

Given functions:

n , \sqrt{n} , $n^{1.5}$, n^2 , $n \log n$, $n \log \log n$, $n \log^2 n$, $\frac{2}{n}$, $2n$, $\frac{2^n}{2}$, 37 , $n^2 \log n$, n^3

To sort the given functions according to their growth rate from **slowest** to **fastest**, we analyze their asymptotic behavior using **Big-O notation**.

Step 1: Identify Growth Rates

1. Constant Function (slowest growth):

- $37 = O(1)$

2. Inverse Growth (decreasing function):

- $\frac{2}{n} = O(1/n)$ (shrinks as n increases)

3. Logarithmic and Sublinear Growth:

- $\sqrt{n} = O(n^{0.5})$
- $n \log \log n$ (grows slightly faster than n)
- $n \log n$ (grows faster than $n \log \log n$)

4. Polynomial Growth:

- $n = O(n)$
- $2n = O(n)$ (same growth as n , just a constant multiplier)
- $n^{1.5} = O(n^{1.5})$
- $n^2 = O(n^2)$
- $n^2 \log n$ (slightly faster than n^2)
- $n^3 = O(n^3)$

5. Exponential Growth (fastest growth):

- $\frac{2^n}{2} = O(2^n)$ (dominates all polynomial functions)

Step 2: Sorting by Growth Order

From slowest to fastest: $\frac{2}{n}$, 37 , \sqrt{n} , n , $2n$, $n \log \log n$, $n \log n$, $n^{1.5}$, $n \log^2 n$, n^2 , $n^2 \log n$, n^3 , $\frac{2^n}{2}$

This order reflects increasing growth rates based on asymptotic analysis.