

# NASIONALE SENIOR SERTIFIKAAT-EKSAMEN NOVEMBER 2019

# TEGNIESE WISKUNDE: VRAESTEL I NASIENRIGLYNE

Tyd: 3 uur 150 punte

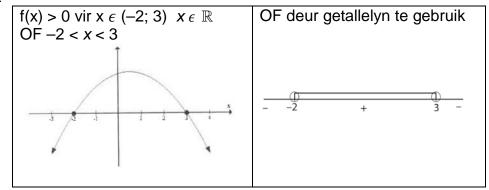
Hierdie nasienriglyne is opgestel vir gebruik deur eksaminators en hulpeksaminators van wie verwag word om almal 'n standaardiseringsvergadering by te woon om te verseker dat die riglyne konsekwent vertolk en toegepas word by die nasien van kandidate se skrifte.

Die IEB sal geen bespreking of korrespondensie oor enige nasienriglyne voer nie. Ons erken dat daar verskillende standpunte oor sommige aangeleenthede van beklemtoning of detail in die riglyne kan wees. Ons erken ook dat daar sonder die voordeel van die bywoning van 'n standaardiseringsvergadering verskillende vertolkings van die toepassing van die nasienriglyne kan wees.

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1.1 1.1.1 
$$6 - x^2 + x = 0$$
  
 $x^2 - x - 6 = 0$   
 $(x - 3)(x + 2) = 0$   
 $x = 3 \text{ of } x = -2$ 

1.1.2



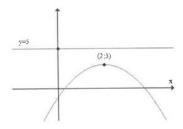
1.3 1.3.1 
$$-(x-2)^2 + 3 = 5$$
  
 $-x^2 + 4x - 4 - 2 = 0$   
 $x^2 - 4x + 6 = 0$   

$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(6)}}{2(1)}$$

$$x = \frac{4 \pm \sqrt{-8}}{2} = \frac{4 \pm 2\sqrt{-2}}{2}$$

$$x = 2 \pm \sqrt{-2} \quad \text{OF} \quad x = 2 \pm \sqrt{2}i$$

1.3.2 
$$-x^2 + 4x - 1 = 5 + k$$
 OF  
 $0 = x^2 - 4x + 6 + k$   
 $\Delta = (-4)^2 - 4(1)(6 + k)$   
 $= 16 - 24 - 4k$   
 $= -4k - 8$   
Dus 2 reële, verskillende wortels  $-4k - 8 > 0$   
 $-4k > 8$   
 $k < -2$ 



Deur inspeksie van grafiek g(x) + k ontmoet f twee keer indien 5 + k < 3 k < -2

1.4 
$$\frac{1 \times 2^{4} + 1 \times 2^{3} + 0 \times 2^{2} + 1 \times 2^{1} + 1 \times 2^{0}}{1 \times 2^{5} + 1 \times 2^{4} + 0 \times 2^{3} + 0 \times 2^{2} + 1 \times 2^{1} + 1 \times 2^{0}}$$

$$= \frac{16 + 8 + 2 + 1}{32 + 16 + 2 + 1}$$

$$= \frac{27}{51}$$

$$= \frac{9}{17}$$

1.5 
$$\varepsilon = \frac{\Delta L}{L}$$

$$0,77 = \frac{182 - L}{L}$$

$$0,77L + L = 182$$

$$L = \frac{182}{1,77}$$

$$= 102,824858 \dots$$

$$\approx 1,02825 \times 10^{2}$$

2.1 
$$\left( (x+2)^{\frac{3}{4}} \right)^{\frac{4}{3}} = (27)^{\frac{4}{3}} \qquad \begin{array}{c} x+2>0 \\ x>-2 \end{array}$$
 OF 
$$\left( (x+2)^{\frac{3}{4}} = 3 \right)$$
 
$$(x+2)^{\frac{1}{4}} = 3$$
 
$$(x+2)^{\frac{3}{4}} = (27)^{\frac{4}{3}}$$
 
$$(x+2)^{\frac{4}{3}} = (27)^{\frac{4}{3}} = (27)^{\frac{4}{3}}$$
 
$$(x+2)^{\frac{4}{3}} = (27)^{\frac{4}{3}} = (27)^$$

2.2 2.2.1 
$$(2\sqrt{3} - \sqrt{3} - 2\sqrt{2})(2\sqrt{3} - \sqrt{3} + 2\sqrt{2})$$
  
=  $(\sqrt{3} - 2\sqrt{2})(\sqrt{3} + 2\sqrt{2})$   
=  $3 - 8$   
=  $-5$ 

$$2.2.2 \quad \frac{3 \cdot 2^{2x+1} - 2^{2x-2} + 4^{x}}{4 \cdot 2^{2x-3}}$$

$$= \frac{3 \cdot 2^{2x} \cdot 2^{1} - 2^{2x} \cdot 2^{-2} + 2^{2x}}{4 \cdot 2^{2x} \cdot 2^{-3}}$$

$$= \frac{2^{2x} \left(3 \cdot 2^{1} - 2^{-2} + 1\right)}{4 \cdot 2^{2x} \cdot 2^{-3}}$$

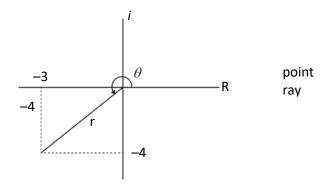
$$= \frac{6 - \frac{1}{4} + 1}{4 \cdot \frac{1}{8}}$$

$$= \frac{27}{4} \times \frac{2}{1}$$

$$= \frac{27}{2}$$

2.3 
$$2(5-2i)-i(6i-1)$$
  
=  $10-4i-6i^2+i$   
=  $10-4i+6+i$   
=  $16-3i$ 

# 2.4 2.4.1



2.4.2 
$$r = |p|$$
  

$$r^{2} = (-3)^{2} + (-4)^{2}$$

$$= 9 + 16 = 25$$

$$r = 5$$

$$\tan \theta = \frac{-4}{-3} = \frac{4}{3}$$

$$\theta = 180^{\circ} + 53,13^{\circ}$$

$$= 233,13^{\circ}$$

$$P = (5; 233,13^{\circ}) \text{ OF } (5 \cos 233,13^{\circ}; 5 \sin 233,13^{\circ})$$

$$OF p = +5 \cos 233,13^{\circ} + 5 \sin 233,13^{\circ}$$

$$OF p = 5 \cos 233,13^{\circ}$$

$$OF p = 5 |233,13^{\circ}$$

3.1 3.1.1 By B: 
$$x + 2 = 0$$
  
 $x = -2$   
B is  $(-2; 0)$ 

3.1.2 Wortels is 
$$-12$$
 en  $-2$   
Vergelyking is  $y = a(x+12)(x+2)$   
Vervang  $(-13; -11)$ :  $-11 = a(-1)(-11)$   
 $-11 = 11a$   
 $-1 = a$   
 $y = -1(x+12)(x+2)$   
 $y = -x^2 - 14x - 24$ 

3.1.3 
$$x_E = -7$$
 (deur simmetrie) OF  $f'(x) = 0$   
 $-2x + 14 = 0$   
 $y_E = -(-7)^2 - 14(-7) - 24$   $x = 7$   
 $= -49 + 98 - 24$   
 $= 25$   
 $x_F = x_E = -7$ : Vervang in  $g$ :  $y_F = -7 + 2 = -5$   
EF =  $y_E - y_F$   
 $= 25 - (-5) = 30$ 

3.1.4 
$$x_E = x_G = -7$$
  
G is (-7; 3)  
By K,  $y = 3$ :  $3 = x + 2$   
 $1 = x$   
K is (1; 3)  
GF =  $3 - (-5) = 8$  GK =  $1 - (-7) = 8$   
Oppervlakte  $\triangle GFK = \frac{1}{2}GF.GK$   
 $= \frac{1}{2} \times 8 \times 8$   
 $= 32$ 

3.2 3.2.1 Laat y = 0

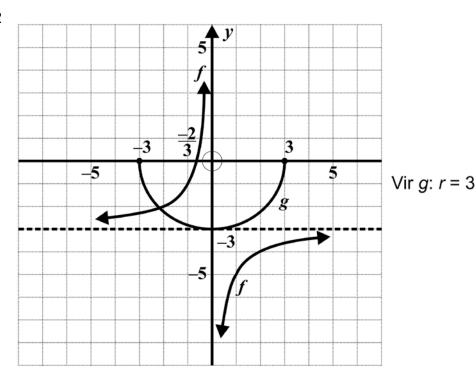
$$0 = \frac{-2}{x} - 3$$

$$3 = \frac{-2}{x}$$

$$3x = -2$$

$$x = -\frac{2}{3} OR \left( -\frac{2}{3}; 0 \right)$$

3.2.2



3.2.3 
$$x \in \left[ -\frac{2}{3}; 0 \right] \text{ OF } -\frac{2}{3} \le x < 0$$

3.3 Asimptoot y = -3

d.w.s. 
$$q = -3$$

$$y=a.b^x-3$$

Vervang 
$$(0; -2)$$
:  $-2 = a.b^0 - 3$ 

$$1 = a$$

Vervang 
$$(1; -1)$$
:  $-1 = b^1 - 3$ 

$$2 = b$$

d.w.s. 
$$y = 2^x - 3$$

4.1 4.1.1 
$$1+i \text{ eff} = \left(1+\frac{0.072}{12}\right)^{12}$$

 $i \text{ eff} = 0.074424 \dots$ 

d.w.s. effektiewe koers ≈7,44%

4.1.2 150 000 = 120 000 
$$\left(1 + \frac{0,072}{12}\right)^n$$

$$\frac{15}{12} = \left(1 + \frac{0,072}{12}\right)^n$$

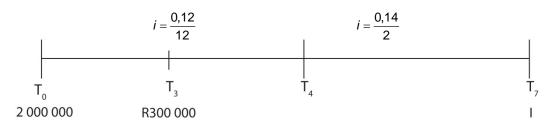
$$\log_{\left(1+\frac{0,072}{12}\right)}\left(\frac{5}{4}\right) = n$$

n ≈ 37,3... maande d.w.s. 38 maande

4.2 
$$I = 2 \times 10^{6} \left( 1 + \frac{0.12}{12} \right)^{48} \left( 1 + \frac{0.14}{2} \right)^{6} - 300\ 000 \left( 1 + \frac{0.12}{12} \right)^{12} \left( 1 + \frac{0.14}{2} \right)^{6}$$
  
 $\approx R4\ 331\ 715.06$ 

OF 
$$\left[ 2 \times 10^{6} \left( 1 + \frac{0,12}{12} \right)^{36} - 300\ 000 \right] \left( 1 + \frac{0,12}{12} \right)^{12} \left( 1 + \frac{0,14}{2} \right)^{6}$$

$$\approx R4\ 331\ 715,06$$



4.3 4.3.1 Verminderende saldo

4.3.2 110 940 = 150 000 
$$(1 - i)^2$$

$$\sqrt{\frac{110\ 940}{150\ 000}} = 1 - i$$

 $i \approx 0.14$ 

Koers is 14%

4.3.3 A = 
$$150\ 000\ (1-0.14)^7$$
  
  $\approx R52\ 189.17$ 

Die boekwaarde van motor na 7 jaar.

5.1 
$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \to 0} \frac{-3(x+h) + 1 - (-3x+1)}{h}$$

$$= \lim_{h \to 0} \frac{-3x - 3h + 1 + 3x - 1}{h}$$

$$= \lim_{h \to 0} \frac{3h}{h}$$

$$= 3$$

5.2 5.2.1 
$$f(x) = \frac{2\sqrt{x}}{\sqrt{x}} - \frac{5}{\sqrt{x}}$$
  
=  $2 - 5x^{-\frac{1}{2}}$   
 $f'(x) = \frac{5}{2}x^{-\frac{3}{2}}$ 

5.2.2 
$$y = 2x(1-x)^2$$
  
=  $2x-4x^2+2x^3$   
 $\therefore \frac{dy}{dx} = 2-8x+6x^2$ 

5.3 
$$f(x) = 3x^2 + 13x$$
  
 $f'(x) = 6x + 13$   
 $m_{tan} = tan 45^\circ = 1$   
d.w.s.  $f'(x) = 1$   
 $6x + 13 = 1$   
 $6x = -12$   
 $x = -2$ 

5.4 5.4.1 Vergelyking is 
$$y = (x+2)(x-1)(x-6)$$
  

$$= (x+2)(x^2-7x+6)$$

$$= x^3-7x^2+6x+2x^2-14x+12$$

$$= x^3-5x^2-8x+12$$

$$b = -5; c = -8; d = 12$$

5.4.2 
$$f'(x) = 3x^{2} - 10x - 8$$
By D en E,  $3x^{2} - 10x - 8 = 0$ 

$$(3x + 2)(x - 4) = 0$$

$$x_{D} = -\frac{2}{3} \qquad x_{E} = 4$$

$$y_{D} = \frac{400}{27} \qquad y_{E} = -36$$
(Gebruik sakrekenaar)
$$D \text{ is } \left(-\frac{2}{3}; \frac{400}{27}\right) \text{ E is } (4; -36)$$

6.1 Teken 
$$A = 1$$

Tyd is tussen t<sub>B</sub> en t<sub>C</sub>

By *B* en *C*, 
$$1 = -t^3 + 2t^2$$

$$t^3 - 2t^2 + 1 = 0$$

Laat 
$$f(t) = t^3 - 2t^2 + 1$$

$$f(1) = 1 - 2 + 1 = 0$$

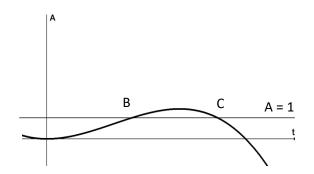
$$\therefore t-1$$
 is 'n faktor

$$(t-1)(t^2-t-1)=0$$

$$t = 1 \text{ of } t = \frac{1 \pm \sqrt{1+4}}{2}$$

$$t = \frac{1 + \sqrt{5}}{2} \approx 1.6 (t > 0)$$

 $\therefore$  tyd is 1,6 – 1 = 0,6 uur = 36 minute



6.2 Omtrek = 
$$2\pi r + 2L$$

$$400 = 2\pi r + 2L$$

$$200 = \pi r + L$$

$$200 - \pi r = L$$

$$S = \pi r^2 + 2r \cdot L$$

$$= \pi r^2 + 2r (200 - \pi r)$$

$$S = 400r - \pi r^2$$

$$\frac{ds}{dr} = 400 - 2\pi r$$

By maksimum,  $400 - 2\pi r = 0$ 

$$r = \frac{200}{\pi}$$
 m

6.3 
$$\int (2x^{-1} + 3x^2 - 1) dx$$
$$= 2 \cdot \ln x + \frac{3x^{2+1}}{2+1} - x + c$$

$$= 2 \ln x + x^3 - x + c$$

6.4 By A en B, 
$$2x^2 - 8x + 6 = 0$$
  
 $x^2 - 4x + 3 = 0$   
 $(x-3)(x-1) = 0$   
 $x = 3$  of  $x = 1$ 

∴ Oppervlakte = 
$$\int_{A}^{B} f(x) dx$$
  
=  $\int_{1}^{3} (2x^{2} - 8x + 6) dx$   
=  $\left[ \frac{2x^{3}}{3} - \frac{8x^{2}}{2} + 6x \right]_{1}^{3}$   
=  $\left[ \frac{2(27)}{3} - 4(9) + 6(3) \right] - \left[ \frac{2}{3} - 4 + 6 \right]$   
=  $\left| -2\frac{2}{3} \right|$ 

Oppervlakte =  $2\frac{2}{3}$ 

Totaal: 150 punte