

## Given functions:

$n$ ,  $\sqrt{n}$ ,  $n^{1.5}$ ,  $n^2$ ,  $n \log n$ ,  $n \log \log n$ ,  $n \log^2 n$ ,  $\frac{2}{n}$ ,  $2n$ ,  $\frac{2^n}{2}$ ,  $37$ ,  $n^2 \log n$ ,  $n^3$

To sort the given functions according to their growth rate from **slowest** to **fastest**, we analyze their asymptotic behavior using **Big-O notation**.

### Step 1: Identify Growth Rates

#### 1. Constant Function (slowest growth):

- $37 = O(1)$

#### 2. Inverse Growth (decreasing function):

- $\frac{2}{n} = O(1/n)$  (shrinks as  $n$  increases)

#### 3. Logarithmic and Sublinear Growth:

- $\sqrt{n} = O(n^{0.5})$
- $n \log \log n$  (grows slightly faster than  $n$ )
- $n \log n$  (grows faster than  $n \log \log n$ )

#### 4. Polynomial Growth:

- $n = O(n)$
- $2n = O(n)$  (same growth as  $n$ , just a constant multiplier)
- $n^{1.5} = O(n^{1.5})$
- $n^2 = O(n^2)$
- $n^2 \log n$  (slightly faster than  $n^2$ )
- $n^3 = O(n^3)$

#### 5. Exponential Growth (fastest growth):

- $\frac{2^n}{2} = O(2^n)$  (dominates all polynomial functions)

### Step 2: Sorting by Growth Order

From slowest to fastest:  $\frac{2}{n}$ ,  $37$ ,  $\sqrt{n}$ ,  $n$ ,  $2n$ ,  $n \log \log n$ ,  $n \log n$ ,  $n^{1.5}$ ,  $n \log^2 n$ ,  $n^2$ ,  $n^2 \log n$ ,  $n^3$ ,  $\frac{2^n}{2}$

This order reflects increasing growth rates based on asymptotic analysis.