

Theory of Automata and Formal Language

Lecture-3

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Examples

Determine the languages generated by the following grammars:-

1. $S \rightarrow 0S1/0A1, A \rightarrow 1A/1$
2. $S \rightarrow aA, A \rightarrow bS, S \rightarrow \epsilon$
3. $S \rightarrow 0S1/0A/0/1B/1, A \rightarrow 0A/0, B \rightarrow 1B/1$
4. $S \rightarrow 0SBA/01A, AB \rightarrow BA, 1B \rightarrow 11, 1A \rightarrow 10, 0A \rightarrow 00$
5. $S \rightarrow 0S1/0A1, A \rightarrow 1A0/10$
6. $S \rightarrow 0A/1S/0/1, A \rightarrow 1A/1S/1$

Examples

Construct the grammars which generates the following languages:-

1. $L(G) = \{ a^n b a^m \mid m, n \geq 1 \}$
2. $L(G) =$ The set of all palindromes over $\{a, b\}$
3. $L(G) = \{ w c w^T \mid w \in \{a, b\}^* \}$
4. $L(G) = \{ a^n b^n c^i \mid n \geq 1 \text{ and } i \geq 0 \}$
5. $L(G) = \{ a^j b^n c^n \mid n \geq 1 \text{ and } j \geq 0 \}$
6. $L(G) = \{ a^n b^n c^n \mid n \geq 1 \}$

Examples

Construct the grammars which generates the following languages:-

1. $L(G) = \{ w \in \{a, b\}^* \mid \text{The number of a's in } w \text{ is divisible by } 3 \}$
2. $L(G) = \{ w \in \{a, b\}^* \mid w \text{ has an equal number of a's and b's} \}$
3. $L(G) = \{ w \in \{a, b\}^* \mid n_a(w) > n_b(w) \}$
4. $L(G) = \{ w \in \{a, b\}^* \mid n_a(w) \neq n_b(w) \}$
5. $L(G) = \{ 0^m 1^n 0^n 1^m \mid m, n \geq 1 \}$
6. $L(G) = \{ 0^n 1^{2n} \mid n \geq 1 \}$
7. $L(G) = \{ 0^n 1^n \mid n \geq 1 \} \cup \{ 1^m 0^m \mid m \geq 1 \}$
8. $L(G) = \{ 0^n 1^m 0^n \mid m, n \geq 1 \} \cup \{ 0^n 1^m 2^m \mid m, n \geq 1 \}$