

INTRO TO AI AND ML

(EE1390)

MATRIX PROJECT

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PROBLEM:31

A variable line drawn through the intersection of lines

$$\begin{bmatrix} 4 & 3 \end{bmatrix} X = 12$$

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meets the coordinate axes at A and B, then find the locus of the mid point.

Solution

The given linear equations are

$$\begin{bmatrix} 4 & 3 \\ 3 & 4 \end{bmatrix} X = \begin{bmatrix} 12 \\ 12 \end{bmatrix}$$

$$\text{Let } P = \begin{bmatrix} 4 & 3 \\ 3 & 4 \end{bmatrix},$$

$$Q = \begin{bmatrix} 12 \\ 12 \end{bmatrix}$$

$$PX = Q$$

$$X = P^{-1}Q$$

X is point of intersection

$$X = \begin{bmatrix} 1.714 \\ 1.714 \end{bmatrix};$$

Variable lines passing through X is

$$[m \ -1]X = 1.714(m-1)$$

where m is parameter

It meets coordinate axes at A and B respectively

$$A = \begin{bmatrix} a \\ 0 \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ b \end{bmatrix}$$

$$a = 1.714 \frac{m-1}{m}, \quad b = 1.714(1-m)$$

The locus of midpoint of A and B is C

$$C = \begin{bmatrix} x \\ y \end{bmatrix}$$

x, y are $\frac{a}{2}$ and $\frac{b}{2}$ respectively

$$x = \frac{0.8571(m-1)}{m}, \quad y = 0.8571(1-m)$$

$$\frac{y}{x} = -m$$

$$xy = 0.8571(x+y)$$

Therefore the locus is a hyperbola whose equation is

$$C = \begin{bmatrix} 0.8571(m-1)/m \\ 0.8571(1-m) \end{bmatrix}$$

m is parameter.

FIGURES

The figure of locus diagram

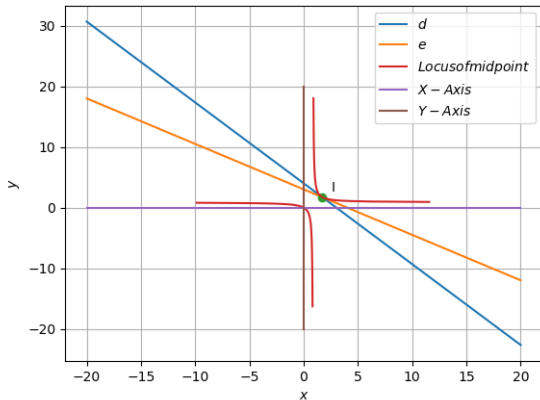


Figure: locus diagram

The figure of variable lines

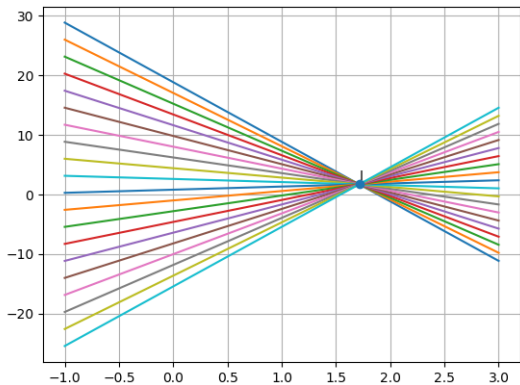


Figure: variable lines