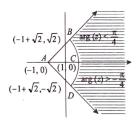
Assignment-1

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I. MCQ's with Single Correct Answer

1) The locus of z which lies in the shaded region (excluding the boundaries) is best represented by

(2005S)



- (a) z: |z+1| > 2 and $|arg(z-1)| < \frac{\pi}{4}$
- (b) z:|z-1|>2 and $|arg(z-1)|<\frac{\pi}{4}$
- (c) z: |z+1| < 2 and |arg(z+1)| <
- (d) z: |z-1| < 2 and $|arg(z+1)| < \frac{\pi}{2}$
- 2) a, b, c are integers, not all simultaneously equal and ω is the cube root of unity $(\omega \neq 1)$, then the minimum value of $|a + b\omega + c\omega^2| l$ is?

(2005S)

- (a) 0
- (b) 1
- (c) $\frac{\sqrt{3}}{2}$ (d) $\frac{1}{2}$
- 3) Let $\omega = \frac{-1}{2} + i\frac{\sqrt{3}}{2}$, then the value of det?

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -1 - \omega^2 & \omega^2 \\ 1 & \omega^2 & \omega^4 \end{vmatrix}$$
 (1)

(2002-2M)

- (a) 3ω
- (b) $3\omega(\omega-1)$
- (c) $3\omega^2$
- (d) $3\omega(1-\omega)$

4) If $\frac{w - \overline{w}z}{1 - z}$ is purely real where $w = \alpha + i\beta, \beta \neq 0$ and $z \neq 1$. Then the set of values of z is?

(2006-3M)

- (a) z : |z| = 1
- (b) $z: z = \overline{z}$
- (c) $z: z \neq 1$
- (d) $z : |z| = 1, z \neq 1$
- 5) A man walks a distance of 3 units from the origin towards the north-east (N 45°E) direction. From there, he walks a distance of 4 units towards the northwest (N 45°W) direction to reach a poit P. The position of P in the Argand Plane is (2007-3M)
 - (a) $3e^{\frac{i\pi}{4}} + 4i$
 - (b) $(3-4i)e^{\frac{i\pi}{4}}$
 - (c) $(4+3i)e^{\frac{i\pi}{4}}$
 - (d) $(3+4i)e^{\frac{i\pi}{4}}$
- 6) If |z| = 1 and $z \neq \pm 1$, then all the values of $\frac{z}{1-z^2}$ (2007-3M)
 - (a) a line not passing through origin
 - (b) $|z| = \sqrt{2}$
 - (c) the x-axis
 - (d) the y-axis
- 7) A particle P starts from the point $z_0 = 1 + 2i$, where $i = \sqrt{-1}$. It moves horizontally away from origin by 5 units and then vertically away from origin by 3 units to reach apoint z_1 . From z_1 , the particle moves $\sqrt{2}$ units in the direction of the vector $\hat{i} + \hat{j}$ and then it moves through an angle $\frac{\pi}{2}$ in anticlockwise direction on a circle with centre at origin, to reach a point z_2 . The point z_2 is given by (2008)
 - (a) 6 + 7i
 - (b) -7 + 6i
 - (c) 7 + 6i
 - (d) -6 + 7i
- 8) Let $z = \cos \theta + i \sin \theta$. Then the value of $\sum_{m=1}^{15}$ $\operatorname{Im}(z^{2m-1})$ at $\theta = 2^{\circ}$ is (2009)
 - (a) $\frac{1}{\sin 2^{\circ}}$ (b) $\frac{1}{3 \sin 2^{\circ}}$

- (c) $\frac{1}{2\sin 2^\circ}$
- (d) $\frac{1}{4\sin 2^{\circ}}$
- 9) Let z = x+iy be a complex number where x and y are integers. Then the area of the rectangle whose vertices are the roots of the equation: $z\bar{z}^3 + \bar{z}z^3 = 350$ is (2009)
 - (a) 48
 - (b) 32
 - (c) 40
 - (d) 80
- 10) Let z be a complex number such that the imaginary part of z is non-zero and $a = z^2 + z + 1$ is real. The a cannot take the value
 - (a) -1

 - (b) $\frac{1}{3}$ (c) $\frac{1}{2}$
 - (d) $\frac{3}{4}$
- 11) Let complex numbers α and $\frac{1}{\alpha}$ lie on circles $(x-x_0)^2 + (y-y_0)^2 = r^2$ and $(x-x_0)^2 + (y-y_0)^2 = r^2$ $4r^2$ respectively. If $z_0 = x_0 + iy_0$ satisfies the equatio $2|z_0|^2 = r^2 + 2$, the $|\alpha| =$
 - (a) $\frac{1}{\sqrt{2}}$

 - (b) $\frac{1}{2}$ (c) $\frac{1}{\sqrt{7}}$ (d) $\frac{1}{3}$
- 12) Let S be the set of all complex numbers z satisfying $|z - 2 + i| \ge \sqrt{5}$. If the complex number z_0 is such that $\frac{1}{|z_0-1|}$ is the maximum of the set $\{\frac{1}{|z-1|}: z \in S^{|z_0-1|}\}$, then the principal argument of $\frac{4-z_0-\overline{z_0}}{z_0-\overline{z_0}+2i}$ is (2019)
 - (a) $\frac{\pi}{4}$ (b) $\frac{3\pi}{4}$
 - (c) $\frac{\pi}{2}$
 - (d) $-\frac{\pi}{2}$
- II. MCQ's with One or More than One Correct
- 1) If $z_1 = a + ib$ and $z_2 = c + id$ are complex numbers such that $|z_1| = |z_2| = 1$ and $\text{Re}(z_1\overline{z_2}) = 0$, then the pair of complex numbers $w_1 = a + ic$ and $w_2 = b + id$ satisfies (1985 - 2 Marks)
 - (a) $|w_1| = 1$
 - (b) $|w_2| = 1$
 - (c) Re $(w_1\overline{w_2})=0$
 - (d) none of these.
- 2) Let z_1 and z_2 be complex numbers such that $z_1 \neq z_2$ and $|z_1| = |z_2|$. If z_1 has positive real

part and z_2 has negative imaginary part, then $\frac{z_1+z_2}{z_1-z_2}$ may be (1986 - 2 Marks)

- (a) zero
- (b) real and positive
- (c) real and negative
- (d) purely imaginary
- (e) none of the these.
- 3) If z_1 and z_2 are two non-zero complex numbers such that $|z_1 + z_2| = |z_1| + |z_2|$, then $\arg z_1 - \arg z_2$ is equal to (1987 - 2 Marks)
 - (a) $-\pi$
 - (b) $-\frac{\pi}{2}$
 - (c) 0
 - (d) $\frac{\pi}{2}$
 - (e) π
- 4) The value of $\sum_{k=1}^{6} (\sin \frac{2\pi k}{7} i \cos \frac{2\pi k}{7})$ is ...

(1987 - 2 Marks)

- (a) -1
- (b) 0
- (c) -i
- (d) *i*
- (e) None