

# Assignment 08 | Advance Algorithms

## CE-092

Assignment submission for Advance Algorithms subject week 8.

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### Task 1:

FordFulkerson algorithm to find the max flow in the given graph.

#### Code:

I have implemented this algorithm using bfs and dfs both.

**fordFulkerson** : Using DFS

**fordFulkerson2** : Using BFS

```
/*
 * @Author: nevil
 * @Date: 2020-09-23 18:46:30
 * @Last Modified by: nevil
 * @Last Modified time: 2020-09-23 18:57:36
 */

#include <bits/stdc++.h>
using namespace std;

#define V 6

bool bfs(int rGraph[V][V], int s, int t, int parent[])
{
    bool visited[V];
```

```

memset(visited, 0, sizeof(visited));

queue <int> q;
q.push(s);
visited[s] = true;
parent[s] = -1;

while (!q.empty())
{
    int u = q.front();
    q.pop();

    for (int v = 0; v < V; v++)
    {
        if (visited[v] == false && rGraph[u][v] >
0)
        {
            q.push(v);
            parent[v] = u;
            visited[v] = true;
        }
    }
}

return (visited[t] == true);
}

bool dfsutil(int rGraph[V][V], int s, int t, int
parent[], bool visited[]) {
    visited[s] = true;
    for (int i = 0; i < V; i++) {
        if (visited[i] == false && rGraph[s][i] > 0 ) {
            parent[i] = s;
            dfsutil(rGraph, i, t, parent, visited);

```

```

    }
}
return (visited[t] == true);
}

void fordFulkerson(int graph[V][V], int s, int t)
{
    int u, v;

    int rGraph[V][V];

    for (u = 0; u < V; u++)
        for (v = 0; v < V; v++)
            rGraph[u][v] = graph[u][v];

    int parent[V];

    int max_flow = 0;

    bool visited[V];
    memset(visited, 0, sizeof(visited));
    parent[s] = -1;

    while (dfsutil(rGraph, s, t, parent, visited))
    {
        int path_flow = INT_MAX;
        cout << t << " ";
        for (v = t; v != s; v = parent[v])
        {
            u = parent[v];
            cout << u << " ";
            path_flow = min(path_flow, rGraph[u][v]);
        }
    }
}

```

```

    }
    cout << "=>" << path_flow << " ";
    cout << "\n ";

    for (v = t; v != s; v = parent[v])
    {
        u = parent[v];
        rGraph[u][v] -= path_flow;
        rGraph[v][u] += path_flow;
    }

    max_flow += path_flow;

    memset(visited, 0, sizeof(visited));
    parent[s] = -1;

}

cout << "\nmax flow : " << max_flow << "\n";
}

int fordFulkerson2(int graph[V][V], int s, int t)
{
    int u, v;

    int rGraph[V][V];

    for (u = 0; u < V; u++)
        for (v = 0; v < V; v++)
            rGraph[u][v] = graph[u][v];

    int parent[V];

```

```

int max_flow = 0;

bool visited[V];
memset(visited, 0, sizeof(visited));
parent[s] = -1;

while (bfs(rGraph, s, t, parent))
{
    int path_flow = INT_MAX;
    cout << t << " ";
    for (v = t; v != s; v = parent[v])
    {
        u = parent[v];
        cout << u << " ";
        path_flow = min(path_flow, rGraph[u][v]);
    }
    cout << "=>" << path_flow << " ";
    cout << "\n ";

    for (v = t; v != s; v = parent[v])
    {
        u = parent[v];
        rGraph[u][v] -= path_flow;
        rGraph[v][u] += path_flow;
    }

    max_flow += path_flow;

    memset(visited, 0, sizeof(visited));
    parent[s] = -1;
}

```

```

    }

    cout << "\nmax flow : ";
    return max_flow;
}

int main()
{
    int graph[V][V] = { {0, 16, 13, 0, 0, 0},
                        {0, 0, 10, 12, 0, 0},
                        {0, 4, 0, 0, 14, 0},
                        {0, 0, 9, 0, 0, 20},
                        {0, 0, 0, 7, 0, 4},
                        {0, 0, 0, 0, 0, 0}
    };

    cout << "possible path and max flow using dfs \n"
    << "\n" ;
    fordFulkerson(graph, 0, 5);

    cout << endl << endl;
    cout << "possible path and max flow using bfs \n" ;
    cout << fordFulkerson2(graph, 0, 5) << endl;
    return 0;
}

```

Output:

The screenshot shows an IDE with two panels. The left panel displays the source code for `FordFulkerson.cpp`, which includes a BFS function and a main function. The right panel shows the test output for the program.

```
1  /*
2  * @Author: nevil
3  * @Date: 2020-09-23 18:46:30
4  * @Last Modified by: nevil
5  * @Last Modified time: 2020-09-23 18:57:36
6  */
7
8  #include <bits/stdc++.h>
9  using namespace std;
10
11  #define V 6
12
13  bool bfs(int rGraph[V][V], int s, int t, int parent[])
14  {
15
16      bool visited[V];
17      memset(visited, 0, sizeof(visited));
18
19      queue <int> q;
20      q.push(s);
21      visited[s] = true;
22      parent[s] = -1;
23
24      while (!q.empty())
25      {
26          int u = q.front();
27          q.pop();
28
29          for (int v = 0; v < V; v++)
30          {
31              if (visited[v] == false && rGraph[u][v] > 0)
32              {
33                  q.push(v);
34                  parent[v] = u;
35                  visited[v] = true;
36              }
37          }
38      }
39
40      return (visited[t] == true);
41  }
```

test 0 edit run time: 51ms

possible path and max flow using dfs

```
5 3 4 2 1 0 =>7
5 4 2 1 0 =>3
5 4 2 3 1 0 =>1
5 3 1 0 =>5
5 3 1 2 0 =>6
5 3 2 0 =>1

max flow : 23

possible path and max flow using bfs
5 3 1 0 =>12
5 4 2 0 =>4
5 3 4 2 0 =>7

max flow : 23
accept
next test
```

This screenshot shows the test output from the Ford-Fulkerson algorithm, including the possible paths and the maximum flow.

```
test 0 edit run time: 51ms

possible path and max flow using dfs

5 3 4 2 1 0 =>7
5 4 2 1 0 =>3
5 4 2 3 1 0 =>1
5 3 1 0 =>5
5 3 1 2 0 =>6
5 3 2 0 =>1

max flow : 23

possible path and max flow using bfs
5 3 1 0 =>12
5 4 2 0 =>4
5 3 4 2 0 =>7

max flow : 23
accept
```

## Complexity :

The analysis of Ford-Fulkerson depends heavily on how the augmenting paths are found. The typical method is to use breadth-first search to find the path. If this method is used, Ford-Fulkerson runs in polynomial time.

If all flows are integers, then the while loop of Ford-Fulkerson is run at most  $|F^*|$ . Where  $F^*$  is the maximum flow. This is because the flow is increased, at worst, by 1 in each iteration.

Finding the augmenting path inside the while loop takes  $O(V + E)$ , where  $E$  is the set of edges in the residual graph. This can be simplified to  $O(E)$ . So, the runtime of Ford-Fulkerson is  $O(V + E)$ .

However since we are using an adjacency matrix in the above approach where bfs takes  $O(V^2)$  time, the overall time complexity of the above algorithm slightly differs from the adjacency list representation .

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