

**B.Tech(2020-21)**  
**Discrete Structures and Theory of Logic(KCS 303)**  
**Assignment-4**

QNo.	Question	CO Type	Bloom's level
1	Obtain all distinct left cosets of $\{0, 3\}$ in the group $(Z_6, +_6)$ and find their union.	CO2	L2
2	Prove that $(R, +, *)$ is a ring with zero divisors, where $R$ is $2 \times 2$ matrix and $+$ and $*$ are usual addition and multiplication operations.	CO2	L4
3	Let $(A, *)$ be a monoid such that for every $x$ in $A$ , $x*x = e$ , where $e$ is the identity element. Show that $(A, *)$ is an abelian group.	CO2	L3
4	Let $Z$ be the group of integers with binary operation $*$ defined by $a*b = a+b-2$ , for all $a, b \in Z$ . Find the identity element of the group $(Z, *)$ .	CO2	L2
5	What do you mean by cosets of a subgroup? Consider the group $Z$ of integers under addition and the subgroup $H = \{\dots, -12, -6, 0, 6, 12, \dots\}$ considering of multiple of 6.  1. Find the cosets of $H$ in $Z$ .  2. What is the index of $H$ in $Z$ .	CO2	L4
6	What is Ring? Define elementary properties of Ring with example.	CO2	L1
7	Prove or disprove that intersection of two normal subgroups of a group $G$ is again a normal subgroup of $G$ .	CO2	L4
8	Consider the group $G = \{1, 2, 3, 4, 5, 6\}$ under multiplication modulo 7.  1. Find the multiplication table of $G$ .  2. Find $2^{-1}, 3^{-1}, 6^{-1}$ .  3. Find the orders and subgroups generated by 2 and 3.  4. Is $G$ cyclic?	CO2	L3

**Bloom's Taxonomy levels** (1- Remembering, 2- Understanding, 3- Applying, 4- Analyzing, 5- Evaluating, 6- Creating)

**CO** - Course Outcome

