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## Phase diagrams and thermochemical modeling of salt lake brine systems. I. LiCl+H<sub>2</sub>O system



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### ABSTRACT

Salt lake brine chemical engineering involves the study of the solid–liquid equilibria of more than one hundred water–salt systems and approximately 70 solid salts over a wide temperature range. Prediction of the crystallization behavior of these complex systems as a function of temperature can only be achieved using a thermodynamic model. However, no systematic simulation studies have been reported for the complex salt lake brine systems, especially those systems containing the highly soluble salt LiCl. To complete this task, we plan to carry out a series of work. As the first part of the series of work, the Pitzer–Simonson–Clegg (PSC) model is selected to represent the thermodynamic properties of the LiCl+H<sub>2</sub>O system in the temperature range of 190 K to nearly 400 K. In this model's framework, the temperature dependence of the thermodynamic functions (entropy, enthalpy and Gibbs energy) of the aqueous species and solid phases are determined using their heat capacities, which serves to keep their inner thermodynamics consistent and confers a strong extrapolation ability. The comprehensive thermodynamic properties, i.e., water activity, mean ionic activity coefficient, enthalpy of dilution and solution, heat capacity and solubility, are used to evaluate the model parameters. The proposed parameter regression strategy has proven successful for the LiCl+H<sub>2</sub>O system. The present work forms a solid foundation for the simulation of thermochemical properties of other complicated salt lake brine systems.

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### 1. Introduction

Salt lake brine and coexisting salt deposits are important inorganic mineral resources, from which a huge amount of valuable salts, i.e., potash fertilizer and lithium compounds, can be produced. Many salt lakes exist on Earth, and over thousands of them are located in China. Salt lake brines are complex multi-component electrolyte aqueous systems, which consist of many inorganic ions, e.g., Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup>, Rb<sup>+</sup>, Mg<sup>2+</sup>, Ca<sup>2+</sup>, Cl<sup>−</sup>, SO<sub>4</sub><sup>2−</sup>, CO<sub>3</sub><sup>2−</sup>, HCO<sub>3</sub><sup>−</sup>, NO<sub>3</sub><sup>−</sup>, and borate. From these brines, dozens of solid salts can be crystallized under certain natural or artificial conditions. Depending on the chemical components of the brine, the salt lakes can be classified into chloride, chloride–sulfate, carbonate, and nitrate types. Because the brine compositions vary with regional characteristics, seasons, and solar evaporation stages, brine crystallization behaviors are very complex and differ from each other.

Usually, the humidity is very low in the regions where a salt lake is located. Salt evaporation pond process is one of the most economical tools to separate the salts from the brine. By adjusting the brine compositions in fractional crystallization processes, effective separation can be achieved. To obtain the desired salts, it is essential to know when and under what conditions (compositions and temperature) a specific type of salt will crystallize. Phase diagrams of the water–salt systems, if we have, can answer these questions. For decades, many authors have studied solid–liquid equilibria of simple binary, ternary and quaternary systems of salt lake brines at a scattered variety of temperatures. However, the exact crystallization sequence of salts and the appearance nodes of the salts cannot be determined from these scattered and limited experimental data alone. For a multi-component brine system, experimental determination of the phase diagram at a certain temperature is strenuous and time consuming work. Therefore, only the phase boundary, rather than a full characterization of the solid–liquid equilibria, is known for a given brine composition. Fortunately, phase diagram calculation approaches make it possible to reveal the phase equilibria behavior of a complex multi-

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component system over the entire composition field using computer assisted simulation. Song and Yao [1] have extended the Pitzer's ion interaction model [2] to describe the excess thermodynamic properties of the simplified salt lake brine system of  $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{Cl}^-$ ,  $\text{SO}_4^{2-}$ – $\text{H}_2\text{O}$  at 25 °C. Applying the model with new model parameters, they have not only simulated the phase diagrams of this complicated system and its lower-order systems, but they have also predicted the salts crystallization sequence of any brine with a specific composition under isothermal evaporation conditions at 25 °C [3–5]. Kwok et al. [6] have also described the thermodynamic and phase equilibrium properties of the simplified salt lake brine system of  $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{Cl}^-$ ,  $\text{SO}_4^{2-}$ – $\text{H}_2\text{O}$  at 25 °C with an extended UNIQUAC equations [7]. Unfortunately, the validity of these models are limited to 25 °C, and cannot be used to predict the phase equilibria of this brine system at temperatures far away from 25 °C.

Most salt evaporation ponds are constructed near salt lakes, and the pond temperatures change with the local environment and seasons. The crystallization route of any brine with a specific composition can change with temperature. For example, halite usually precipitates from a chloride–sulfate type brine during evaporation processes in the summer, while mirabilite precipitates in the winter. Based on the fact that  $\text{Li}_2\text{CO}_3$  solubility decreases with increasing temperature, a novel Li-extraction approach has been proposed to precipitate  $\text{Li}_2\text{CO}_3$  from a carbonate-type brine at high temperatures [8]. In these cases, the influence of temperature on the crystallization route of brine can be significant. To understand the crystallization route of a brine at various temperatures, its solid–liquid phase diagram at various temperatures must be known. However, known thermodynamic models cannot represent the phase equilibria behavior of brine at various temperatures, especially for systems containing Li-salts. Some research groups [9–14] have extended the primitive Pitzer model to represent the solid–liquid phase diagram of oceanic salt systems, where Li-salts are absent, at multiple temperatures. For salt lake brine systems where Li-salts are present, the phase diagram simulation becomes challenging. Because Li-salts, such as LiCl, are very soluble, e.g., nearly 20 mol  $\text{kg}^{-1}$  at 25 °C and more than 30 mol  $\text{kg}^{-1}$  at 100 °C for LiCl, the primitive Pitzer model cannot successfully simulate the thermodynamic properties of the system [15]. A proper thermodynamic model should be chosen to simulate the salt lake brine containing Li-salts.

Based on the above considerations, we intend to develop a thermodynamically consistent model for the simulation of salt lake brine systems. This simulation will aid in the design of evaporation crystallization processes and optimization of salt lake brine. This series of work will begin with the simulation of simple binary and ternary systems at multiple temperatures, and it will gradually extend to more complex multi-component systems. In the first part of the series papers, the  $\text{LiCl}+\text{H}_2\text{O}$  system will be simulated, and the model selection and parameter determination methodology will be established.

## 2. Modeling methodology

### 2.1. Model selection

Pitzer's equations for most pure electrolytes are valid to a maximum of 6 mol  $\text{kg}^{-1}$  at 298.15 K with the parameters reported by Pitzer and co-workers [2]. Many publications [9–14] have shown that the Pitzer's model can be valid up to the solubility limits of most salts when proper parameters are introduced. Kim and Frederick [16] reported Pitzer ion interaction parameters for 304 single salts in aqueous solution valid up to nearly saturation at

298.15 K. Holmes and co-workers [17–19] have reported some temperature dependent Pitzer ion interaction parameters for pure salts determined from isopiestic results at elevated temperature. Many other temperature dependent ion interaction parameters have been summarized in a monograph by Pitzer [2]. Unfortunately, Pitzer's equations do not satisfactorily represent  $\text{LiCl}$  (aq) and  $\text{CaCl}_2$ (aq) systems at elevated temperature due to the very high concentrations of the solutions [15].

The assumption of a continuous solvent that is made in the primitive Pitzer model seems to be unreasonable for very concentrated aqueous solutions where the ion–water interactions are significantly strong. To describe the thermodynamic properties of very concentrated aqueous solutions, Pitzer and Simonson [20,21] proposed a mole fraction based ion interaction model. In this model, solvents are seen as particles instead of as a continuous medium, and a general Margules equation instead of virial expansion was introduced to describe the short range interactions of the particles. Clegg and Pitzer [22] and Clegg et al. [23] extended the Pitzer–Simonson equations to an indefinite number of components, including ions of different charge types. Unlike the Pitzer–Simonson equations, the Clegg–Pitzer equations used an asymmetric reference state. The final version of the mole fraction-based model equations proposed by Clegg et al. [23] is usually used and is called the Pitzer–Simonson–Clegg (PSC) model. The validity of these equations to very concentrated aqueous solutions has been widely proven [24–26]. Therefore, the PSC activity coefficient model is used to describe the non-ideality of the aqueous phase in this work and the following works of this series.

### 2.2. PSC-model description

The molar excess Gibbs energy ( $g^{\text{ex}}$ ) equation and the derived equations for the activity coefficients ( $f_1$ ,  $f_M^*$  and  $f_X^*$ ), the apparent relative molal enthalpy ( $\phi L_m$ ), and the apparent molal heat capacity ( $\phi C_{p,m}$ ) of the PSC model for a pure electrolyte aqueous system  $\text{M}_{\text{vM}}\text{X}_{\text{vX}} + \text{H}_2\text{O}$  were derived by Clegg et al. [24] and are repeated here in Eqs. (1)–(7).

$$g^{\text{ex}}/RT = -(4A_x/\rho)I_x \ln(1 + \rho I_x) + x_M x_X B_{MX} g(\alpha I_x) + x_M x_X B_{MX}^1 g(\alpha I_x) + 1/2(x_M Z_M + x_X Z_X)x_i(Z_M + Z_X)/(Z_M Z_X)W_{1,MX} + x_i x_M x_X (Z_M + Z_X)^2/(Z_M Z_X)U_{1,MX} + 4x_i^2 x_M x_X V_{1,MX} \quad (1)$$

$$\ln f_1 = 2A_x I_x^{3/2}/(1 + \rho I_x^{1/2}) - x_M x_X B_{MX} \exp(-\alpha I_x^{1/2}) - x_M x_X B_{MX}^1 \exp(-\alpha I_x^{1/2}) + x_i^2 W_{1,MX} + x_i^2 (x_i - x_i)U_{1,MX} + 4x_i x_M x_X (2 - 3x_i)V_{1,MX} \quad (2)$$

$$\ln f_M^* = -Z_M^2 A_x [(2/\rho) \ln(1 + \rho I_x^{1/2}) + I_x^{1/2}(1 - 2I_x/Z_M^2)/(1 + \rho I_x^{1/2})] + x_X B_{MX} g(\alpha I_x^{1/2}) - x_M x_X B_{MX} [Z_M^2 g(\alpha I_x^{1/2})/(2I_x) + (1 - Z_M^2/(2I_x)) \exp(-\alpha I_x^{1/2})] + x_X B_{MX}^1 g(\alpha I_x^{1/2}) - x_M x_X B_{MX}^1 [Z_M^2 g(\alpha I_x^{1/2})/(2I_x) + (1 - Z_M^2/(2I_x)) \exp(-\alpha I_x^{1/2})] + x_i [(Z_M + Z_X)/(2Z_X) - x_i] W_{1,MX} + x_i x_i [(Z_M + Z_X)/Z_X - 2x_i] U_{1,MX} + 4x_i^2 x_X (1 - 3x_M) V_{1,MX} - (1/2)[(Z_M + Z_X)/Z_X] W_{1,MX} \quad (3)$$

$$\begin{aligned} \ln f_X^* = & -Z_X^2 A_X [(2/\rho) \ln(1 + \rho I_X^{1/2}) + I_X^{1/2} (1 - 2I_X/Z_X^2) / (1 + \rho I_X^{1/2})] \\ & + x_M B_{MX} g(\alpha I_X^{1/2}) - x_M x_X B_{MX} [Z_M^2 g(\alpha I_X^{1/2}) / (2I_X) \\ & + (1 - Z_X^2 / (2I_X)) \exp(-\alpha I_X^{1/2})] + x_M B_{MX}^1 g(\alpha I_X^{1/2}) \\ & - x_M x_X B_{MX}^1 [Z_M^2 g(\alpha I_X^{1/2}) / (2I_X) \\ & + (1 - Z_X^2 / (2I_X)) \exp(-\alpha I_X^{1/2})] + x_1 (Z_M + Z_X) / (2Z_M) - x_1 \\ & W_{1,MX} + x_1 x_1 (Z_M + Z_X) / Z_M - 2x_1 U_{1,MX} + 4x_1^2 x_X (1 - 3x_X) \\ & V_{1,MX} - (1/2) [(Z_M + Z_X) / Z_M] W_{1,MX} \end{aligned} \quad (4)$$

$$\begin{aligned} {}^p L_m = & \nu Z_M Z_X (A_{H,X} / 2\rho) \ln(1 + \rho I_X^{1/2}) \\ & - \nu x_1 R T^2 (Z_M Z_X / (Z_M + Z_X)^2) (B_{MX}^L g(\alpha I_X^{1/2}) + B_{MX}^{1,L} g(\alpha I_X^{1/2})) \\ & + \nu x_1 R T^2 (W_{1,MX}^L - x_1 U_{1,MX}^L - 4x_1^2 (Z_M Z_X / (Z_M + Z_X)^2) V_{1,MX}^L) \end{aligned} \quad (5)$$

$$\begin{aligned} {}^p C_{p,m} = & C_{p,m}^\ominus + \nu Z_M Z_X (A_{C,X} / 2\rho) \ln(1 + \rho I_X^{1/2}) \\ & - \nu x_1 R T^2 (Z_M Z_X / (Z_M + Z_X)^2) (B_{MX}^J g(\alpha I_X^{1/2}) + B_{MX}^{1,J} g(\alpha I_X^{1/2})) \\ & + \nu x_1 R T^2 (W_{1,MX}^J - x_1 U_{1,MX}^J - 4x_1^2 (Z_M Z_X / (Z_M + Z_X)^2) V_{1,MX}^J) \end{aligned} \quad (6)$$

where

$$g(x) = 2[1 - (1 + x) \exp(-x)] / x^2 \quad (7)$$

In the equations,  $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$  is the gas constant, and  $T$  is the absolute temperature in Kelvin.  $A_X$ ,  $A_{H,X}$  and  $A_{C,X}$  are the Debye–Hückel slopes for the mole fraction based ionic activity coefficient, enthalpy and heat capacity, respectively. The Bradley–Pitzer equation [27] for the dielectric constant and the Wagner–Pruss equation of state [28] for the density of pure liquid water are introduced to produce these Debye–Hückel slopes.  $\rho$  is a constant set to 13.0.  $I_X$  is the mole fraction based ionic strength ( $I_X = (1/2)(Z_M^2 x_M + Z_X^2 x_X)$ ). The charge magnitudes of the ions  $M$  and  $X$  are  $Z_M$  and  $Z_X$ , respectively. The mole fraction of water is  $x_1$ , and  $x_1$  is the total mole fraction of the ions ( $x_1 = x_M + x_X$ ).  $\nu$  ( $\nu = \nu_M + \nu_X$ ) in Eqs. (5) and (6) is the number of moles of ions produced by the complete dissociation of one mole of the salt  $M_{\nu_M} X_{\nu_X}$ .  $C_{p,m}^\ominus$  in Eq. (6) is the standard state heat capacity of the solute.

The temperature dependence of the PSC parameters ( $P = B_{MX}$ ,  $B_{MX}^1$ ,  $W_{1,MX}$ ,  $U_{1,MX}$  and  $V_{1,MX}$ ) in the activity coefficient equations is defined in this work as

$$P(T) = a_0 + a_1 T + a_2 T \ln(T) + a_3 T^2 + a_4 T^3 + a_5 / T \quad (8)$$

The temperature dependence of the parameters in Eqs. (5) and (6) for the respective enthalpy ( $P^L = B_{MX}^L$ ,  $B_{MX}^{1,L}$ ,  $W_{1,MX}^L$ ,  $U_{1,MX}^L$  and  $V_{1,MX}^L$ ) and heat capacity ( $P^J = B_{MX}^J$ ,  $B_{MX}^{1,J}$ ,  $W_{1,MX}^J$ ,  $U_{1,MX}^J$  and  $V_{1,MX}^J$ ) can be derived according to the definitions in Eqs. (9) and (10).

$$P^L(T) = \partial P(T) / \partial T \quad (9)$$

$$P^J(T) = \partial^2 P(T) / \partial T^2 + (2/T) \partial P(T) / \partial T \quad (10)$$

Generally, the experimental activity coefficient for the ions is a molality scale mean ionic activity coefficient ( $\gamma_{\pm}$ ), and its relationship with the mole fraction based activity coefficients ( $f_M^*$  and  $f_X^*$ ) is

$$\gamma_{\pm} = [(x_M f_M^*)^{\nu_M} (x_X f_X^*)^{\nu_X}]^{1/\nu} \quad (11)$$

Water activity ( $a_w$ ) and the osmotic coefficient ( $\phi$ ) can be calculated from Eqs. (12) and (13).

$$a_w = x_1 f_1 \quad (12)$$

$$\phi = -(n_1 / \nu n_2) \ln a_w \quad (13)$$

where,  $n_1$  is the mole number of water, and  $n_2$  is the mole number of the electrolyte.

### 2.3. Temperature dependence of the standard state thermodynamic properties

The standard Gibbs energy  $G_i^\ominus(T)$  of any species  $i$  at temperature  $T$  can be calculated by following relationships:

$$\begin{aligned} G_i^\ominus(T) &= H_i^\ominus(T) - S_i^\ominus(T) T \\ &= H_{i,298.15}^\ominus + \int_{298.15}^T C_{p,i}^\ominus(T) dT \\ &\quad - (S_{i,298.15}^\ominus + \int_{298.15}^T \frac{C_{p,i}^\ominus(T)}{T} dT) T \end{aligned} \quad (14)$$

So long the values of  $H_{i,298.15}^\ominus$ ,  $S_{i,298.15}^\ominus$  and  $C_{p,i}^\ominus(T)$  are known, the value of  $G_i^\ominus(T)$  can be calculated.

The temperature dependence of the standard isobaric heat capacity  $C_{p,i}^\ominus$  for a species  $i$  is represented with Eq. (15) as recommended by the NIST Webbook [29].

$$C_{p,i}^\ominus(t) = A + Bt + Ct^2 + Dt^3 + E/t^2 \quad (15)$$

where,  $t = (T/K)/1000$ , and  $T$  is the absolute temperature in Kelvin.  $A$ ,  $B$ ,  $C$ ,  $D$ , and  $E$  are temperature coefficients.

Substituting Eq. (15) into Eq. (14), we have

$$H_i^\ominus(t) = At + Bt^2/2 + Ct^3/3 + Dt^4/4 - E/t + F \quad (16)$$

$$S_i^\ominus(t) = A \ln t + Bt + Ct^2/2 + Dt^3/3 - E/2t^2 + G \quad (17)$$

$$G_i^\ominus(t) = A(t - \ln t) - Bt^2/2 - Ct^3/6 - Dt^4/12 - E/2t + F - Gt \quad (18)$$

where

$$F = H_{i,298.15}^\ominus - (At_R + Bt_R^2/2 + Ct_R^3/3 + Dt_R^4/4 - E/t_R) \quad (19)$$

$$G = S_{i,298.15}^\ominus - (A \ln t_R + Bt_R + Ct_R^2/2 + Dt_R^3/3 - E/2t_R^2) \quad (20)$$

and  $t_R = 0.29815$ .

The temperature coefficients  $A$ ,  $B$ ,  $C$ ,  $D$ ,  $E$ ,  $F$ , and  $G$  for the aqueous species  $\text{Li}^+(\text{aq})$  and  $\text{Cl}^-(\text{aq})$ , liquid water, and ice are determined prior to regression of the PSC equation parameters.

The temperature coefficients  $A$ ,  $B$ ,  $C$ ,  $D$  and  $E$  in Eq. (15) for the aqueous species  $\text{Li}^+(\text{aq})$  and  $\text{Cl}^-(\text{aq})$  are determined by fitting the individual isobaric heat capacity values calculated from the Helgeson–Kirkham–Flowers (HKF) equations of state (eos) [30,31] incorporated in the CHNOSZ software package [32] over the temperature range of 273.15 K to 523.15 K.  $H_{i,298.15}^\ominus$  and  $S_{i,298.15}^\ominus$  are calculated by the same software package, then from Eqs. (16) and (17) the coefficients  $F$  and  $G$  are determined.

The temperature coefficients in Eq. (15) for  $\text{H}_2\text{O}_{(l)}$  listed in the NIST Webbook [29] are only valid in the temperature range from 298 K to 500 K, which is insufficient for the thermodynamic description of some electrolyte systems, such as  $\text{LiCl} + \text{H}_2\text{O}$  where the solution temperature is as low as 194 K. Clegg and Brimblecombe [33] have discussed the problem of the heat capacity equation of supercooled water in detail. In the end, they adopted Hill's equation of state to derive a heat capacity equation for supercooled water that was valid to approximately 190 K, though the exploration of Hill's equation of state to subzero temperatures is inconsistent with the experimentally determined heat capacities of supercooled water [34,35]. We fit the experimental heat capacities of supercooled water using Eq. (15), and found that an accurate representation of the experimental data can only be obtained to approximately 230 K. Therefore, to obtain the temperature coefficients  $A$ ,  $B$ ,  $C$ ,  $D$ , and  $E$  for  $\text{H}_2\text{O}_{(l)}$  that are valid over a

**Table 1**The experimental data used for parameter determination of the LiCl+H<sub>2</sub>O system.

Experimental method	Data type	Fitted quantity	Temperature range/K	Composition range/mol kg <sup>-1</sup>	Data points	$\sigma_{\text{est}}^a$	$\sigma_{\text{fit}}^b$	Ref.
Isoopiestic	$\phi$	$\ln a_w$	318.15	0.5055–4.2057	19	0.003	0.0003	[42]
Isoopiestic	$\phi$	$\ln a_w$	323.15	0.3322–2.0149	10	0.003	0.0002	[43]
Vapor pressure	$\phi$	$\ln a_w$	298.15–373.15	1.0208–18.585	54	0.003	0.0048	[44]
Tables	$\phi$	$\ln a_w$	298.15	0.001–19.219	43	0.003	0.0025	[45]
Isoopiestic	$R$	$\ln a_w$	382.96 – 443.92	0.6264–5.5658	118	0.003	0.0033	[46]
Vapor pressure	$p$	$\ln a_w$	298.15	1.0–18.0	12	0.003	0.0051	[47]
Vapor pressure	$p$	$\ln a_w$	398.15, 423.15	0.9934, 0.9946	2	0.003	0.0009	[48]
Isoopiestic	$a_w$	$\ln a_w$	298.15	0.3044–18.992	23	0.003	0.0073	[49]
Isoopiestic	$a_w$	$\ln a_w$	298.15	0.5181–19.848	21	0.003	0.0054	[50]
Tables	$\phi$	$\ln a_w$	298.15	0.1–20.0	51	0.003	0.0048	[51]
Isoopiestic	$\phi$	$\ln a_w$	273.15	0.4819–9.1298	14	0.003	0.0040	[52]
Isoopiestic	$\phi$	$\ln a_w$	323.15	0.8675–8.1272	14	0.003	0.0023	[53]
Isoopiestic	$R$	$\ln a_w$	428.65	7.4194–20.949	16	0.003	0.0101	[54]
Vapor pressure	$p$	$\ln a_w$	291.15	0.725–15.59	14	0.003	0.0057	[55]
Vapor pressure	$p$	$\ln a_w$	298.15	0–19.22	22	0.01	0.0223	[56]
Vapor pressure	$p$	$\ln a_w$	303.15–373.15	3.496–18.675	72	0.005	0.0094	[57]
Vapor pressure	$p$	$\ln a_w$	323.15–373.15	0.4479–3.202	18	0.005	0.0039	[58]
Isoopiestic	$\phi$	$\ln a_w$	372.75	0.8–4.0	12	0.003	0.0016	[59]
Vapor pressure	$p$	$\ln a_w$	303.15 – 343.15	3.01–18.456	40	0.005	0.0084	[60]
Freezing point	$T_{\text{fus}}$	$\ln a_w$	197.45 – 262.35	2.5834–7.9476	8	0.003	0.0096	[61]
Freezing point	$T_{\text{fus}}$	$\ln a_w$	205.15 – 268.05	1.294–7.5315	10	0.003	0.0079	[62]
Freezing point	$\Delta T_{\text{fus}}$	$\ln a_w$	267.52–273	0.04381–1.4216	16	0.003	0.0004	[63]
Freezing point	$\Delta T_{\text{fus}}$	$\ln a_w$	268.351–272.91	0.06–1.18	5	0.003	0.0014	[64]
Freezing point	$\Delta T_{\text{fus}}$	$\ln a_w$	251.61–273.1	0.0141–3.8946	22	0.003	0.0006	[65]
Saturated vapor pressure	$p_{\text{sat}}$	$\ln a_w$	288.15–393.15	18.49–31.11	16	0.01	0.1146	[66]
Saturated vapor pressure	$p_{\text{sat}}$	$\ln a_w$	333.6–413.25	23.39–31.68	15	0.01	0.0620	[67]
Saturated vapor pressure	$p_{\text{sat}}$	$\ln a_w$	233.8–283.4	11.406–17.706	7	0.01	0.0528	[68]
e.m.f	$\gamma_{\pm}$	$\ln \gamma_{\pm}$	273.15–308.15	0.05–5.0	19	0.003	0.0099	[69]
e.m.f	$\gamma_{\pm}$	$\ln \gamma_{\pm}$	273.15–323.15	0.1–6.0	65	0.05	0.0524	[70]
Tables	$\gamma_{\pm}$	$\ln \gamma_{\pm}$	298.15	0.001 – 19.219	43	0.005	0.0072	[45]
Tables	$\gamma_{\pm}$	$\ln \gamma_{\pm}$	298.15	0.1–20.0	51	0.005	0.0110	[51]
Calorimetric	$\Delta_{\text{dil}}H_m$	$\Delta_{\text{dil}}H_m/RT$	373.15, 423.65	0.0155–16.508	37	0.008	0.0255	[71]
Calorimetric	$\Delta_{\text{dil}}H_m$	$\Delta_{\text{dil}}H_m/RT$	303.15	0.2416–1.1499	18	0.008	0.0147	[72]
Calorimetric	$\Delta_{\text{dil}}H_m$	$\Delta_{\text{dil}}H_m/RT$	298.15	0.1378–3.0	9	0.008	0.0142	[73]
calorimetric	$\Delta_{\text{dil}}H_m$	$\Delta_{\text{dil}}H_m/RT$	293.15	0.1388–2.2204	4	0.008	0.0197	[74]
Calorimetric	$\Delta_{\text{dil}}H_m$	$\Delta_{\text{dil}}H_m/RT$	298.15	0.25–6.75	9	0.008	0.0281	[75]
Calorimetric	$\Delta_{\text{sol}}H_m$	$\phi L_m/RT$	298.15	0.1388–19.900	41	0.14	0.1358	[76]
Calorimetric	$\phi C_{p,m}$	$\phi C_{p,m}/R$	298.15	0.0455–0.1	3	0.6	0.2417	[77]
Calorimetric	$\phi C_{p,m}$	$\phi C_{p,m}/R$	298.15	0.1–0.96	8	0.06	0.2728	[77]
Calorimetric	$\phi C_{p,m}$	$\phi C_{p,m}/R$	303.15–403.15	0.497–1.755	33	0.06	0.2542	[78]
Calorimetric	$\phi C_{p,m}$	$\phi C_{p,m}/R$	298.15	0.04–2.4614	17	1.55	0.7583	[79]
Calorimetric	$c_p$	$\phi C_{p,m}/R$	308.15–343.15	4.1630–19.316	56	0.06	0.1102	[80]
Calorimetric	$c_p$	$\phi C_{p,m}/R$	299.65	0.00–19.8779	36	0.12	0.3120	[76]
Calorimetric	$c_p$	$\phi C_{p,m}/R$	293	2.2204	4	0.06	0.1497	[74]
Thermal analysis	$(T, m_s)$	$\ln K$	199.25–249.45	8.3101–13.1835	8	0.02	0.0595	[61]
Visual polythermal	$(T, m_s)$	$\ln K$	194.65–291.4	8.2455–19.1924	28	0.02	0.03	[62]
Visual polythermal	$(T, m_s)$	$\ln K$	207.75–333.15	9.7057–23.3651	23	0.02	0.0316	[81]
Isothermal	$(T, m_s)$	$\ln K$	273.15–372.65	16.064–29.83	14	0.02	0.0358	[82]
Isothermal	$(T, m_s)$	$\ln K$	273.15, 290.65	16.064–18.9993	2	0.02	0.0219	[83]
Isothermal	$(T, m_s)$	$\ln K$	273.15, 373.15	16.325, 29.78	2	0.02	0.0368	[84]
Isothermal	$(T, m_s)$	$\ln K$	273.15, 353.15	16.305, 26.294	4	0.02	0.0253	[85]
Isothermal	$(T, m_s)$	$\ln K$	273.15, 323.15	16.211, 22.056	2	0.02	0.0133	[86]
Isothermal	$(T, m_s)$	$\ln K$	283.15, 323.15	17.536, 21.986	2	0.02	0.0182	[87]
Isothermal	$(T, m_s)$	$\ln K$	274.2–413.45	16.325–32.981	14	0.02	0.0138	[67]
Isothermal	$(T, m_s)$	$\ln K$	273.15–361.15	16.292–28.3023	21	0.02	0.0192	[88]
Isothermal	$(T, m_s)$	$\ln K$	344.65–413.65	25.160–33.199	15	0.02	0.0113	[89]
Visual polythermal	$(T, m_s)$	$\ln K$	277.45–398.12	16.8596–32.06	18	0.02	0.0164	[90]
Isothermal	$(T, m_s)$	$\ln K$	291.15	19.5523	1	0.02	0.0331	[55]
Isothermal	$(T, m_s)$	$\ln K$	298.15	19.9585	1	0.02	0.0144	[51]
Isothermal	$(T, m_s)$	$\ln K$	298.15	19.2234	1	0.02	0.1313	[56]

<sup>a</sup> Estimated standard deviation as respect to the fitted quantity.<sup>b</sup> Standard deviation of the fitting as respect to the fitted quantity.

wide temperature from 190 K to 523 K, we fit them to the heat capacities of water calculated from Hill's equation of state at temperatures below zero and the NIST Webbook equation at temperatures above zero. From the standard enthalpy and entropy of H<sub>2</sub>O<sub>(l)</sub> at 298.15 K listed in the NIST Webbook, the coefficients  $F$  and  $G$  for H<sub>2</sub>O<sub>(l)</sub> are determined with Eqs. (19) and (20).

Feistel and Wagner [36] listed individual evaluated heat capacities of H<sub>2</sub>O<sub>(cr,l)</sub> from 0 K to 273 K, from which the temperature coefficients  $A$ ,  $B$ ,  $C$ ,  $D$ , and  $E$  for H<sub>2</sub>O<sub>(cr,l)</sub> are determined by fitting

over the temperature range from 180 K to 273 K. Starting from the enthalpy (–292.744 kJ mol<sup>-1</sup>) and entropy (44.776 J mol<sup>-1</sup> K<sup>-1</sup>) of ice at 298.15 K reported by Kobaylin et al. [37], the standard Gibbs energy of H<sub>2</sub>O<sub>(cr,l)</sub> as a function of temperature in the form of Eq. (18) is determined.

To simulate the solid–liquid equilibria (SLE), the standard Gibbs free energy  $G_i^{\text{el}}(T)$  for a solid phase  $M_{\text{vM}}X_{\text{vX}} \cdot n\text{H}_2\text{O}_{(\text{s})}$  as function of temperature, i.e., Eq. (18), is necessary. These coefficients can be

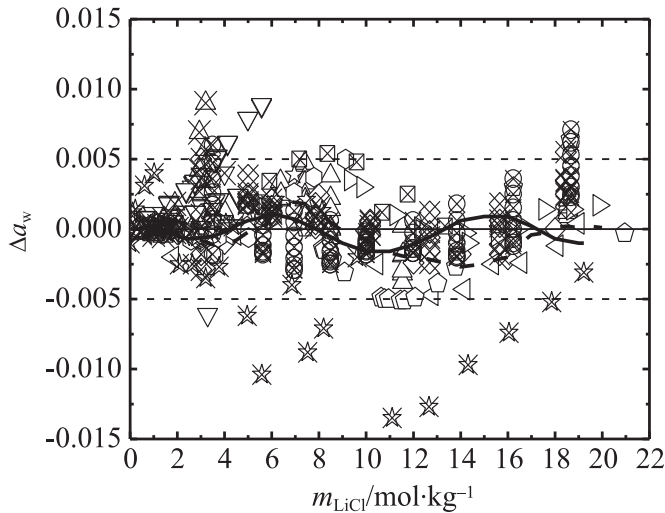
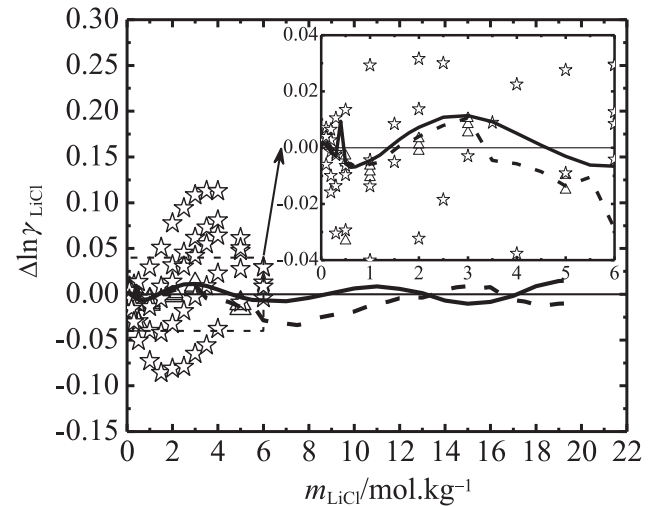


**Table 2**Gibbs free energy functions of aqueous and solid species in the LiCl+H<sub>2</sub>O system at standard state.

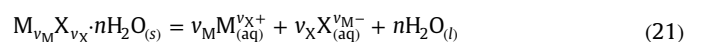
Species	$G_f^\circ(t) = A(t - \ln t) - Bt^2/2 - Ct^3/6 - Dt^4/12 - E/2t + F - Gt^a$							T/K
	A	B	C	D	E	F	G	
Li <sup>+</sup> <sub>(aq)</sub> <sup>b</sup>	4908.41	−26,562.4	54573.6	−40,213.6	−63.4622	−1176.824	11,443.528	273–523
Cl <sup>−</sup> <sub>(aq)</sub> <sup>b</sup>	29,421.3	−157,725	316,626	−227,316	−412.404	−5660.068	68,302.467	273–523
H <sub>2</sub> O <sub>(l)</sub> <sup>c</sup>	−90.0669	748.166	−1377.94	1055.31	3.26118	−271.203	−191.886	180–523
H <sub>2</sub> O <sub>(cr,l)</sub> <sup>d</sup>	13.44	20.2535	371.643	−418.377	−0.0301987	−300.209	42.01	100–273
LiCl <sub>(cr)</sub> <sup>e</sup>	43.7437	20.3706	0.3064	−0.0942	−0.1604	−423.3378	106.7998	368–403
LiCl · H <sub>2</sub> O <sub>(cr)</sub> <sup>f</sup>	−429.3131	1746.9163	0	0	0	−662.5562	−940.5144	291–371
LiCl · 2H <sub>2</sub> O <sub>(cr)</sub> <sup>f</sup>	112.3047	76.2211	0	0	0	−1050.1934	251.3980	248–292
LiCl · 3H <sub>2</sub> O <sub>(cr)</sub> <sup>f</sup>	−1447.8245	5454.8197	0	0	0	−1126.6395	−3220.1464	205–253
LiCl · 5H <sub>2</sub> O <sub>(cr)</sub> <sup>f</sup>	−3647.1742	13,123.2743	0	0	0	−1417.0329	−8150.9733	194–208

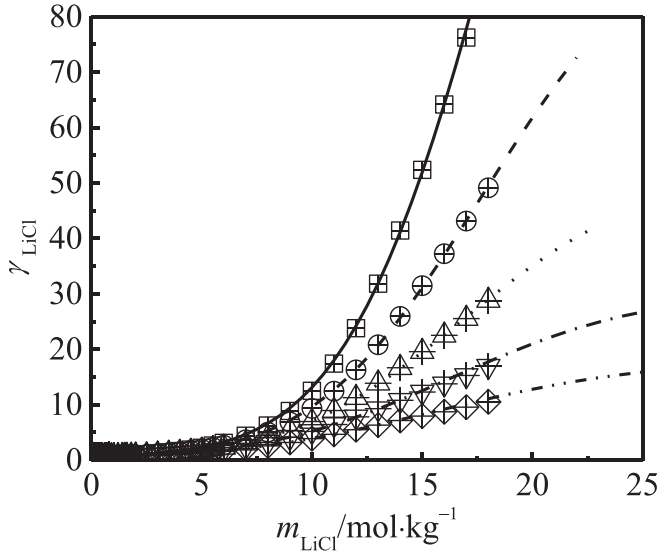
<sup>a</sup>  $t = (T/K)/1000$ .<sup>b</sup> The parameters A, B, C, D, and E are determined by fitting the heat capacity values calculated from the HKF eos [30, 31] temperature from 273.15 K to 523.15 K, and further the parameters F and G are determined from Eqs. (19) and (20) with the calculated standard enthalpy of formation and standard entropy from the same eos at 298.15 K.<sup>c</sup> See text.<sup>d</sup> The parameters A, B, C, D, and E are determined from the evaluated heat capacity of H<sub>2</sub>O(cr, l) [36], and the standard enthalpy of formation and standard entropy of ice at 298.15 K are taken from [37].<sup>e</sup> The parameters A, B, C, D, and E are taken from the NIST webbook [29], and the parameters F and G are determined in this work.<sup>f</sup> All parameters are determined in this work.**Table 3**The assessed PSC equation parameters for LiCl(aq) in this work according to Eq. (8).<sup>a</sup>

Parameter	$P(T) = a_0 + a_1T + a_2T \ln(T) + a_3T^2 + a_4T^3 + a_5/T$					
	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$
$B_{MX}$	1.3010382052E+05	−3.1705782693E+03	5.3668013223E+02	−9.5789670500E−01	3.0982145524E−04	−5.8444748172E+06
$B_{MX}^1$	−1.2387122226E+04	6.3919531162E+01	−1.4788013388E−01	−1.4622455132E−01	1.2411839690E−04	1.0684222082E+06
$W_{1,MX}$	−1.3864671327E+04	3.3123688967E+02	−5.5662564035E+01	9.2621743326E−02	−2.5628544062E−05	6.3728226406E+05
$U_{1,MX}$	−2.2118502055E+04	5.6608505408E+02	−9.6801383941E+01	1.8397236076E−01	−6.3850511009E−05	9.3580509545E+05
$V_{1,MX}$	7.6423337014E+03	−1.7462518431E+02	2.8910893675E+01	−4.1523732843E−02	7.3586558412E−06	−3.6887115877E+05

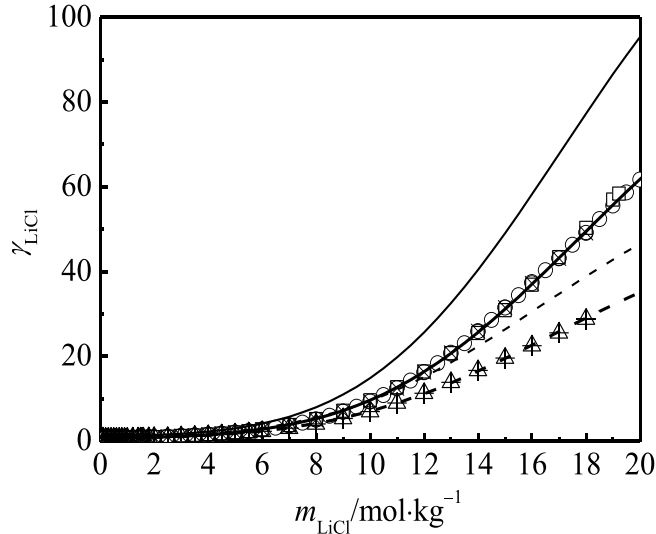
<sup>a</sup>  $\alpha = 13.0$ ,  $\alpha_1 = 2.0$ **Fig. 1.** Differences  $\Delta a_w = a_w(\text{expt}) - a_w(\text{calc})$  of the experimental water activities from those calculated in this work for unsaturated solution.  $\square$ : 318.15 K [42],  $\circ$ : 323.15 K [43],  $\triangle$ : 298.15 K to 373.15 K [44],  $\nabla$ : 382.96 K to 473.61 K [46],  $\diamond$ : 298.15 K [47],  $\triangleleft$ : 298.15 K [49],  $\triangleright$ : 298.15 K [50],  $\circ$ : 273.15 K [52],  $\star$ : 323.15 K [53],  $\diamond$ : 428.65 K [54],  $\triangleleft$ : 291.15 K [55],  $\times$ : 298.15 K [56],  $\boxtimes$ : 303.15 K to 373.15 K [57],  $\boxtimes$ : 323.15 K to 373.15 K [58],  $\boxtimes$ : 372.75 K [59],  $\boxtimes$ : 303.15 K to 343.15 K [60], thick solid line: 298.15 K table values [45], thick dash line: 298.15 K table values [51].**Fig. 2.** Difference  $\Delta \ln \gamma_{LiCl} = \ln \gamma_{LiCl}(\text{expt}) - \ln \gamma_{LiCl}(\text{calc})$  of the experimental mean ionic activity coefficients from those calculated with this model.  $\triangle$ : [69],  $\star$ : [70], thick solid line: 298.15 K [45], thick dash line: 298.15 K [51].

obtained by fitting the SLE data of the dissolution reaction:





**Fig. 3.** Mean ionic activity coefficients of LiCl(aq) at various temperatures. All symbols are literature data [44]:  $\square$ : 273.15 K;  $\bigcirc$ : 298.15 K;  $\triangle$ : 323.15 K;  $\diamond$ : 348.15 K,  $\nabla$ : 373.15 K. All lines are model values in this work.



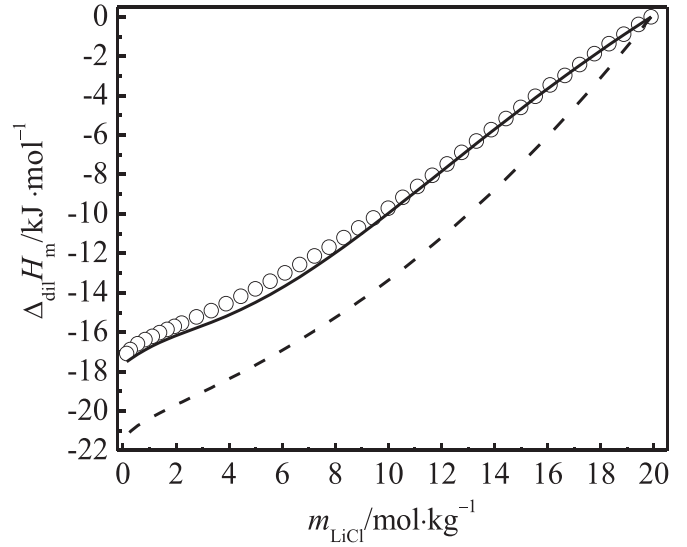
**Fig. 4.** Mean ionic activity coefficients of LiCl(aq) at various temperatures.  $\bigcirc$ : 298.15 K [44],  $\triangle$ : 323.15 K [44],  $\square$ : 298.15 K [45],  $\bigcirc$ : 298.15 K [51], thick solid line: model values at 298.15 K in this work, thick dash line: model values at 323.15 K in this work, thin solid line: calculated with the model parameters in Ref. [92] at 298.15 K, thin dash line: calculated with the model parameters in Ref. [92] at 323.15 K.

at various temperatures with the following thermodynamic relationships

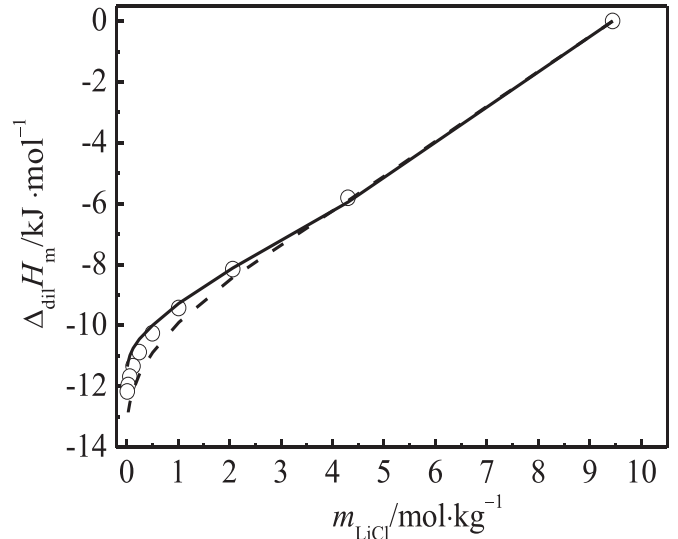
$$G_{m,M_{vM}^{vX} \cdot nH_2O(s)}^\theta = v_M G_{m,M_{(aq)}^{vX+}}^\theta + v_X G_{m,X_{(aq)}^{vM-}}^\theta + n G_{m,H_2O(l)}^\theta + RT \ln K \quad (22)$$

where  $K = a_M^v a_X^v a_{H_2O}^n$ ,  $G_{m,M_{vM}^{vX} \cdot nH_2O(s)}^\theta$ ,  $G_{m,M_{(aq)}^{vX+}}^\theta$ ,  $G_{m,X_{(aq)}^{vM-}}^\theta$ , and  $G_{m,H_2O(l)}^\theta$  are the standard molar Gibbs free energies of  $M_{vM}^{vX} \cdot nH_2O(s)$ ,  $M_{(aq)}^{vX+}$ ,  $X_{(aq)}^{vM-}$ , and  $H_2O(l)$ , respectively.  $a_i$  is the activity of substance  $i$  at saturation.

To eliminate the arbitrary nature of the parameters in Eq. (18) for a certain solid and to make the parameters more physically meaningful, the temperature coefficients  $A$ ,  $B$ ,  $C$ ,  $D$ , and  $E$  are fixed in advance according to the heat capacities in the form of Eq. (15). In most cases, the heat capacities of anhydrous salt solids are available. In the cases where the heat capacities of hydrated salts



**Fig. 5.** Plot of enthalpies of dilution against molality at 298.15 K for LiCl(aq). The initial molality is  $m_1 = 19.001 \text{ mol kg}^{-1}$ . The enthalpies of dilution are plotted as a function of the final molality  $m_2$ .  $\bigcirc$ : [76], and solid line: model values in this work, dash line: model values in the literature [93].



**Fig. 6.** Plot of enthalpies of dilution against molality at 373.15 K for LiCl(aq). The initial molality is  $m_1 = 9.443 \text{ mol kg}^{-1}$ . The enthalpies of dilution are plotted as a function of the final molality  $m_2$ .  $\bigcirc$ : [71], solid line: this model values, dash line: model values in the literature [93].

are unavailable, the following two approximation evaluation approaches are used:

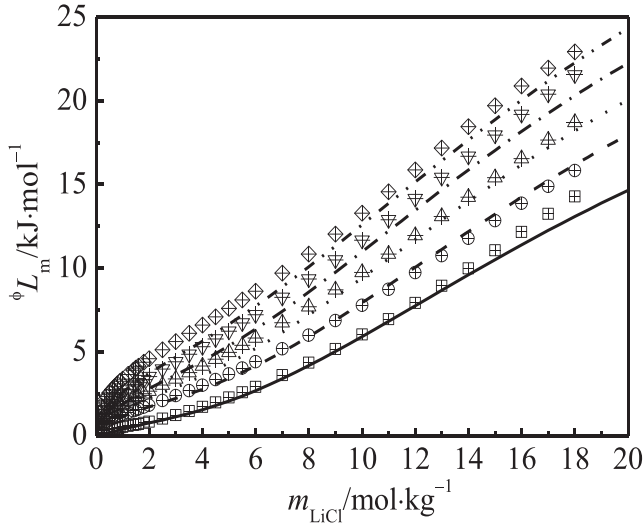
(1) An additivity rule is applied to estimate the heat capacity of a hydrated salt as a function of temperature, as expressed by Eq. (23).

$$C_{p,MX \cdot nH_2O(s)}^\theta(t) = C_{p,MX(s)}^\theta(t) + n C_{p,H_2O}^\theta \quad (23)$$

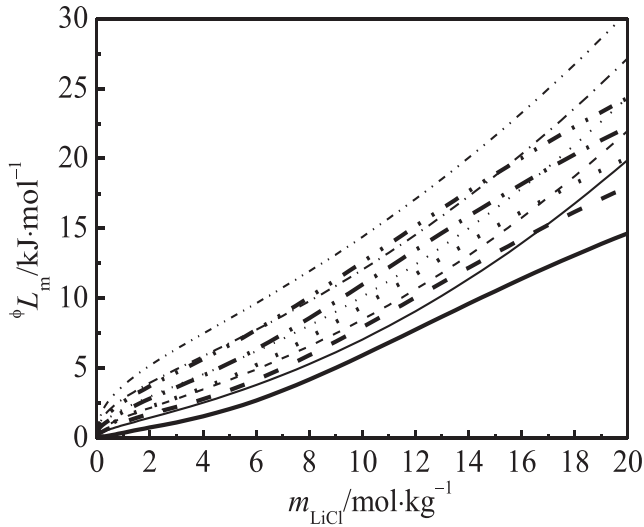
where  $C_{p,MX \cdot nH_2O(s)}^\theta(t)$  and  $C_{p,MX(s)}^\theta(t)$  are the heat capacity of the hydrated and anhydrous salt at temperature  $t$ , respectively, and  $C_{p,H_2O(l)}^\theta$  is the group contribution of one crystal water molecular to the heat capacity of the hydrated salt independent of temperature and set to  $43.5 \text{ J K}^{-1} \text{ mol}^{-1}$  as recommended by Archer [38].

(2) An alternative approach is to express the heat capacity of a hydrated salt solid using a simplified form Eq. (24):

$$C_{p,MX \cdot nH_2O(s)}^\theta(t) = A + Bt \quad (24)$$



**Fig. 7.** Apparent relative molal enthalpies of LiCl(aq) at various temperatures. Symbols: literature values [44],  $\square$ : 273.15 K,  $\circ$ : 298.15 K,  $\triangle$ : 323.15 K,  $\nabla$ : 348.15 K,  $\diamond$ : 373.15 K. Lines: this model values, solid line: 273.15 K, dash line: 298.15 K, dot line: 323.15 K, dash dot line: 348.15 K, dash dot dot line: 373.15 K.



**Fig. 8.** Comparisons of the apparent relative molal enthalpies of LiCl(aq). Thick lines, this work; thin lines, Holmes and Mesmer [93]; solid line: 273.15 K, dash line: 298.15 K, dot line: 323.15 K, dash dot line: 348.15 K, dash dot dot line: 373.15 K.

When the heat capacity at 298.15 K is known, Eq. (24) can be simplified as

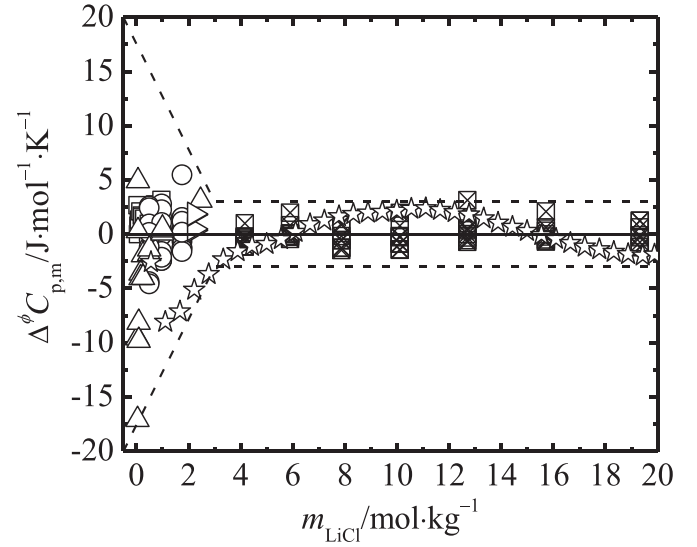
$$C_{p,MX \cdot nH_2O(s)}^\theta(t) = C_{p,MX \cdot nH_2O(s)}^\theta(0.29815) + (t - 0.29815)B \quad (25)$$

In this case, the parameter  $C_{p,MX \cdot nH_2O(s)}^\theta(0.29815)$  is evaluated by Eq. (23).

The remaining coefficients  $B$ ,  $F$  and  $G$  for all salts (anhydrous and hydrated), along with the PSC model parameters, are regressed by fitting the experimental activity and thermal property data for the aqueous phases, as well as the SLE data.

### 3. Parameter regression method

Multiple properties of an electrolyte system, i.e., water activity ( $a_w$ ), mean ionic activity coefficient ( $\gamma_{\pm}$ ), enthalpy of dilution ( $\Delta_{dil}H_m$ ), apparent relative molal enthalpy ( $\phi L_m$ ), apparent molal heat capacity ( $\phi C_{p,m}$ ) and solid–liquid equilibria data ( $T$ ,  $m_s$ ), are



**Fig. 9.** Difference  $\Delta\phi C_{p,m} = \phi C_{p,m}(\text{expt}) - \phi C_{p,m}(\text{calc})$  of the experimental apparent molal heat capacity of LiCl(aq) from those calculated with this model.  $\triangleright$ : [74],  $\star$ : [76],  $\square$ : [77],  $\circ$ : [78],  $\triangle$ : [79],  $\diamond$ : [80]. Dash lines: evaluated measurement errors of apparent molal heat capacity.

used simultaneously to regress the model parameters using a weighted least square method.

The objective function (OF) of a weighted least square is

$$OF = \sum_{i=1}^n w_i (P_i^c - P_i^e)^2 \quad (26)$$

where  $n$  is the number of properties (expressed as  $P_i$ ) to be reproduced,  $P_i^c$ ,  $P_i^e$  and  $w_i$  are the calculated and experimental values of property  $i$  and the weight factor of property  $i$ , respectively.  $w_i$  values are calculated from the standard deviation  $\sigma_i$  of property  $i$  from Eq. (27)

$$w_i = \frac{1}{\sigma_i^2} \quad (27)$$

where, the standard deviation  $\sigma_i$  of property  $i$  is estimated with the following steps: (1) To get a initial estimate on  $\sigma_i$  of property  $i$  (for each set of data the  $\sigma_i$  is the same), each set of data listed in Table 1 are fitted with the thermodynamic model separately. (2) With these estimated standard deviations of each set of data, all the data are fitted in one simultaneous, and then the standard deviations of overall fitting are calculated and compared with the initial estimates. (3) Adjust the initial estimates of the standard deviations to meet the overall fitting, and then go to (2) until all the new generated standard deviations are agreed with the values of the overall fitting generally.

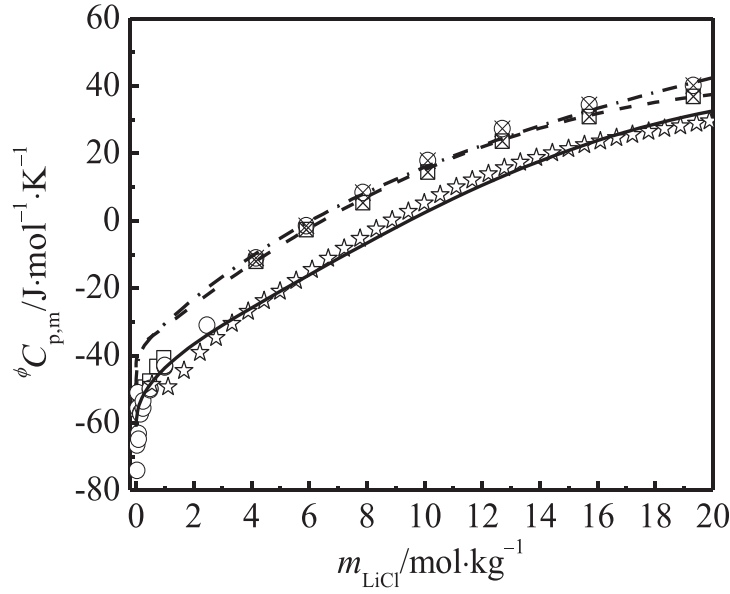
The property terms include  $\ln a_w$ ,  $\ln \gamma_{\pm}$ ,  $\Delta_{dil}H_m/RT$ ,  $\phi L_m/RT$ ,  $\phi C_{p,m}/R$ , and  $\ln K$  and are approximately in the same order of magnitude. A parameter regression program named PSCBREG was written for this purpose, where the standard weighted linear least squares algorithm implemented in the GNU scientific library [39] is called for the optimization.

For the experimental data given in a form other than  $a_w$ ,  $\gamma_{\pm}$ ,  $\Delta_{dil}H_m$ ,  $\phi L_m$ , or  $\phi C_{p,m}$ , necessary conversions have been made to adapt to the parameter regression program.

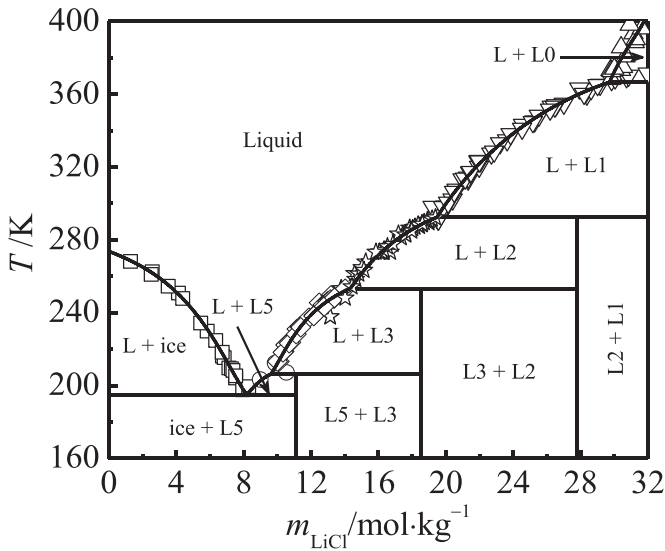
Experimental osmotic coefficients given in isopiestic ratios referred to NaCl(aq) are converted to water activity  $a_w$  as a function of NaCl concentration recommended by Pitzer et al. [40].

Vapor pressure data are converted to water activity  $a_w$  with the following equation:

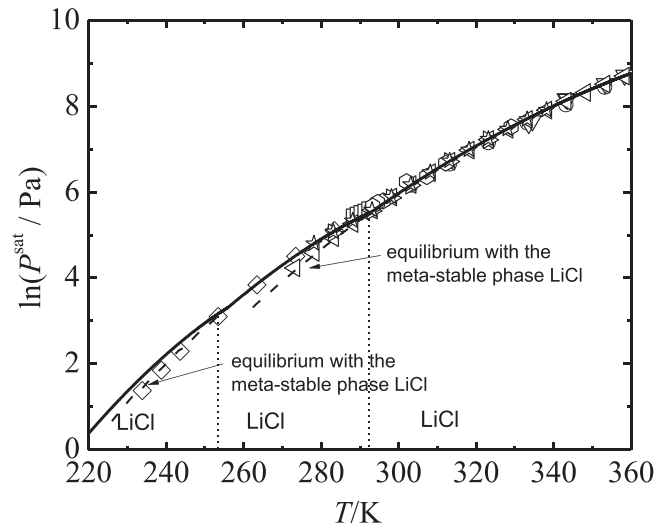




**Fig. 10.** Apparent molal heat capacities of LiCl(aq) at about 299.65 K, 323.15 K and 343.15 K. ☆: 299.65 K [76], ○: 298.15 K [77], □: 298.15 K [79], △: 323.15 K [80], ⊠: 343.15 K [80]. Lines: this model values, solid line: 299.65 K, dash line: 323.15 K, dash dot line: 343.15 K.



**Fig. 11.** Phase diagram of LiCl + H<sub>2</sub>O system temperature from 160 K to 400 K. L: Liquid, L0: LiCl(cr), L1: LiCl · H<sub>2</sub>O(cr), L2: LiCl · 2H<sub>2</sub>O(cr), L3: LiCl · 3H<sub>2</sub>O(cr), L5: LiCl · 5H<sub>2</sub>O(cr). □: ice [61,62], ○: L5 [61], ◇: L3 [61,62,81], ☆: L2 [61,62,67,81–83, 85–88,90], ▽: L1 [51,55,56,82,85–90], △: L0 [67,82,84,89,90].



**Fig. 12.** Vapor pressures of the LiCl(aq) solution saturated with LiCl · H<sub>2</sub>O(cr), LiCl · 2H<sub>2</sub>O(cr) and LiCl · 3H<sub>2</sub>O(cr). □: LiCl · 2H<sub>2</sub>O(cr) [66], ○: LiCl · H<sub>2</sub>O(cr) [66], ▽: LiCl · H<sub>2</sub>O(cr) [67], ⊙: solid phase unknown [94], ☆: solid phase unknown [95], ▷: solid phase unknown [96], ◁: solid phase unknown [97], ◇: solid phase unknown [68], solid line: this model values (stable equilibria), dash line: this model values (metastable equilibria).

$$\ln a_w = \ln\left(\frac{p}{p_0}\right) + \frac{B_T(p - p_0)}{RT} \quad (28)$$

where  $B_T$  is the second virial coefficient taken from Ref. [41], and  $p_0$  is the vapor pressure of pure water taken from Ref. [28].

Data of freezing point or freezing point depression are converted to water activity by the following relation:

$$G_{m,H_2O(s)}^\theta = G_{m,H_2O(l)}^\theta + RT \ln a_w \quad (29)$$

where  $G_{m,H_2O(s)}^\theta$  and  $G_{m,H_2O(l)}^\theta$  are already known.

Experimental data of the enthalpy of solution are converted to apparent relative molal enthalpies based on Eq. (30)

$$\Delta_{sol}H_m(m) = \Delta_{sol}H_m(\infty) + \phi L_m(m) \quad (30)$$

where  $\Delta_{sol}H_m(m)$ ,  $\Delta_{sol}H_m(\infty)$  and  $\phi L_m(m)$  are the integral heat of solution at concentration  $m$ , the integral heat of solution at infinite dilution, and the apparent relative molal enthalpy at concentration  $m$ , respectively.

Specific heat capacity data are converted to apparent molal heat capacity of solute with Eq. (31)

$$\phi C_{p,m}(m) = M_s c_p(m) + \frac{1000}{m} (c_p(m) - c_p^0) \quad (31)$$

where  $\phi C_{p,m}(m)$  is the apparent molal heat capacity of solute,  $c_p(m)$  and  $c_p^0$  are the specific heat of aqueous solution concentration  $m$  and the specific heat of pure water, respectively.  $M_s$  is the molar mass of the solute.

**Table 4**

Literature data on the temperature and the saturated solution composition at two-solid saturation points of the LiCl+H<sub>2</sub>O system.

Solid phases	Trans. Temp. (K)	Comp. (wt%)	Ref.
Eutectic point Ice+LiCl·5H <sub>2</sub> O	189.15	25.2	[62]
	193.15	25.3	[98]
	198.15	24.8	[99]
	197.25	25.02	[100]
	197.65	25.3	[101]
	194.95	25.33	[102]
	193.88	25.64	[103]
	194.9	25.76	This work
Peritectic point LiCl·5H <sub>2</sub> O+LiCl·3H <sub>2</sub> O	205.95	29.3	[62]
	207.75	29.15	[81]
	205.15	28.7	[98]
	208.65	31.2	[99]
	207.75	29.39	[100]
	204.95	28.7	[101]
	205.95	29.05	[102]
	205.02	28.74	[103]
	206.35	29.0	This work
Peritectic point LiCl·3H <sub>2</sub> O+LiCl·2H <sub>2</sub> O	254.15	38.0	[62]
	252.65	37.8	[81]
	253.15	36.9	[98]
	255.15	38.5	[99]
	255.89	38.23	[100]
	253.25	36.9	[101]
	253.65	37.59	[102]
	254.18	37.46	[103]
Peritectic point LiCl·2H <sub>2</sub> O+LiCl·H <sub>2</sub> O	292.25	45.2	[62]
	292.55	45.15	[81]
	285.65	40.5	[98]
	291.65	45	[99]
	293.94	45.34	[100]
	292.25	45.2	[101]
	293.05	45.32	[102]
	293.86	45.54	[103]
Peritectic point LiCl·H <sub>2</sub> O+LiCl	292.4	45.23	This work
	366.65	–	[67]
	373.65	56.5	[98]
	371.15	56.7	[99]
	369.74	56.19	[100]
	366.95	55.8	[101]
	369	56.30	[102]
	367.15	–	[104]
	366.65	55.74	This work

#### 4. Thermodynamic modeling of the LiCl+H<sub>2</sub>O system

To determine the model parameters of the LiCl+H<sub>2</sub>O system, the water activity (or osmotic coefficient), the mean ionic activity coefficients, the enthalpy of dilution and solution, the heat capacity of the aqueous phase and solubility data are used. The data used are listed in Table 1, and cover a temperature range from 194 K to 443 K and a concentration range from infinitely dilute to the solubility limit.

The temperature coefficients  $A$ ,  $B$ ,  $C$ ,  $D$  and  $E$  in the heat capacity, standard Gibbs energy, enthalpy and entropy equations of LiCl(cr) are taken from the NIST Webbook directly. Eq. (25) is used to represent the temperature dependence of the heat capacity for LiCl·H<sub>2</sub>O(cr), LiCl·2H<sub>2</sub>O(cr), LiCl·3H<sub>2</sub>O(cr) and LiCl·5H<sub>2</sub>O(cr). The remaining coefficients  $F$  and  $G$  for LiCl(cr) and  $B$ ,  $F$  and  $G$  for LiCl·H<sub>2</sub>O(cr), LiCl·2H<sub>2</sub>O(cr), LiCl·3H<sub>2</sub>O(cr) and LiCl·5H<sub>2</sub>O(cr) are

determined together with the PSC equation parameters in one simultaneous regression. The obtained standard Gibbs energy equations for all of the species are shown in Table 2.

The regressed PSC equation parameters for LiCl(aq) are listed in Table 3 with the temperature dependence of Eq. (8). The standard deviations of the overall fitting with respect to the terms  $\ln a_w$ ,  $\ln \gamma_{\pm}$ ,  $\Delta_{\text{dil}}H_m/RT$ ,  $\phi_{L_m}/RT$ ,  $\phi_{C_{p,m}}/R$ , and  $\ln K$  are 0.007, 0.085, 0.0324, 0.0218, 0.1358, 0.3207, and 0.0286, respectively.

##### 4.1. Water activity

The standard deviations of the water activity at all temperatures are 0.0024 and 0.01 for the unsaturated and saturated solutions, respectively. The water activity deviations between the literature and the values computed in this work for the unsaturated solutions are shown in Fig. 1. Most derivations fall in the range of  $\pm 0.005$ . At 298.15 K, our model values agreed with the recommended values [45,51].

The data (crossed star in Fig. 1) of Pearce and Nelson [56] at 298.15 K depart from the model values significantly with a maximum error of 0.0135; thus, they are unreliable. The same conclusion has been drawn by Zeng and Zhou [91].

The deviations of the model values from the experimental data (open down-triangle in Fig. 1) reported by Holmes and Mesmer [46] are relatively large. Possibly, the validity of the model decreases at high temperatures.

##### 4.2. Mean ionic activity coefficient

In the parameter regression, the literature data [45,51,69,70] for the mean ionic activity coefficients of LiCl(aq) are applied. Among them, the data from [69,70] are electrochemical cell results, and the data from [45,51] are recommended. The model values in this work agree with the data [45,51,70] satisfactorily, as shown in Fig. 2. The experimental data reported by Caramazza [70] are remarkably scattered. It is pleasing that the model results in this work agree with another set of model values reported by Gibbard and Scatchard [44] over a wide temperature range, as shown in Fig. 3, although the latter are never used in the parameter regression.

In our previous work [92], the PSC model parameters were determined by fitting to the water activities only. However, the calculated salt activity coefficients with these parameters differ from the present work remarkably, as shown in Fig. 4. The present model parameters are more reasonable, as they were obtained under more thermodynamic constraints.

##### 4.3. Thermal properties of LiCl(aq)

The standard deviation of the overall fitting for the enthalpy of dilution, enthalpy of solution, and apparent molal heat capacity are 67 J mol<sup>−1</sup>, 300 J mol<sup>−1</sup>, and 2.7 J K<sup>−1</sup> mol<sup>−1</sup>, respectively.

The enthalpy of dilution of LiCl(aq) calculated in this work agrees with the experimental data [71, 76] very well at 298.15 K and 373.15 K, however, quite differ from the values calculated by the Pitzer model parameters given by Holmes and Mesmer [93] at 298.15 K, as shown in Figs. 5 and 6. We notice that Holmes and Mesmer [93] evaluated their Pitzer model parameters in the LiCl concentrations below 9.443 mol kg<sup>−1</sup>. At higher LiCl concentrations, the validity of the model parameters could be weak.

Fig. 7 showed that the apparent relative molal enthalpy of LiCl(aq) calculated in this work agrees with those reported by Gibbard and Scatchard [44] very well, although the latter is not used in the present parameter regression.

Equivalently to the enthalpy of dilution, the apparent relative molal enthalpies of LiCl(aq) in this work differ from the model

**Table 5**Standard state thermodynamic values of solid phases at 298.15 K in LiCl+H<sub>2</sub>O system.

Solids	$\Delta_f G_m^0$ (kJ mol <sup>-1</sup> )	$\Delta_f H_m^0$ (kJ mol <sup>-1</sup> )	$S_m^0$ (J mol <sup>-1</sup> K <sup>-1</sup> )	$C_{p,m}^0$ (J mol <sup>-1</sup> K <sup>-1</sup> )	Ref.
LiCl(cr)	-389.72	-414.8	56.5	234.0	[100]
	-384.015	-408.26	-	48.03	[103]
	-384.37	-408.61	59.33	47.99	[105]
	-385.531	-	52.206	48.037	[106]
	-385.07	-408.85	59.06	48.04	This work
LiCl · H <sub>2</sub> O(cr)	-632.02	-714.55	97.18	494.1	[100]
	-631.8	-698.499	-	89.063	[103]
	-631.8	-712.58	102.84	-	[105]
	-631.728	-	101.838	84.4456	[106]
	-631.22	-712.91	99.87	91.53	This work
LiCl · 2H <sub>2</sub> O(cr)	-869.14	-1013.7	139.2	-	[100]
	-874.244	-996.125	-	130.095	[103]
	-	-1012.65	-	-	[105]
	-874.136	-	145.901	130.001	[106]
	-873.51	-1013.32	138.22	135.03	This work
LiCl · 3H <sub>2</sub> O(cr)	-1106.27	-1309.12	188.3	-	[100]
	-1114.98	-1287.94	-	171.128	[103]
	-	-1311.3	-	-	[105]
	-1114.73	-	198.775	113.456	[106]
	-1112.50	-1315.86	158.31	178.53	This work
LiCl · 5H <sub>2</sub> O(cr)	-1580.53	-1889.11	302.24	-	[100]
	-1592.2	-1871.19	-	253.193	[103]
	-1592.53	-	337.3417	298.807	[106]
	-1583.80	-1921.15	175.39	265.53	This work

values by Holmes and Mesmer [93], as seen in Fig. 8.

The differences of the apparent molal heat capacity of LiCl(aq) between literature values and the model values in this work are plotted in Fig. 9. Most of the deviations falls in the range of  $\pm 2.0$  J K<sup>-1</sup> mol<sup>-1</sup>. The deviations increase reasonably at dilute solutions. Fig. 10 showed the calculated apparent molal heat capacity isotherms in this work compared with the experimental data from literature at 298.15 K, 323.15 K and 343.15 K. We can see the model reproduces these experimental data excellently.

#### 4.4. Phase diagram, invariant points and saturated vapor pressures

Figs. 11 and 12 show the phase diagram of the LiCl+H<sub>2</sub>O system and vapor pressures over saturated LiCl(aq) solutions, respectively. The calculated liquidus in the LiCl+H<sub>2</sub>O system showed excellent agreement with the experimental results. Simultaneously, the predicted water vapor pressure of saturated LiCl(aq) solutions agrees with most literature data [66,67,94–96], though it does deviate from some literature data [68,97] in a certain temperature range. Notably, Greenspan [97] and Morillon et al. [68] reported the vapor pressure data without the corresponding solid phases. When we extrapolated the vapor pressure lines of LiCl · 2H<sub>2</sub>O and LiCl · H<sub>2</sub>O to the lower meta-stable temperature ranges, the calculated results agree with the literature data [68,97] very well. Possibly, the authors reported the vapor pressure data at meta-stable states.

Invariant points in the LiCl+H<sub>2</sub>O system predicted from this model are listed in Table 4 and compared with literature values. The predicted invariant points agree with the most recent evaluations of Pátek and Klomfar [102] very well, except for the peritectic point for LiCl · H<sub>2</sub>O + LiCl.

#### 4.5. Standard state thermodynamics of the solid phases

The determined thermodynamic values of the solid phases at the standard state and 298.15 K are listed in Table 5. The thermodynamic values ( $\Delta_f G_m^0$ ,  $\Delta_f H_m^0$ ,  $S_m^0$ ,  $C_{p,m}^0$ ) for LiCl(cr), LiCl · H<sub>2</sub>O(cr)

and LiCl · 2H<sub>2</sub>O(cr) produced in this work agree with the literature values [100, 103, 105, 106] very well, except for the heat capacity values of LiCl(cr) and LiCl · H<sub>2</sub>O(cr) given by Monnin et al. [100]. These heat capacities of solids are significantly larger than the values from others. Slight differences appear in the data for the solids LiCl · 3H<sub>2</sub>O(cr). Obvious inconsistency of the data for the solid phase LiCl · 5H<sub>2</sub>O(cr) at 298.15 K arise among all of the reported data, including the present work. After all, extrapolation of data from the deeply low temperatures (195–206 K) to 298 K is a challenge for all researchers when the heat capacities of super-cooled liquid water are unknown at such low temperatures. Fortunately, the thermodynamic data of LiCl · 3H<sub>2</sub>O(cr) and LiCl · 5H<sub>2</sub>O (cr) are more important at lower temperatures than at 298 K, as these phases can only exist in multi-component systems at temperatures lower than their stable formation temperatures in binary systems based on the phase diagram rule.

## 5. Conclusions

The PSC model is selected to represent the thermodynamic properties of the salt lake brine systems containing Li-salts at multiple temperatures. The temperature dependence of the thermodynamic functions (entropy, enthalpy and Gibbs energy) for the aqueous species and the solid phases are determined using their heat capacities. In this way, the thermodynamic inner consistence of the parameters is held. Comprehensive thermodynamic properties, i.e., water activity, mean ionic activity coefficient, enthalpy of dilution and solution, heat capacity and solubility, are used to evaluate the model parameters. The proposed parameter regression strategy has proven successful in the highly soluble LiCl+H<sub>2</sub>O system, and the present thermodynamic model of the LiCl+H<sub>2</sub>O system is valid in the temperature range of 190 K to nearly 400 K. The present work forms a solid foundation for the thermochemical properties simulation of other complicated salt lake brine systems.

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## Appendix A. Supplementary material

Supplementary data associated with this article can be found in the online version at <http://dx.doi.org/10.1016/j.calphad.2015.05.001>.

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