

1.2.26

AI24BTECH11036 - Shreedhanvi Yadlpally

Question:

A man can swim with a speed of 4.0 km/h in still water. How long does he take to cross a river 1.0 km wide if the river flows steadily at 3.0 km/h and he makes his strokes normal to the river current? How far down the river does he go when he reaches the outer bank?

Solution:

Variable	Description
v_m	Speed of the man in still water
v_r	Speed of the river flow
w	Width of the river
t	Time taken to cross the river
d	Distance drifted downstream

TABLE 0: Variables Used

$$v_m = 4.0 \text{ km/h} \quad (0.1)$$

$$v_r = 3.0 \text{ km/h} \quad (0.2)$$

$$w = 1.0 \text{ km} \quad (0.3)$$

The man is swimming perpendicular to the river current, so his speed relative to the riverbank is 4.0 km/h (which is his speed in still water). Then,

$$t = \frac{w}{v_m} = \frac{1.0 \text{ km}}{4.0 \text{ km/h}} = 0.25 \text{ hours} \quad (0.4)$$

For the distance he drifts downstream when he reaches the other bank,

$$d = v_r \times t = 3.0 \text{ km/h} \times 0.25 \text{ hours} = 0.75 \text{ km} \quad (0.5)$$

For the resultant velocity vector

$$\mathbf{v}_m = \begin{pmatrix} 0 \\ 4 \end{pmatrix} \text{ km/h} \quad (0.6)$$

$$\mathbf{v}_r = \begin{pmatrix} 3 \\ 0 \end{pmatrix} \text{ km/h} \quad (0.7)$$

$$\mathbf{v}_{\text{res}} = \mathbf{v}_m + \mathbf{v}_r = \begin{pmatrix} 3 \\ 4 \end{pmatrix} \text{ km/h} \quad (0.8)$$

Swimmer's Velocity, River Current, and Resultant Velocity

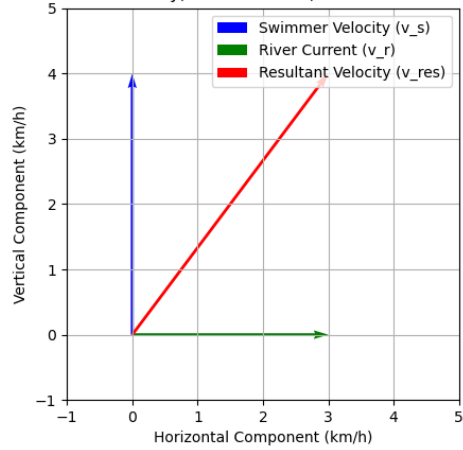


Fig. 0.1: Vector Plot