Smooth and Nonsmooth Markowitz Portfolio Optimization

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I. Introduction

What is the aim of this work?
What are the main results?
This is a concise introduction to your work. See Section 3 for details.

II. Data

How did you handle the raw data?
How did you estimate μ and Σ?
A positive semi-definite covariance matrix would greatly improve the model. Why? Is it PSD? If not, can you make it naturally?

III. Smooth Model

A. Model

B. Projected Gradient Descent

Description of the methods
What do you need for each of them?
Compare the theory with some first numerical results.
What can be improved compared to the theory? Why? Is it normal?
For example:

Input: step size $\alpha > 0$
Output: approximate solution x_N

    for $k = 0, 1, ..., N - 1$ **do**
      compute a gradient g_k
      $x_{k+1} = x_k - \alpha g_k$
end for

Algorithm 1. Gradient Descent

I need a gradient and a step size for Algorithm 1 to work, so the gradient is ... and a classical choice of step size is ..., so I need to compute ....

C. Projected Gradient Descent with Momentum

What is the momentum doing?

D. Projected Randomized Coordinate Descent

Is it smart to make deterministic choices for the coordinates? Is the answer the same in theory and in practice? Discuss it.

IV. Non-smooth Model

A. Model

Key differences with the smooth case. What fundamental changes are you expecting? Do you verify them?

B. Projected Subgradient Method

C. Proximal Gradient Descent

Did you think of other methods? Why could they help solve the problem? What structure of the problem made you think of this method?

V. Numerical results

What comparisons could you make between the different methods? Is it always a fair choice?
Can some methods be greatly improved compared to the theory?
Are some of them disappointing? Do you have an explanation?
In general, does a model (smooth or non-smooth) bring better solutions? What do you mean by better? Are the methods faster? Do the solutions have a particular structure? Is it normal?

VI. Conclusion

Summary.

References