
5  Ok(_) => pushed += 1,
```

```
Err(_) => break,

passert!(pushed > 0, "Should_push_at_least_one_item");

// Verify queue rejects items when full
assert!(!queue.available() || queue.push(999).is_err());

// Test space recovery after pop

if pushed > 0 {
    assert!(queue.pop().is_ok());
    assert!(queue.available());
    assert!(queue.push(888).is_ok());
}
```

In listing 6.16 lines 3 to 8 test filling the queue to capacity, counting successful pushes. Line 9 tests that at least one item could be pushed. Line 12 tests that a full queue either reports no available space or rejects push attempts. Lines 15 to 19 test that after removing an element, space becomes available for new items.

For queues with buffering mechanisms, additional testing was required:

Listing 6.17: Buffered queue capacity test

```
1 // BiffQ attempts to push beyond capacity
2 for i in 0..BIFFQ_CAPACITY + 100 {
      match queue.push(i) {
3
          Ok(_) => pushed_total += 1,
4
          Err(_) => {
5
              // Flush local buffer to main queue
              let _ = queue.flush_producer_buffer();
              if queue.push(i).is_err() {
                  break; // No space in main queue
              } else {
11
                  pushed_total += 1;
12
13
          }
14
      // Periodic flushing every 32 items
15
      if i % 32 == 31 {
16
17
          let _ = queue.flush_producer_buffer();
18
19 }
20 // Final flush to ensure all buffered items are visible
21 let _ = queue.flush_producer_buffer();
23 // Verify capacity behavior based on how full the queue got
24 if pushed_total >= BIFFQ_CAPACITY - 32 {
25
      // Nearly full: test pop/push with limited space
26
      assert!(queue.pop().is_ok());
      // Try to push after making space
27
for _ in 0..10 {
```

```
let _ = queue.flush_producer_buffer();
30
           if queue.push(99999).is_ok() {
31
              break;
32
           let _ = queue.pop(); // Make more space
33
      }
34
35 } else {
      // Partially full: verify basic push/pop works
36
37
      assert!(queue.pop().is_ok());
      assert!(queue.push(99999).is_ok());
39 }
```

The BIFFQ test in listing 6.17 tests the buffering system. When push fails in line 5, line 7 flushes the local buffer to the main queue. If the retry in line 8 still fails, it means the main queue lacks space. Lines 16 to 18 periodically flushes every 32 items (the buffer size). The test in lines 24 to 39 checks different behaviors based on how full the queue is: lines 24 to 33 test the case where the main queue might not have room for a complete buffer flush, while lines 35 to 39 test basic operations when the queue is only partially full.

# 6.4.3. Memory Alignment Verification

Since the implementations target shared memory with specific alignment requirements, tests as in listing 6.18 verified proper memory alignment for all queue structures:

Listing 6.18: Memory alignment verification test

```
1 // Allocate memory with specific alignment
2 let layout = Layout::from_size_align(size, alignment)
      .expect("Invalid_layout");
4 let ptr = unsafe { alloc_zeroed(layout) };
6 // Verify pointer alignment
7 assert_eq!(
      ptr as usize % alignment, 0,
      "Memory_not_aligned_to_{} bytes", alignment
10 );
11
12 // Initialize queue with aligned memory
13 let queue = unsafe {
14
      <$queue_type>::init_in_shared(ptr, capacity)
15 };
16
17 // For YangCrummeyQueue requiring 128-byte alignment
18 let queue_offset = sync_size;
19 let queue_offset_aligned = (queue_offset + 127) & !127;
20 let queue_ptr = unsafe { shm_ptr.add(queue_offset_aligned) };
21 assert_eq! (
      queue_ptr as usize % 128, 0,
22
      "Queue_not_properly_aligned_to_128_bytes"
23
24 );
```

Lines 2 to 4 in listing 6.18 create memory with the required alignment and allocate it so that lines 7 to 10 can test that the allocation has the correct alignment using modulo arithmetic. For YMC, lines 18 and 19 calculate the aligned offset, where (offset + 127) & !127 rounds up to the next 128-byte boundary. Lines 21 to 24 test that the final queue pointer has the required 128-byte alignment.

Position-independent addressing was verified in listing 6.19 through shared memory tests:

Listing 6.19: Position-independent addressing test

```
1 // Map shared memory at arbitrary address
2 let shm_ptr = unsafe {
     libc::mmap(
         std::ptr::null_mut(), // Let OS choose address
         libc::PROT_READ | libc::PROT_WRITE,
         libc::MAP_SHARED | libc::MAP_ANONYMOUS,
          -1,
         0,
      ) as *mut u8
10
11 };
13 // Initialize queue - must work at any address
14 let queue = unsafe {
15
      Queue::init_in_shared(shm_ptr, capacity)
16 };
17
18 // Verify queue operates correctly regardless of base address
19 queue.push(42).unwrap();
20 assert_eq!(queue.pop().unwrap(), 42);
```

Line 4 in listing 6.19 passes null to let the OS choose the memory address and lines 6 and 7 specify shared anonymous memory for inter-process access. Lines 14 and 15 initializes the at any address. Lines 19 and 20 test that the queue works correctly regardless of its memory location.

#### **Memory Pool Management**

The pre-allocated memory pools of the queues were tested for correct allocation, recycling, and pool exhaustion handling:

Listing 6.20: Memory pool management test

```
1 // Test pool allocation and recycling
2 unsafe {
3     // Allocate from pool
4    let seg1: *mut Segment<i32> = queue.new_segment(1);
5    assert!(!seg1.is_null());
6    assert_eq!((*seg1).id, 1);
7
8     // Return to pool
```

```
queue.release_segment_to_pool(seg1);
10
11
       // Test pool exhaustion
12
      let mut segments = vec![];
       for i in 2..segment_pool_capacity as u64 {
13
           let seg = queue.new_segment(i);
14
           if !seg.is_null() {
15
               segments.push(seg);
17
           } else {
              break; // Pool exhausted
18
19
           }
      }
20
21
      // Return all to pool
22
      for seg in segments {
23
           queue.release_segment_to_pool(seg);
24
25
       }
26 }
27
28 // Test free list reuse in Jiffy Queue
29 let free_head = self.node_array_slice_free_list_head
       .load(Ordering::Acquire);
31 if !free_head.is_null() {
      // Reuse from free list
32
      let next_free = (*(free_head as *mut AtomicPtr<Node<T>>))
33
           .load(Ordering::Acquire);
34
35
      if self.node_array_slice_free_list_head.compare_exchange(
37
          free_head,
38
          next_free,
          Ordering::AcqRel,
39
          Ordering::Acquire
40
41
      ).is_ok() {
          return free_head; // Successfully reused
42
43
44 }
```

Lines 4 to 6 in listing 6.20 test basic allocation from the pool and test that the segment is properly initialized. Line 9 tests returning the segment to the pool. Lines 12 to 20 test pool exhaustion by allocating until <code>new\_segment</code> returns null in line 18. Lines 23 to 25 test that segments can be returned to the pool. Lines 29 to 44 test the free list implementation in Jiffy Queue, where lines 36 to 41 test atomic removal of the free list head using compare-exchange. Since we only test, that the allocations work and can be used, assertions were not used, since only correct behavior is testet.

### 6.4.4. Concurrent Operation Tests

Concurrent tests validated the correctness of queue operations under contention. Different kinds of tests were implemented to stress the queues in various ways:

#### **Producer-Consumer Patterns**

Tests spawned separate threads for producers and consumers to test correct concurrent operation as seen in listing 6.21:

Listing 6.21: Concurrent test pattern

```
1 let barrier = Arc::new(Barrier::new(num_threads));
2 let mut handles = vec![];
4 // Spawn producer threads
5 for tid in 0..num_producers {
      let barrier_clone = barrier.clone();
      let handle = thread::spawn(move | | {
          barrier_clone.wait(); // Synchronize start
          for i in 0..items_per_thread {
              queue.push(tid * items_per_thread + i, tid).unwrap();
11
      });
      handles.push(handle);
13
14 }
15
16 // Wait for all threads and verify results
17 for handle in handles {
      handle.join().unwrap();
18
19 }
```

Line 1 in listing 6.21 creates a barrier to synchronize thread startup. Line 8 ensures all threads start at the same time, creating maximum contention. Line 10 generates unique values per producer using  $\verb|tid| * items_per_thread| + i to test data integrity.$  Lines 17 to 19 wait for all producers to complete before verification. This is just a simple test to ensure that the queues can handle concurrent operations without deadlocks or data corruption.

#### **Stress Tests**

In listing 6.22 high-contention scenarios were tested with multiple producers and consumers operating simultaneously:

Listing 6.22: High-contention stress test

```
1  // Stress test with multiple concurrent producers and consumers
2  let num_threads = 4;
3  let items_per_thread = 1000;
4  let produced = Arc::new(AtomicUsize::new(0));
5  let consumed = Arc::new(AtomicUsize::new(0));
6  let done = Arc::new(AtomicBool::new(false));
7  // Spawn producer threads
9  for tid in 0..num_threads / 2 {
10    let p = Arc::clone(&produced);
11  let handle = thread::spawn(move || {
```

```
for i in 0..items_per_thread {
               let value = tid * items_per_thread + i;
13
               let mut retries = 0;
14
               while queue.push(value, tid).is_err() && retries < 1000 {</pre>
15
                    retries += 1;
16
                    thread::yield_now();
17
18
               if retries < 1000 {
19
                   p.fetch_add(1, Ordering::Relaxed);
20
21
22
       });
23
24
       handles.push(handle);
25 }
26
27 // Spawn consumer threads
28 for tid in num_threads / 2..num_threads {
29
       let c = Arc::clone(&consumed);
30
       let d = Arc::clone(&done);
       let handle = thread::spawn(move || {
31
           let mut consecutive_failures = 0;
32
33
           loop {
               if queue.pop(tid).is_ok() {
34
                   c.fetch_add(1, Ordering::Relaxed);
35
                    consecutive_failures = 0;
36
               } else {
37
                    consecutive_failures += 1;
38
                    if d.load(Ordering::Relaxed) &&
                        consecutive_failures > 100 {
40
41
                        break;
42
43
                    thread::yield_now();
               }
44
45
46
       });
       handles.push(handle);
47
48 }
50 // Let threads run under contention
51 thread::sleep(Duration::from_millis(100));
52 done.store(true, Ordering::Relaxed);
53
54 // Verify no items lost
55 let produced_count = produced.load(Ordering::Relaxed);
16 let consumed_count = consumed.load(Ordering::Relaxed);
57 assert! (
       consumed_count >= produced_count * 9 / 10,
58
59
       "Should_consume_at_least_90%_of_produced_items"
60 );
```

Lines 4 to 6 in listing 6.22 create atomic counters to track production and consumption across threads. Lines 15 to 17 test retry behavior with yield to handle temporary failures. Lines 19 and 20 only count successfully pushed items. Lines 33 to 45 test the consumer loop that continues until signaled to stop and experiences many failures in lines 39 to 41. Lines 51 and 52 signal consumers to terminate. Lines 55 to 60 test that at least 90% of produced items were consumed.

In the following listing 6.23 correct FIFO ordering was tested:

Listing 6.23: FIFO ordering verification under stress

```
1 // Collect all dequeued items
2 let mut items = Vec::new();
3 while let Some(item) = queue.pop() {
      items.push(item);
4
5 }
7 // Verify correct count
8 assert_eq!(items.len(), NUM_PRODUCERS * ITEMS_PER_PRODUCER);
10 // Sort and verify no duplicates or missing items
items.sort();
12 for (i, &item) in items.iter().enumerate() {
13
      assert_eq!(item, i, "Missing_or_duplicate_items_detected");
14 }
15
16 // For strict FIFO queues, verify ordering per producer
17 for producer_id in 0..num_producers {
      let producer_items: Vec<_> = items.iter()
18
          .filter(|\&\&x| \times / 1000 == producer_id)
19
          .collect();
20
21
      // Items from same producer must maintain order
22
23
      for window in producer_items.windows(2) {
24
          assert!(window[0] < window[1],</pre>
25
                   "FIFOuorder_violated_for_producer_{{}}", producer_id);
26
      }
27 }
```

Lines 2 to 5 in listing 6.23 collect all items from the queue. Lines 11 to 14 test for missing or duplicate items by checking sequential values after sorting. Lines 17 to 20 filter items by producer. Lines 23 to 26 test that items from the same producer maintain their order.

#### 6.4.5. Inter-Process Communication (IPC) Tests

One important test is that the queues' behavior in true IPC scenarios remains correct using process forking. These tests verify that under process contention the queues still operate correctly, properly handle shared memory regions, and that atomic operations are visible between processes. The IPC tests followed a consistent pattern using fork() to create separate processes as seen in listing 6.24:

#### Listing 6.24: IPC test structure

```
match unsafe { fork() } {
      Ok(ForkResult::Child) => {
           // Producer process
3
           for i in 0..NUM_ITEMS {
4
               loop {
5
                   match queue.push(i) {
6
                       Ok (_) => break,
                       Err(_) => thread::yield_now(),
8
9
10
               }
11
12
           unsafe { libc::_exit(0) };
13
       }
14
       Ok(ForkResult::Parent { child }) => {
          // Consumer process
15
           let mut received = Vec::new();
16
           while received.len() < NUM_ITEMS {</pre>
17
               match queue.pop() {
18
19
                   Ok(item) => received.push(item),
                   Err(_) => thread::yield_now(),
21
22
           // Verify all items received in order
23
24
           waitpid(child, None).expect("waitpid_failed");
25
       }
26 }
```

Line 2 in listing 6.24 creates a child process that shares the queue's memory with the parent. Lines 5 to 10 test the producer's retry loop, yielding on failure in line 8. Line 12 uses <code>\_exit(0)</code> to avoid cleanup handlers that might affect shared memory. Lines 17 to 21 test the consumer loop collecting all items. Line 24 waits for the child process to complete before final verification.

### 6.4.6. Special Feature Validation

Algorithm-specific features required targeted validation:

#### **Buffering Mechanisms**

Queues with local buffering like BIFFQ and MultiPush were tested like in listing 6.25 for correct flush operations and visibility of buffered items:

Listing 6.25: Buffer mechanism test

```
1 // Test BiffQ flush operations
2 for i in 0..10 {
3    queue.push(i).unwrap();
4 }
5
```

```
6 // Verify items not visible before flush
7 assert_eq!(queue.cons.shared_count.load(Ordering::Acquire), 0);
9 // Flush and verify visibility
10 let flushed = queue.flush_producer_buffer().unwrap();
n assert!(flushed > 0);
13 // Now items should be visible to consumer
14 for i in 0..10 {
      assert_eq!(queue.pop().unwrap(), i);
16 }
17
18 // Test automatic flush on buffer overflow
19 for i in 0..32 { // Local buffer size
20
      queue.push(i).unwrap();
21 }
22 // Should auto-flush when buffer full
assert_eq!(queue.local_count.load(Ordering::Relaxed), 0);
```

Lines 2 to 4 in listing 6.25 push items into the local buffer. Line 7 tests that items remain invisible to consumers before flushing. Lines 10 and 11 test explicit buffer flushing. Lines 14 to 16 test that items are now consumable in correct order. Lines 19 to 23 test automatic flushing when the 32-item buffer fills.

### **Helper Thread Coordination**

Verma's queue from section 5.2.4 with its helper thread requires special tests seen in listing 6.26 to verify that the helper thread functions correctly:

Listing 6.26: Helper thread coordination test

```
n match unsafe { fork() } {
      Ok(ForkResult::Child) => {
         // Child runs helper thread
          queue.run_helper();
          std::process::exit(0);
6
      Ok(ForkResult::Parent { child }) => {
7
          thread::sleep(Duration::from_millis(20));
          // Test operations with helper
10
          assert!(queue.push(42, 0).is_ok());
11
          thread::sleep(Duration::from_millis(10));
12
13
          match queue.pop(0) {
14
              Ok(val) => assert_eq!(val, 42),
15
              Err(_) => panic!("Pop_should_succeed_with_helper"),
16
17
          // Stop helper and verify cleanup
          queue.stop_helper();
```

```
waitpid(child, None).unwrap();

waitpid(child, None).unwrap();

// Test without helper - queue should still be functional
assert!(queue.is_empty(), "Queue_operational_without_helper");
```

Line 4 in listing 6.26 starts the helper thread in a separate process. Line 8 allows time for helper initialization. Lines 11 to 17 test that operations complete successfully with helper assistance. Line 12 provides time for the helper to process the request. Lines 20 and 21 test proper helper termination and cleanup. Finally, line 25 tests that the queue remains functional without a helper thread.

#### 6.4.7. Miri Validation

Miri tests provided validation of memory safety in concurrent scenarios. In the test folder of the repository there are miri test files additionally to the unit test files. While structurally similar to the regular unit tests, Miri tests had to use significantly reduced parameters and simplified concurrency patterns to accommodate Miri's execution overhead. The advantage of Miri tests are, that Miri simulates extreme contention leading to detect undefined behavior easier. Miri tests will fail if undefined behavior like data races happens.

#### 6.4.8. Test Coverage

As we can see in fig. 6.1 a total function coverage of 81.12% and total line coverage of 70.03% was achieved, showing that most of the code paths were executed during testing. Branch coverage only lies at 44.78%, which is still fine in concurrent programming.

Figure 6.1.: Total Coverage of the Rust implementation

Filename	<b>Function Coverage</b>	Line Coverage	Region Coverage	<b>Branch Coverage</b>
<pre>mpmc/feldman_dechev_queue.rs</pre>	82.93% (34/41)	66.56% (404/607)	67.20% (635/945)	38.97% (53/136)
<pre>mpmc/kogan_petrank.rs</pre>	83.87% (26/31)	90.44% (350/387)	92.91% (577/621)	81.71% (67/82)
mpmc/turn_queue.rs	80.00% (16/20)	83.53% (284/340)	83.41% (513/615)	58.82% (40/68)
<pre>mpmc/verma_wf.rs</pre>	80.95% (17/21)	82.30% (200/243)	78.81% (331/420)	62.50% (20/32)
<pre>mpmc/wcq_queue.rs</pre>	65.22% (30/46)	42.57% (602/1414)	40.55% (912/2249)	21.69% (82/378)
<pre>mpmc/ymc_queue.rs</pre>	81.82% (27/33)	65.28% (361/553)	63.58% (611/961)	30.00% (36/120)
mpsc/dqueue.rs	94.74% (18/19)	73.70% (426/578)	78.44% (753/960)	52.44% (86/164)
mpsc/drescher_queue.rs	100.00% (12/12)	97.39% (112/115)	98.60% (211/214)	80.00% (8/10)
<pre>mpsc/jayanti_petrovic_queue.rs</pre>	86.49% (32/37)	84.98% (345/406)	88.91% (489/550)	57.69% (30/52)
mpsc/jiffy_queue.rs	90.91% (20/22)	63.45% (486/766)	65.48% (715/1092)	40.91% (90/220)
mpsc/sesd_jp_queue.rs	100.00% (6/6)	90.67% (68/75)	93.13% (122/131)	66.67% (8/12)
<pre>spmc/david_queue.rs</pre>	70.00% (14/20)	55.69% (137/246)	56.08% (212/378)	29.17% (7/24)
spsc/biffq.rs	88.89% (16/18)	85.89% (207/241)	84.81% (335/395)	76.32% (29/38)
spsc/blq.rs	85.71% (12/14)	78.05% (128/164)	77.63% (177/228)	62.50% (10/16)
spsc/bqueue.rs	64.29% (9/14)	87.59% (120/137)	88.70% (212/239)	91.67% (22/24)
spsc/dspsc.rs	77.78% (7/9)	92.45% (98/106)	93.78% (181/193)	50.00% (4/8)
spsc/ffq.rs	81.82% (9/11)	87.76% (86/98)	86.74% (157/181)	66.67% (8/12)
spsc/iffq.rs	88.24% (15/17)	87.43% (153/175)	86.64% (253/292)	81.82% (18/22)
<pre>spsc/lamport.rs</pre>	69.23% (9/13)	81.93% (68/83)	80.65% (125/155)	100.00% (4/4)
spsc/llq.rs	80.00% (8/10)	83.33% (95/114)	85.08% (154/181)	100.00% (8/8)
spsc/mspsc.rs	69.23% (9/13)	82.05% (96/117)	83.64% (184/220)	66.67% (8/12)
<pre>spsc/sesd_jp_spsc_wrapper.rs</pre>	87.50% (7/8)	92.71% (89/96)	91.37% (127/139)	75.00% (9/12)
spsc/uspsc.rs	80.00% (8/10)	91.16% (134/147)	93.26% (249/267)	65.00% (13/20)
Totals	81.12% (361/445)	70.05% (5049/7208)	70.83% (8235/11626)	44.78% (660/1474)

To finish the objective of this thesis at last a setting needs to be build were these algorithms are used for IPC over shared memory. This setting was also used to benchmark the performance of these algorithms to Identify the best performing wait-free algorithms that can be used. In the [50] the folder benches includes the setting and benchmark of these algorithms. As seen as before these algorithms were divided into 4 categories, MPMC, MPSC, SPMC and SPSC. Therefore 4 different IPC over shared memory settings were build to analyze firstly if all algorithms work as intended and secondly to compare the performance of all algorithms. Eventhough SPMC category only has one algorithm, the build setting was still interesting to check and validate if the algorithm works as intended. After identifying the best algorithm 3 more settings were build. One setting was to see if the SPMC queue or the best performing queues of the other categories would be faster for the SPSC category. The same was done for the MPSC category by checking if the best MPMC queue or the best MPSC queue would perform better. Finally for the SPMC category the same was done to check if the best MPMC or SPMC queue would be better. The best SPSC queue could not be testet for higher producer or consumer numbers, since the missing helping structures and missing atomic primitives would lead to deadloccks or inconsistent data. The benchmarks were done on a system with an Intel i7-12700H x86 processer with 14 cores. The benchmarks were implemented with the help of the criterion crate, which is a benchmarking library for Rust. This chapter will show in general how the benchmarks settings were impplemented to understand the results later.

## 7.1. Benchmark Structure

All benchmarks follow a consistent architecture to ensure fair comparison between queue implementations. The benchmarks measure the time taken for producers and consumers to exchange a fixed number of items through each queue implementation using IPC over shared memory. This section explains the general benchmark structure using the MPMC benchmark as a representative example, as the same patterns apply to all queue categories. Not every line will be explained, but the most important lines will be explained to understand the general structure of the benchmarks.

## 7.1.1. Benchmark Parameters and Configuration

Before examining the benchmark implementation details, it is important to understand the benchmark parameters that control the test scenarios. These constants define the scale and scope of the performance measurements, as shown in listing 7.1.

Listing 7.1: Benchmark configuration constants

```
const ITEMS_PER_PROCESS_TARGET: usize = 170_000;
const PROCESS_COUNTS_TO_TEST: &[(usize, usize)] = &[(1, 1), (2, 2), (4, 4), (6, 6)];
const MAX_BENCH_SPIN_RETRY_ATTEMPTS: usize = 100_000_000_000;
```

Line 1 sets the number of items each producer process will generate. The value of 170,000 items provides sufficient workload to measure performance while keeping individual benchmark runs reasonable in duration. Line 2 defines the producer and consumer configurations to test as tuples. The array  $[\ (1,\ 1),\ (2,\ 2),\ (4,\ 4),\ (6,\ 6)\ ]$  tests symmetric configurations from single producer and single consumer up to 6 producers and 6 consumers, allowing analysis of scalability. Line 3 sets the maximum spin attempts before considering an operation failed. This large value ensures that wait-free operations have sufficient opportunity to complete.

For other benchmark categories, these constants are adjusted appropriately. For example, the MPSC benchmark uses:

Listing 7.2: MPSC-specific configuration

```
const ITEMS_PER_PRODUCER_TARGET: usize = 500_000;
const PRODUCER_COUNTS_TO_TEST: &[usize] = &[1, 2, 4, 8, 14];
```

The MPSC configuration tests up to 14 producers with a single consumer, using more items per producer to ensure the consumer remains busy throughout the benchmark. Similarly, SPMC and SPSC benchmarks have their own tailored parameters to effectively measure their specific use-cases.

# 7.1.2. Benchmark Interface Implementation

Each queue implementation must provide a uniform interface for benchmarking. This is achieved through a common trait that abstracts the queue-specific operations, as shown in listing 7.3. The following pop and push traits implement the dequeue and enqueue operations respectively for the queues.

Listing 7.3: Benchmark trait for MPMC queues

```
1 trait BenchMpmcQueue<T: Send + Clone>: Send + Sync + 'static {
      fn bench_push(&self, item: T, process_id: usize) -> Result<(), ()>;
      fn bench_pop(&self, process_id: usize) -> Result<T, ()>;
3
      fn bench_is_empty(&self) -> bool;
4
      fn bench_is_full(&self) -> bool;
5
6 }
8 // Example implementation for YangCrummeyQueue
9 impl<T: Send + Clone + 'static> BenchMpmcQueue<T> for YangCrummeyQueue<T>
      ← {
      fn bench_push(&self, item: T, process_id: usize) -> Result<(), ()> {
10
          self.enqueue(process_id, item)
11
```

```
14
       fn bench_pop(&self, process_id: usize) -> Result<T, ()> {
15
           self.dequeue(process_id)
16
17
       fn bench_is_empty(&self) -> bool {
18
           self.is_empty()
19
20
21
22
       fn bench_is_full(&self) -> bool {
23
           false // YangCrummeyQueue has unbounded capacity
24
25 }
```

The trait in lines 1 to 6 defines a common interface that all MPMC queues must implement. The process\_id parameter in lines 2 and 3 allows queues to distinguish between different processes, which is necessary for some algorithms. Lines 9 to 24 show how the YMC queue maps its specific methods to the common interface. The bench\_is\_full method in line 23 returns false for queues with unbounded capacity. This mapping is done for all queues in the respective categories, so that the benchmarks can be run with all queues without changing the benchmark code to to compare fairly.

# 7.1.3. Process Synchronization Infrastructure

Benchmarking concurrent algorithms requires careful synchronization to ensure all processes start simultaneously and coordinate their completion for fair comparisons. Two synchronization structures manage this coordination, as shown in listing 7.4.

Listing 7.4: Process synchronization structures

```
1 #[repr(C)]
2 struct MpmcStartupSync {
      producers_ready: AtomicU32,
      consumers_ready: AtomicU32,
      go_signal: AtomicBool,
6 }
8 impl MpmcStartupSync {
       fn new_in_shm(mem_ptr: *mut u8) -> &'static Self {
9
          let sync_ptr = mem_ptr as *mut Self;
10
           unsafe {
11
12
               ptr::write(
13
                   sync_ptr,
14
                   Self {
                       producers_ready: AtomicU32::new(0),
15
                       consumers_ready: AtomicU32::new(0),
16
                       go_signal: AtomicBool::new(false),
17
18
                   },
19
               );
20
               &*sync_ptr
```

```
22
23
24
      fn shared_size() -> usize {
           std::mem::size_of::<Self>()
25
26
27 }
28
29 #[repr(C)]
30 struct MpmcDoneSync {
31
      producers_done: AtomicU32,
32
      consumers_done: AtomicU32,
33
      total_consumed: AtomicUsize,
```

The MpmcStartupSync structure in lines 1 to 6 coordinates the startup phase. Producers increment producers\_ready in line 3 when ready, consumers increment consumers\_ready in line 4, and all processes wait for go\_signal in line 5 before starting. The new\_in\_shm method in lines 9 to 22 initializes the structure directly in shared memory using placement new. The MpmcDoneSync structure in lines 29 to 34 tracks completion, with total\_consumed in line 33 which is used to verify that no items were lost during the benchmark.

#### 7.1.4. Benchmark Execution Framework

The core benchmark logic is implemented in a generic function that handles process creation, execution, and measurement, as demonstrated in listing 7.5.

Listing 7.5: Generic benchmark execution function

```
1 fn fork_and_run_mpmc_with_helper<Q, F>(
      queue_init_fn: F,
2
3
      num_producers: usize,
      num_consumers: usize,
      items_per_process: usize,
5
      needs_helper: bool,
7 ) -> Duration
8 where
      Q: BenchMpmcQueue<usize> + 'static,
9
      F: FnOnce() -> (&'static Q, *mut u8, usize),
10
11 {
12
      let total_items = num_producers * items_per_process;
13
14
      // Initialize queue in shared memory
      let (q, q_shm_ptr, q_shm_size) = queue_init_fn();
16
17
      // Allocate synchronization structures
18
      let startup_sync_size = MpmcStartupSync::shared_size();
19
      let startup_sync_shm_ptr = unsafe { map_shared(startup_sync_size) };
      let startup_sync = MpmcStartupSync::new_in_shm(startup_sync_shm_ptr);
20
```

```
21
       let mut producer_pids = Vec::with_capacity(num_producers);
22
       let mut consumer_pids = Vec::with_capacity(num_consumers);
23
24
       // Fork producer processes
25
       for producer_id in 0..num_producers {
26
           match unsafe { fork() } {
27
28
               Ok (ForkResult::Child) => {
29
                    // Signal ready and wait for go signal
                    startup_sync.producers_ready.fetch_add(1,
30
      → Ordering::AcqRel);
                   while !startup_sync.go_signal.load(Ordering::Acquire) {
31
                        std::hint::spin_loop();
32
33
                    }
34
                    // Produce items
35
36
                    for i in 0..items_per_process {
37
                        let item_value = producer_id * items_per_process + i;
                        while q.bench_push(item_value, producer_id).is_err() {
                            std::hint::spin_loop();
39
40
41
                    }
42
                   unsafe { libc::_exit(0) };
43
44
               Ok(ForkResult::Parent { child }) => {
45
                   producer_pids.push(child);
46
47
               Err(e) => panic!("Fork_failed:_{{}}", e),
48
49
           }
50
       }
51
       // Wait for all processes to be ready
52
       while startup_sync.producers_ready.load(Ordering::Acquire) <</pre>
53
      → num_producers as u32
           || startup_sync.consumers_ready.load(Ordering::Acquire) <</pre>
54
      → num_consumers as u32
           std::hint::spin_loop();
57
58
       // Start timing and signal processes to begin
59
       let start_time = std::time::Instant::now();
60
       startup_sync.go_signal.store(true, Ordering::Release);
61
62
       // Wait for completion
63
       for pid in producer_pids {
64
65
           waitpid(pid, None).expect("waitpid_failed");
66
67
68
       start_time.elapsed()
```

69 }

The function signature in lines 1 to 10 accepts a queue initialization function and benchmark parameters. The <code>needs\_helper</code> parameter in line 6 supports queues like Verma's that require a helper thread. Line 15 initializes the queue using the provided function, which returns the queue reference and shared memory details. Lines 26 to 50 show the producer process creation where line 30 signals readiness, lines 31 to 33 implement ensures that every process waits for the go signal, and lines 36 to 41 produce items with retry logic. Lines 53 to 57 ensure all processes are ready before starting. Line 60 captures the start time immediately before signaling processes to begin in line 61. Lines 64 to 66 wait for all producer processes to complete before calculating the elapsed time in line 68.

# 7.1.5. Queue-Specific Benchmark Integration

Each queue type requires a specific benchmark function that integrates with the Criterion framework, as shown in listing 7.6.

Listing 7.6: Queue-specific benchmark function

```
1 fn bench_yang_crummey(c: &mut Criterion) {
2
      let mut group = c.benchmark_group("YangCrummeyMPMC_");
3
4
      for &(num_prods, num_cons) in PROCESS_COUNTS_TO_TEST {
           let items_per_process = ITEMS_PER_PROCESS_TARGET;
5
          let total_processes = num_prods + num_cons;
6
          group.bench_function(
               format!("{}P_{{}}C", num_prods, num_cons),
10
               |b: &mut Bencher| {
11
                   b.iter_custom(|_iters| {
12
      → fork_and_run_mpmc_with_helper::<YangCrummeyQueue<usize>, _>(
13
14
                                // Calculate required shared memory size
                               let bytes =
15
      YangCrummeyQueue::<usize>::shared_size(total_processes);
                               let shm_ptr = unsafe { map_shared(bytes) };
16
17
                                // Initialize queue in shared memory
18
19
                                let q = unsafe {
20
                                    YangCrummeyQueue::init_in_shared(shm_ptr,
      → total_processes)
21
                                };
22
23
                                (q, shm_ptr, bytes)
24
                           },
25
                           num_prods,
26
                           num_cons,
27
                           items_per_process,
28
                           false, // YangCrummey doesn't need helper
```

Line 2 creates a benchmark group with a descriptive name. Line 4 iterates through different producer/consumer configurations from the constant array PROCESS\_COUNTS\_TO\_TEST. Line 9 formats the benchmark name to indicate the configuration. Lines 11 to 30 use Criterion's iter\_custom method to measure custom timing, as the benchmark itself measures process execution time. The closure in lines 13 to 23 initializes the queue where line 15 calculates the exact shared memory size needed and line 16 allocates the shared memory region. After that lines 19 to 21 initialize the queue at the allocated address.

## 7.1.6. Consumer Process Implementation

The consumer processes follow a similar pattern but with additional logic to handle termination and verify correctness, as shown in listing 7.7.

Listing 7.7: Consumer process implementation

```
1 // Fork consumer processes
2 for consumer_id in 0..num_consumers {
3
      match unsafe { fork() } {
4
           Ok(ForkResult::Child) => {
5
               startup_sync.consumers_ready.fetch_add(1, Ordering::AcqRel);
6
               while !startup_sync.go_signal.load(Ordering::Acquire) {
7
                    std::hint::spin_loop();
8
9
               }
10
               let mut consumed_count = 0;
11
               let target_items = total_items / num_consumers;
12
               let extra_items = if consumer_id < (total_items %</pre>
13
      → num consumers) {
14
                   1
15
               } else {
16
                   Ω
17
               };
18
               let my_target = target_items + extra_items;
               let mut consecutive_empty_checks = 0;
20
               const MAX_CONSECUTIVE_EMPTY_CHECKS: usize = 40000;
21
22
23
               while consumed_count < my_target {</pre>
24
                   match q.bench_pop(num_producers + consumer_id) {
                       Ok(_item) => {
25
```

```
consumed_count += 1;
27
                             consecutive_empty_checks = 0;
28
                        Err(_) => {
29
                            if
30
      → done_sync.producers_done.load(Ordering::Acquire)
31
                                 == num_producers as u32
32
33
                                 consecutive_empty_checks += 1;
34
                                 if consecutive_empty_checks >
35
       → MAX_CONSECUTIVE_EMPTY_CHECKS {
                                     break; // Queue likely empty
36
37
                             }
38
39
                             // Backoff strategy
41
                             for _ in 0..100 {
42
                                 std::hint::spin_loop();
43
44
45
                    }
               }
46
47
               done_sync
48
49
                    .total_consumed
                    .fetch_add(consumed_count, Ordering::AcqRel);
50
51
               done_sync.consumers_done.fetch_add(1, Ordering::AcqRel);
52
53
               unsafe { libc::_exit(0) };
54
55
           Ok(ForkResult::Parent { child }) => {
               consumer_pids.push(child);
56
57
           Err(e) => panic!("Fork_failed_for_consumer:_{{}}", e),
58
59
       }
```

Lines 12 to 18 calculate each consumer's share of items, distributing any remainder among the first consumers. The main consumption loop in lines 23 to 46 implements a termination strategy where lines 25 to 27 reset the empty check counter on successful pop while lines 30 to 38 check if all producers have finished and implement a termination condition. Lines 48 to 51 atomically update the total consumed count for later verification. Line 53 uses <code>\_exit</code> to avoid cleanup that might interfere with shared memory.

#### 7.1.7. Validation

After all producer and consumer processes complete, the benchmark validates that no items were lost or double read during the concurrent operations. This validation is important for

ensuring the correctness of each queue implementation under IPC scenarios, as shown in listing 7.8.

Listing 7.8: Post-benchmark validation of results

```
1 // Wait for all processes to complete
2 for pid in producer_pids {
       waitpid(pid, None).expect("waitpid_for_producer_failed");
4 }
5
6 for pid in consumer_pids {
       waitpid(pid, None).expect("waitpid_for_consumer_failed");
8 }
10 let duration = start_time.elapsed();
11
12 // Validate that all items were consumed
13 let total_consumed = done_sync.total_consumed.load(Ordering::Acquire);
14
if total_consumed != total_items {
16
      eprintln!(
17
           "Warning_{\square}(MPMC):_{\square}Total_{\square}consumed_{\square}{}/{}_{\square}items._{\square}Q:_{\square}{},_{\square}Prods:_{\square}{},_{\square}
      → Cons: []",
18
           total_consumed,
19
           total_items,
           std::any::type_name::<Q>(),
20
21
          num_producers,
           num_consumers
22
23
      );
24 }
25
26 // Clean up shared memory regions
27 unsafe {
       if !q_shm_ptr.is_null() {
28
29
           unmap_shared(q_shm_ptr, q_shm_size);
30
31
       unmap_shared(startup_sync_shm_ptr, startup_sync_size);
       unmap_shared(done_sync_shm_ptr, done_sync_size);
32
33 }
34
35 duration
```

Lines 2 to 8 wait for all processes to complete before proceeding with validation. After that line 13 atomically reads the total number of items consumed across all consumer processes. The validation check in lines 15 to 24 compares the consumed count against the expected total. If items are missing, line 17 prints a detailed warning that includes the actual versus expected counts in line 18, the queue type name in line 20, and the producer and consumer configuration in lines 21 and 22. This warning helps identify queue implementations that may lose items under high contention or have synchronization issues and to verify that the queue operates correctly under concurrent access, if the warning does not appear.

# 7.1.8. Benchmark Configuration

The benchmarks use Criterion's configuration options to ensure reliable measurements, as shown in listing 7.9.

Listing 7.9: Criterion benchmark configuration

```
1 fn custom_criterion() -> Criterion {
    Criterion::default()
3
        .warm_up_time(Duration::from_secs(1))
4
          .measurement_time(Duration::from_secs(4200))
          .sample_size(500)
5
6 }
8 criterion_group! {
     name = benches;
     config = custom_criterion();
     targets =
         bench_wcq_queue,
13
         bench_turn_queue,
14
         bench_kogan_petrank_queue,
15
         bench_yang_crummey
16 }
17
18 criterion_main! (benches);
```

Line 3 sets a 1-second warm-up period to stabilize system state. Line 4 configures 4200 seconds of measurement time per benchmark. Line 5 sets 500 samples, as each sample involves creating multiple processes and produce and consume a set number of items. Lines 8 to 16 define the benchmark group with all queue implementations to test.

The same benchmark structure is applied to all benchmarks with appropriate modifications to the number of producers and consumers. This consistent approach ensures fair comparison across all implementations while accurately measuring their performance characteristics under IPC scenarios.

## 7.2. Benchmark Results

# 8. Conclusion and Future Work

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# **List of Acronyms**

**IPC** Inter-Process Communication

HRTS Hard Real-Time System

**SRTS** Soft Real-Time System

RTOS Real-Time Operating System

RTS Real-Time System

**CAS** Compare and Swap

**DWCAS** Double-With Compare and Swap

**DCAS** Double Compare and Swap

FIFO First In First Out

LIFO Last In First Out

MPMC Multi Producer Multi Consumer

MPSC Multi Producer Single Consumer

**SPMC** Single Producer Multi Consumer

**SPSC** Single Producer Single Consumer

FAA Fetch and Add

FAS Fetch and Store

LL/SC Load-Linked and Store-Conditional

LL Load-Linked

sc Store-Conditional

**VL** Validate-Link

FFQ FastForward Queue

IFFQ Improved FastForward Queue

**BIFFQ** Batched Improved FastForward Queue

uSPSC Unbounded Single Producer Single Consumer

dSPSC Dyncamic Single Producer Single Consumer

mSPSC MultiPush Single Producer Single Consumer

**BLQ** Batched Lamport Queue

# List of Acronyms

LLQ Lazy Lamport Queue

**BLQ** Batched Lamport Queue

wCQ Wait-Free Circular Queue

YMC Yang Mellor-Crummey

sCQ Scalable Circular Queue

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