B.TECH.

THEORY EXAMINATION (SEM–IV) 2016-17 THEORY OF AUTOMATA AND FORMAL LANGUAGES

Time: 3 Hours Max. Marks: 100

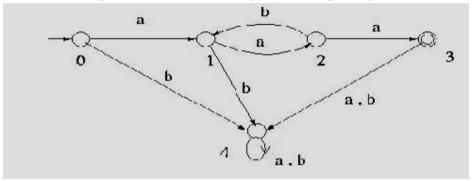
Note: Be precise in your answer. In case of numerical problem assume data wherever not provided.

SECTION - A

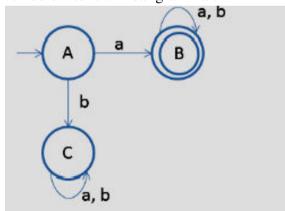
1. Explain the following:

 $10 \times 2 = 20$

- (a) Design the DFA that accepts an even number of a's and even number of b's.
- (b) Consider the DFA given below and identify the L accepted by the machine.



- (c) State the pumping lemma theorem for regular languages.
- (d) Convert the FA given below to left linear grammar.



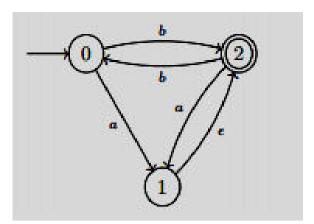
- (e) Check whether the grammar is ambiguous or not. $R-> R+R/RR/R^*/a/b/c$. Obtain the string $w=a+b^*c$
- (f) S->aB/bA A->a/aS/bAA B-> b/bS/aBB. Identify the strings obtained from this grammar.
- (g) Define PDA. Draw the graphical representation for PDA.
- (h) Design a PDA which accepts set of balanced paranthesis ({ { } } }).
- (i) Eliminate unit productions in the grammar. S->A/bb A->B/b B->S/a
- (j) What are checking off symbols?

SECTION - B

2. Attempt any five of the following questions:

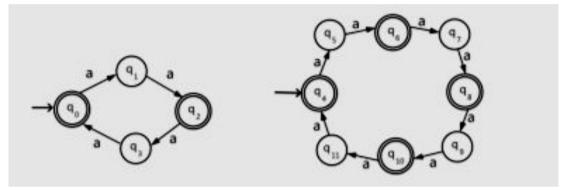
 $5 \times 10 = 50$

(a) (i) Convert the NFA- ε to DFA.



(ii) Check with the comparison method for testing equivalence of two FA given

below.



- **(b)** Prove that the compliment, homomorphism and inverse homomorphism, closure of a regular language is regular.
- (c) State and prove kleene's theorem with an example.
- (d) Consider the grammar with the production S->aSS A->b. Compute the string aababbb with the left most and right most derivation. Draw the derivation tree.
- (e) (i) Find out whether the language $L = \{x^n y^n z^n \mid n \ge 1\}$ is context free or not.
 - (ii) Construct a PDA that accepts $L = \{ ww^{R} | w = (a+b)^{*} \}$
- (f) (i) Convert the following CFG into CNF

$$S \to XY \mid Xn \mid p$$

$$X \rightarrow mX \mid m$$

$$Y \rightarrow Xn \mid o$$

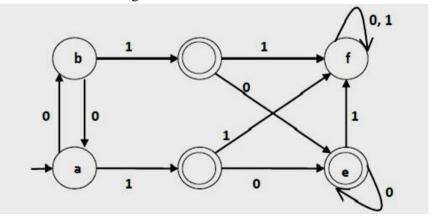
- (ii) Convert the following CFG into CNF $S \rightarrow ASA \mid aB, A \rightarrow B \mid S, B \rightarrow b \mid \epsilon$
- (g) Design a TM to recognize all strings consisting of an odd number of α 's.
- (h) Prove that the halting problem is undecidable.

SECTION - C

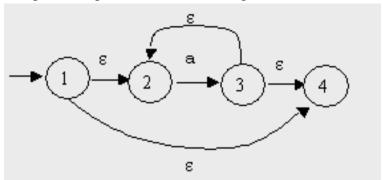
Attempt any two of the following questions:

 $2 \times 15 = 30$

3. (a) Minimize the automata given below



(b) Compute the epsilon- closure for the given NFA. Convert it into DFA.



- **4.** (a) Construct PDA to accept $L = \{0^n \ 1^n \mid n \ge 0\}$
 - (b) Construct a PDA from the following CFG. $G = (\{S, X\}, \{a, b\}, P, S) \text{ where the productions are } S \rightarrow XS \mid \epsilon, A \rightarrow aXb \mid Ab \mid ab$
- 5. (a) Prove that single tape machines can simulate multi tape machines.
 - (b) Design a TM to recognize all strings consisting of an odd number of α 's.