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**LAB REPORT
On**

ANALYSIS AND DESIGN OF ALGORITHMS (23CS4PCADA)

Submitted by

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**in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING
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This is to certify that the Lab work entitled "**ANALYSIS AND DESIGN OF ALGORITHMS**" carried out by Dharunya Balavelavan (**1BM23CS090**), who is a bonafide student of **B. M. S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum during the year 2024-25. The Lab report has been approved as it satisfies the academic requirements in respect of Analysis and Design of Algorithms Lab - (**23CS4PCADA**) work prescribed for the said degree.

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Course outcomes:

CO1	Analyze time complexity of Recursive and Non-recursive algorithms using asymptotic notations.
CO2	Apply various design techniques for the given problem.
CO3	Apply the knowledge of complexity classes P, NP, and NP-Complete and prove certain problems are NP-Complete
CO4	Design efficient algorithms and conduct practical experiments to solve problems.

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NAME Dharunya Balavelavan SUBJECT ADA

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2.	✓	Quick sort	14/25	10 ✓
3.	✓	Prim's Algorithm	14/25	10 ✓
4.	✓	Kruskal's Algorithm	14/25	10 ✓
5.	✓	Topological ordering using source removal method	16/5/25	10 ✓
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7.	✓	Floyd's Algorithm	16/5/25	
8.	✓	Dijkstra's Algorithm	17/5/25	✓
9.	✓	count of range sum	17/5/25	10 ✓
10.	leet code	k-th largest element in array	17/5/25	10 ✓
11.	gns	course schedule	17/5/25	10 ✓
12.	gns	Pizza with 3n slices	17/5/25	10 ✓
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14.	✓	Maximum units on a truck	17/5/25	10 ✓
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17.	✓	Johnson Trotter	23/5/25	10 ✓
18.	✓	Heap sort	23/5/25	10 ✓

GITHUB LINK:

<https://github.com/Dharunya21/ADA->

Lab program 1:

Write a program to obtain the Topological ordering of vertices in a given digraph.

Code:

```
#include <stdio.h>

#define MAX 100

int adj[MAX][MAX], n, visited[MAX], stack[MAX], top = -1;

void dfs(int v) {

    visited[v] = 1;
    for (int i = 0; i < n; i++)
        if (adj[v][i] && !visited[i])
            dfs(i);
    stack[++top] = v;
}

void topologicalSort() {
    for (int i = 0; i < n; i++)
        if (!visited[i])
            dfs(i);
    while (top >= 0)
        printf("%d ", stack[top--]);
}

int main() {
    int edges, u, v;
    printf("Enter number of vertices and edges: ");
    scanf("%d %d", &n, &edges);
    for (int i = 0; i < edges; i++) {
        scanf("%d %d", &u, &v);
        adj[u][v] = 1;
    }
}
```

```

adj[u][v] = 1;
}

printf("Topological Order: ");

topologicalSort();

return 0;
}

```

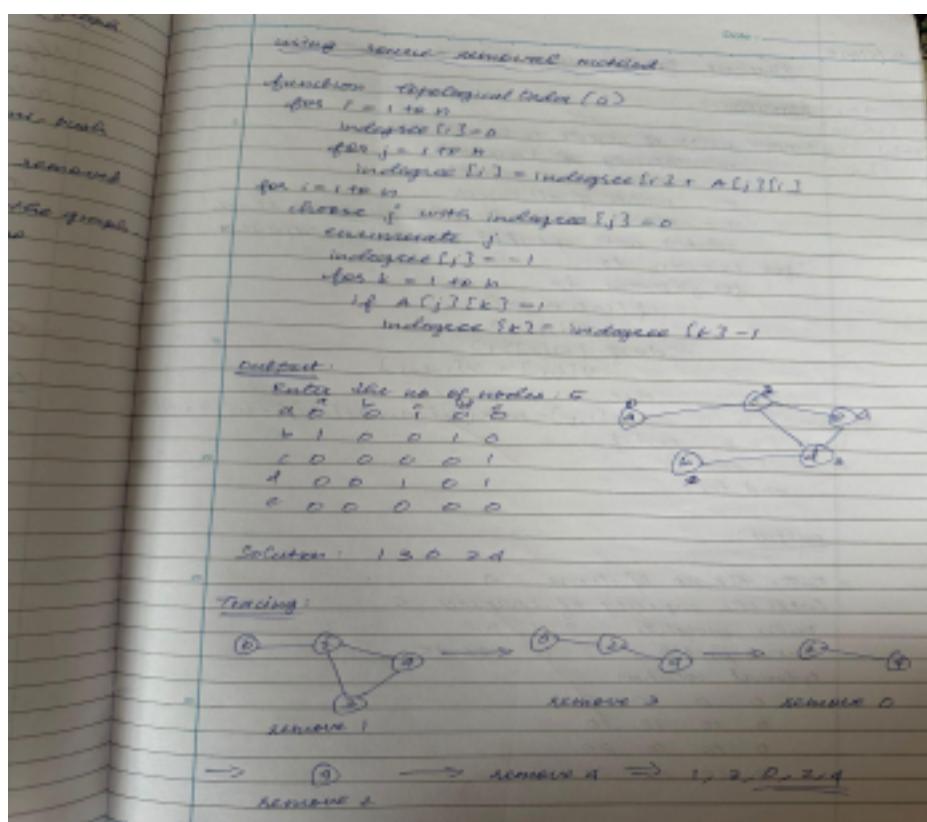
Result:

```

Enter number of vertices and edges: 6 7
0 1
0 2
2 1
2 3
3 4
3 5
4 5
Topological Order: 0 2 3 4 5 1

```

Algorithm and Tracing Screenshot:



Code:

```
typedef struct Node {  
    int course;  
    struct Node *next;  
} Node;  
  
void addEdge(Node **graph, int src, int dest) {  
    Node *newNode = (Node *)malloc(sizeof(Node));  
    newNode->course = dest;  
    newNode->next = graph[src];  
    graph[src] = newNode;  
}  
bool canFinish(int numCourses, int** prerequisites, int prerequisitesSize,  
int* prerequisitesColSize) {  
  
    Node **graph = (Node **)calloc(numCourses, sizeof(Node *));  
    int *indegree = (int *)calloc(numCourses, sizeof(int));  
  
    for (int i = 0; i < prerequisitesSize; i++) {  
  
        int course = prerequisites[i][0];  
        int pre = prerequisites[i][1];  
        addEdge(graph, pre, course);  
        indegree[course]++;  
    }  
    int *queue = (int *)malloc(numCourses * sizeof(int));  
    int front = 0, rear = 0;  
  
    for (int i = 0; i < numCourses; i++) {  
        if (indegree[i] == 0) {  
            queue[rear++] = i;  
        }  
    }  
  
    int count = 0;  
    while (front < rear) {  
  
        int current = queue[front++];  
        count++;  
    }  
}
```

```

Node *temp = graph[current];
while (temp != NULL) {
    indegree[temp->course]--;
    if (indegree[temp->course] == 0) {
        queue[rear++] = temp->course;
    }
    temp = temp->next;
}
for (int i = 0; i < numCourses; i++) {
    Node *temp = graph[i];
    while (temp != NULL) {
        Node *next = temp->next;
        free(temp);
        temp = next;
    }
    free(graph);
    free(indegree);
    free(queue);
}

return count == numCourses;
}

```

Result:

```
Testcase | Test Result
Accepted Runtime: 0 ms
Case 1 Case 2
Input
numCourses =
2

prerequisites =
[[1,0]]
Output
true
Expected
true
```

Lab program 2 :

Implement Johnson Trotter algorithm to generate permutations. Code:

```
#include <stdio.h>

#include <stdlib.h>

void swap(int* a, int* b) {

int temp = *a;

*a = *b;

*b = temp;

}

void generatePermutations(int arr[], int start, int end) {

if (start == end) {

for (int i = 0; i <= end; i++) {

printf("%d ", arr[i]);

}

printf("\n");

} else {

for (int i = start; i <= end; i++) {

swap(&arr[start], &arr[i]);

generatePermutations(arr, start + 1, end);

}
```

```
swap(&arr[start], &arr[i]); // backtrack  
}  
}  
}  
  
int main() {  
    int n;  
  
    printf("Enter the number of elements: ");  
    scanf("%d", &n);  
  
    int* arr = (int*)malloc(n * sizeof(int));  
  
    printf("Enter the elements: "); for (int  
        i = 0; i < n; i++) {  
  
        scanf("%d", &arr[i]); }  
  
    generatePermutations(arr, 0, n - 1);  
  
    free(arr);  
  
    return 0;  
}
```

Result:

```
1 2 3 4
1 2 4 3
1 4 2 3
4 1 2 3
4 1 3 2
1 4 3 2
1 3 4 2
1 3 2 4
3 1 2 4
3 1 4 2
3 4 1 2
4 3 1 2
4 3 2 1
3 4 2 1
3 2 4 1
3 2 1 4
2 3 1 4
2 3 4 1
2 4 3 1
4 2 3 1
4 2 1 3
2 4 1 3
2 1 4 3
2 1 3 4
```

Lab program 3 :

Sort a given set of N integer elements using Merge Sort technique and compute its time taken. Run the program for different values of N and record the time taken to sort.

Code:

```
#include <stdio.h>
#include <stdlib.h> // for exit

#include <time.h> // for clock timing

void split(int[], int, int);

void combine(int[], int, int, int);

int main() {
    int a[15000], n, i, j, ch, temp;

    clock_t start, end;

    while (1) {

        printf("\n1: For manual entry of N value and array elements");

        printf("\n2: To display time taken for sorting number of elements N in the range 500 to 14500");
    }
}
```



```

temp = 38 / 600;

}

end = clock();

printf("\nTime taken to sort %d numbers is %f Secs", n, ((double)(end - start)) /
CLOCKS_PER_SEC);

n = n + 1000;

}

break;

case 3:

exit(0);
}

} return 0;

}

```

```

// Recursive function to divide the
array void split(int a[], int low, int
high) {

int mid;

if (low < high) {

mid = (low + high) / 2;

split(a, low, mid);

split(a, mid + 1, high);

combine(a, low, mid, high);

}

}

// Function to merge two sorted halves void

combine(int a[], int low, int mid, int high) { int
c[15000], i, j, k;

i = k = low;

j = mid + 1;

```

```
while (i <= mid && j <= high) {
```

```
    if (a[i] < a[j]) {
```

```
        c[k++] = a[i++];
```

```
    } else {
```

```
        c[k++] = a[j++];
```

```
}
```

```
}
```

```
    while (i <= mid) {
```

```
        c[k++] = a[i++];
```

```
}
```

```
    while (j <= high) {
```

```
        c[k++] = a[j++];
```

```
}
```

```
    for (i = low; i <= high; i++) {
```

```
        a[i] = c[i];
```

```
}
```

Result:

```
1: For manual entry of N value and array elements
2: To display time taken for sorting number of elements N in the range 500
   to 14500
3: To exit
Enter your choice: 2
```

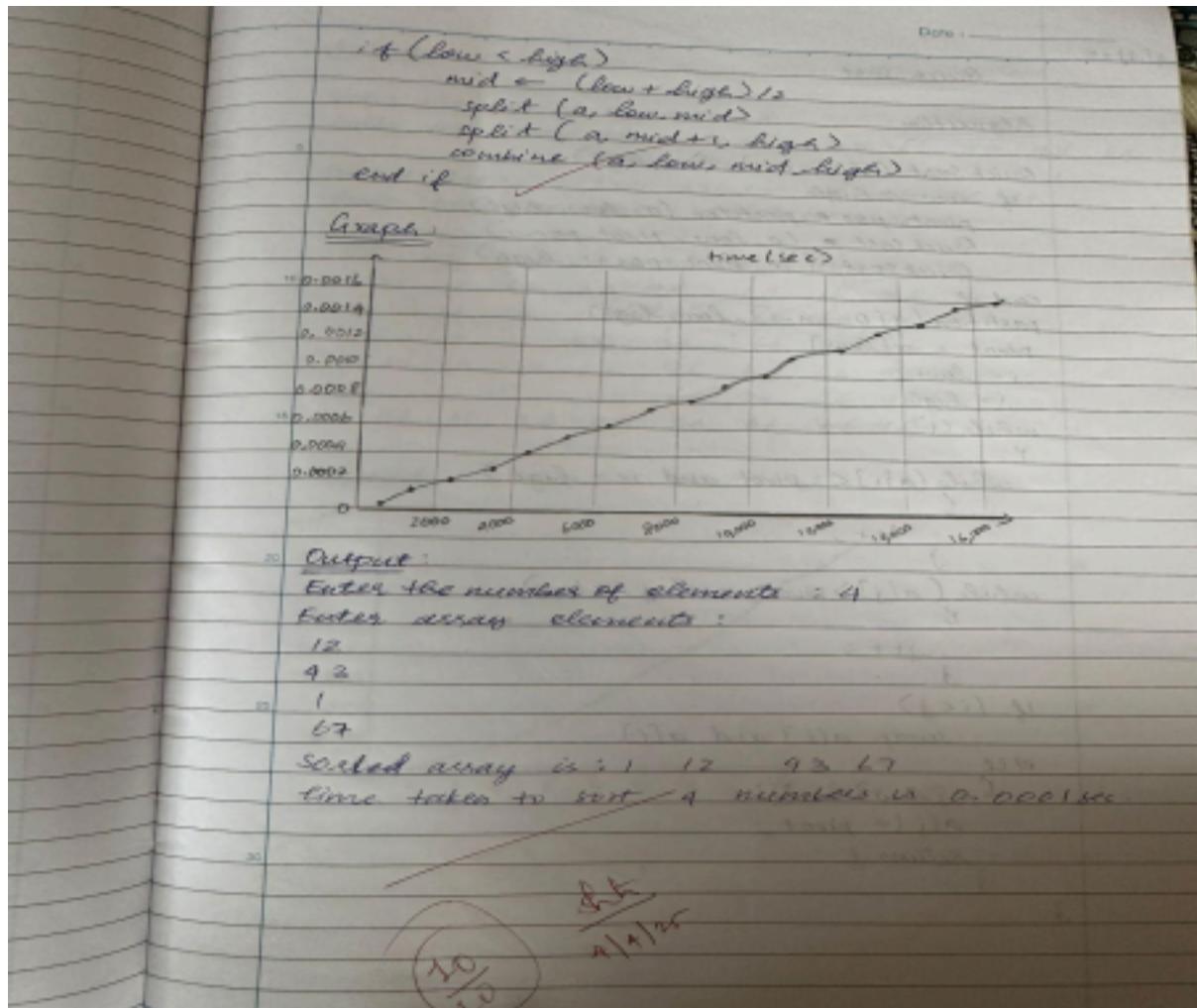
```
Time taken to sort 500 numbers is 0.000524 Secs
Time taken to sort 1500 numbers is 0.000593 Secs
Time taken to sort 2500 numbers is 0.000587 Secs
Time taken to sort 3500 numbers is 0.000526 Secs
Time taken to sort 4500 numbers is 0.000597 Secs
Time taken to sort 5500 numbers is 0.000642 Secs
Time taken to sort 6500 numbers is 0.000698 Secs
Time taken to sort 7500 numbers is 0.000743 Secs
Time taken to sort 8500 numbers is 0.000821 Secs
Time taken to sort 9500 numbers is 0.000863 Secs
Time taken to sort 10500 numbers is 0.000918 Secs
Time taken to sort 11500 numbers is 0.000992 Secs
Time taken to sort 12500 numbers is 0.001044 Secs
Time taken to sort 13500 numbers is 0.001105 Secs
Time taken to sort 14500 numbers is 0.001276 Secs
```

Algorithm and Tracing :

21/3/25 Merge sort

Algorithm:

```
combine (a[low...mid], a[mid+1...high])
    i = low
    j = mid + 1
    k = low
    while (i <= mid) and (j <= high) do
        if a[i] <= a[j]
            c[k] = a[i]
            k = k + 1
            i = i + 1
        else
            c[k] = a[j]
            k = k + 1
            j = j + 1
        end if
        end while
        if j > high
            while i <= mid do
                c[k] = a[i]
                k = k + 1
                i = i + 1
            end while
        end if
        if i > high
            while j <= high do
                c[k] = a[j]
                k = k + 1
                j = j + 1
            end while
        end if
        for k = low to high do
            a[i] = c[i]
        end for
```



Lab program 4 :

Sort a given set of N integer elements using Quick Sort technique and compute its time taken.

Code:

```

#include <stdio.h>
#include <stdlib.h>
#include <time.h>

// Function to swap two elements
void swap(int *a, int *b) {
  int temp = *a;
  *a = *b;
  *b = temp;
}

// Partition function for Quick Sort
int partition(int arr[], int low, int high) {
  int pivot = arr[high]; // pivot element
  int i = (low - 1); // index of smaller element
  
```

```

for (int j = low; j < high; j++) {
    if (arr[j] <= pivot) {
        i++;
        swap(&arr[i], &arr[j]);
    }
}

swap(&arr[i + 1], &arr[high]);
return (i + 1);
}

void quickSort(int arr[], int low, int high) {
    if (low < high) {
        int pi = partition(arr, low, high); // partitioning index
        quickSort(arr, low, pi - 1); // Recursively sort left subarray
        quickSort(arr, pi + 1, high); // Recursively sort right subarray
    }
}

} // Main function

int main() {
    int n; // Input the size of the array
    printf("Enter number of elements: ");
    scanf("%d", &n);
    int arr[n];

    // Seed the random number generator
    srand(time(0));

    // Generate random numbers for the array
    printf("Generated array: ");
    for (int i = 0; i < n; i++) {
        arr[i] = rand() % 1000; // Generate random numbers between 0 and 999
        printf("%d ", arr[i]);
    }

    printf("\n"); // Measure time taken for sorting
    clock_t start = clock();
    quickSort(arr, 0, n - 1);
}

```

```

clock_t end = clock();

double time_taken = ((double)(end - start)) / CLOCKS_PER_SEC;

// Output the sorted array
printf("Sorted array: ");
for (int i = 0; i < n; i++) {
    printf("%d ", arr[i]);
}
printf("\n");

// Output the time taken
printf("Time taken to sort: %f seconds\n", time_taken);

return 0;
}

```

Result:

```

Enter number of elements: 50
Generated array: 884 882 720 913 672 874 888 214 358 271 901 763 182 97 744 312 557 988 355 545 148 584 793 990 682 632
129 496 73 945 900 113 561 772 828 220 358 341 128 869 789 244 285 265 472 188 312 985 590 978
Sorted array: 73 97 113 128 129 140 180 182 205 214 220 244 265 271 312 312 341 355 358 358 472 496 584 545 551 557 590
632 672 682 720 744 763 772 789 793 800 802 884 828 869 874 900 901 905 988 913 945 978 990

```

Algorithm and Tracing :

Quick Sort

Algorithm:

```

Quick Sort (a[0...n-1], low, high)
if low < high
    pivot = partition (a, low, high)
    RecurSort (a, low, pivot-1)
    QuickSort (a, pivot+1, high)
end if
partition (a[0...n-1], low, high)
pivot = a[low]
i = low+1
j = high
while (i < j)
    while (a[i] <= pivot and i <= high)
        i++
    j++
    while (a[j] >= pivot and j >= low)
        j--
    if (i < j)
        swap a[i] and a[j]
    else
        a[low] = a[j]
        a[j] = pivot
    return
}

```

Output:

Enter the no. of elements : 8
 Enter 8 no. array elements : 12 45 66 23 98 64
 16 76
 Sorted Array : 12 16 23 45 64 66 76 98
 Time taken to sort 0.00001 seconds.

12	45	66	23	16	64	76	98
last	12	66	23	45	64	16	76
12	16	23	45	64	66	76	98
12	16	23	45	48	64	76	98
12	16	23	48	64	76	66	98
12	16	23	48	64	76	66	98
12	16	23	48	64	76	66	98
12	16	23	48	64	66	76	98

Graph:

LEETCODE: 3Sum

Code:

```
var threeSum = function (nums) {
```

```

nums.sort((a, b) => a - b);

const op = [];

for (let i = 0; i < nums.length; i++) {
    if (i > 0 && nums[i] === nums[i - 1]) continue;

    const target = -nums[i];

    let left = i + 1, right = nums.length - 1;

    while (left < right) {

        const current_sum = nums[left] + nums[right];

        if (current_sum === target) {
            op.push([nums[i], nums[left], nums[right]]);

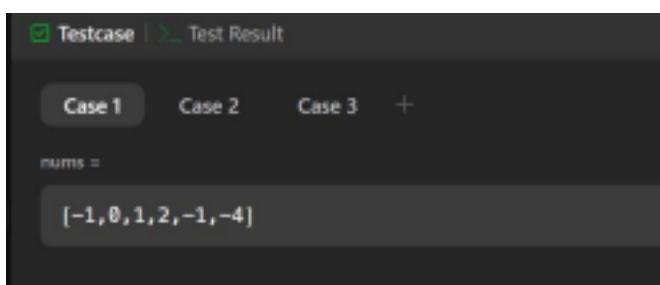
            while (left < right && nums[left] === nums[left + 1]) left++;
            while (left < right && nums[right] === nums[right - 1]) right--;

            left++;
            right--;
        } else if (current_sum < target) {
            left++;
        } else {
            right--;
        }
    }
}

return op;
};

```

Result:



Lab program 5 :

Sort a given set of N integer elements using Heap Sort technique and compute its time taken.

Code:

```
#include <stdio.h>
#include <time.h>
#define MAX 1000
int a[MAX];
int n;
void heapify(int a[], int n, int i) {
    int largest = i;
    int left = 2 * i + 1;
    int right = 2 * i + 2;
    if (left < n && a[left] > a[largest])
        largest = left;
    if (right < n && a[right] > a[largest])
        largest = right;
    if (largest != i) {
        int temp = a[i];
        a[i] = a[largest];
        a[largest] = temp;
        heapify(a, n, largest);
    }
}
```

```
void heapSort(int a[], int n) {
    // Build max heap
    for (int i = n / 2 - 1; i >= 0; i--)
        heapify(a, n, i);
    for (int i = n - 1; i >= 1; i--) {
        int temp = a[0];
        a[0] = a[i];
        a[i] = temp;
        heapify(a, n, 0);
    }
}
```

```

a[i] = temp;

heapify(a, i, 0);
}

}

int main() {
    clock_t start, end;
    double time_taken;
    printf("Enter number of elements: ");
    scanf("%d", &n);

    if (n > MAX) {
        printf("Error: Maximum number of elements is %d.\n",
               MAX); return 1;
    }

    printf("Enter %d elements:\n", n);
    for (int i = 0; i < n; i++)
        scanf("%d", &a[i]);
    start = clock();
    heapSort(a, n);
    end = clock();

    time_taken = ((double)(end - start)) / CLOCKS_PER_SEC;
    printf("Sorted array:\n");
    for (int i = 0; i < n; i++)
        printf("%d ", a[i]);
    printf("\n");
    printf("Time taken to sort using Heap Sort: %f seconds\n", time_taken); return 0;
}

```

Result:

```
Enter number of elements: 6
```

```
Enter 6 elements:
```

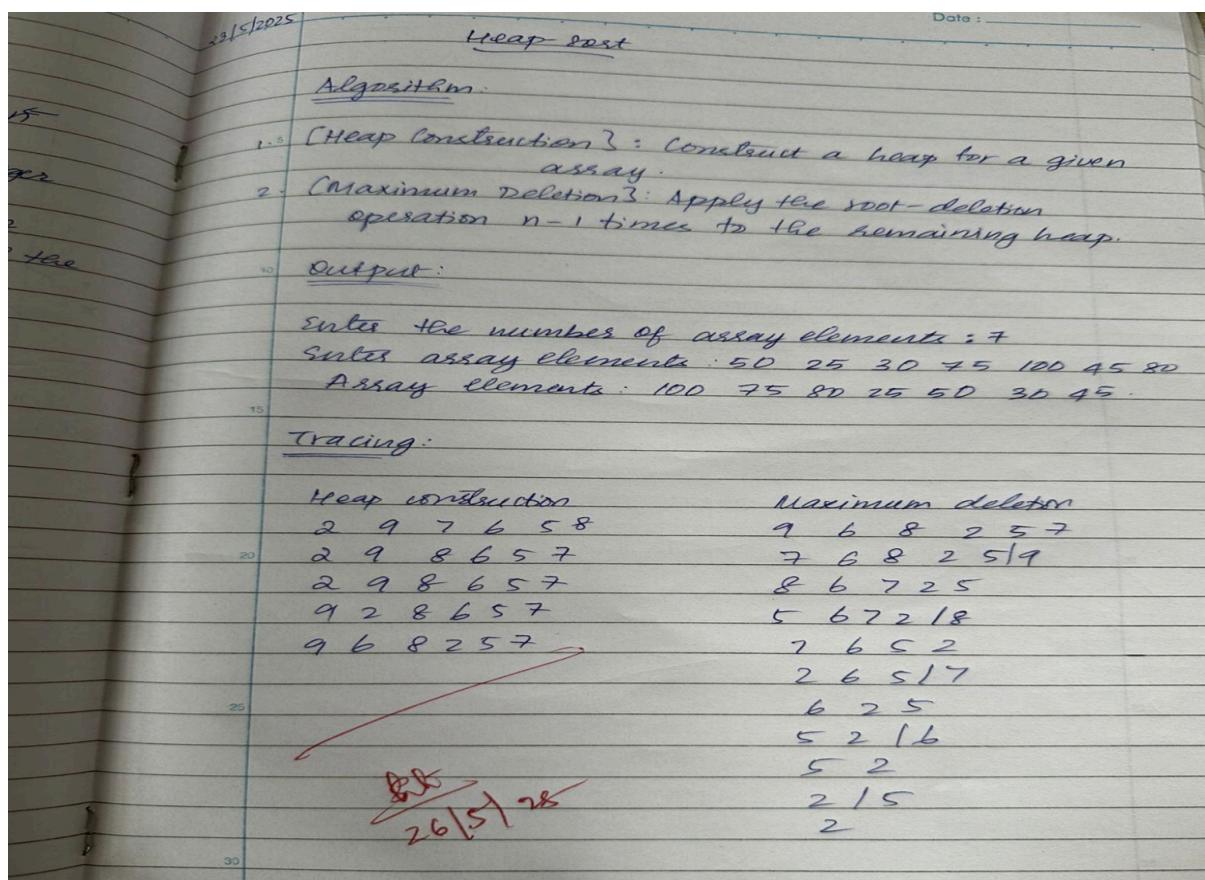
```
5 12 45 23 31 10
```

```
Sorted array:
```

```
5 10 12 23 31 45
```

```
Time taken to sort using Heap Sort: 0.000002 seconds
```

Algorithm and Tracing :



Lab program 6 :

Implement 0/1 Knapsack problem using dynamic programming. Code:

```
#include <stdio.h>

int n, m, w[10], p[10], v[11][11];

void knapsack(int, int, int[], int[]);
```

```
int max(int, int);

int main() {
    int i, j;

    printf("Enter the number of items: ");
    scanf("%d", &n);

    printf("Enter the capacity of the knapsack: ");
    scanf("%d", &m);

    printf("Enter weights:\n");
    for (i = 1; i <= n; i++) {
        scanf("%d", &w[i]);
    }

    printf("Enter profits:\n");
    for (i = 1; i <= n; i++) {
        scanf("%d", &p[i]);
    }

    knapsack(n, m, w, p);

    printf("\nDP Table:\n");
    for (i = 0; i <= n; i++) {
        for (j = 0; j <= m; j++) {
            printf("%3d ", v[i][j]);
        }
        printf("\n");
    }

    printf("\nOptimal Profit: %d\n", v[n][m]);

    return 0;
}

void knapsack(int n, int m, int w[], int p[])
{
    int i, j;

    for (i = 0; i <= n; i++) {
```

```

for (j = 0; j <= m; j++) {
    if (i == 0 || j == 0) {
        v[i][j] = 0;
    } else if (w[i] > j) {
        v[i][j] = v[i - 1][j];
    } else {
        v[i][j] = max(v[i - 1][j], v[i - 1][j - w[i]] + p[i]);
    }
}

int max(int a, int b) {
    return (a > b) ? a : b;
}

```

Result:

```

Enter the number of items: 4
Enter the capacity of the knapsack: 5
Enter weights:
2 1 3 2
Enter profits:
12 10 20 15

DP Table:
 0   0   0   0   0   0
 0   0   12  12  12  12
 0   10  12  22  22  22
 0   10  12  22  30  32
 0   10  15  25  30  37

Optimal Profit: 37

```

Algorithm and Tracing:

Date : _____

Knapsack Problem using dynamic programming

Algorithm:

Input: n - No. of objects to be selected
 m - capacity of knapsack
 w - weight of all objects
 p - profit of all objects
 v - optimal solution for the number of objects selected with specified remaining capacity.

```

for i=0->n do
    for j=0->m do
        if (i=0 or j=0)
            v[i,j]=0
        else if (w[i]>j)
            v[i,j] = v[i-1,j]
        else
            v[i,j] = max (v[i-1,j], v[i-1,j-w[i]] + p[i])
        end if
    end for
end for.

```

Output:

= Enter the no. of items : 4
Enter the capacity of knapsack : 5
Enter weights : 2 1 3 2
Enter profits : 12 10 20 15
Optimal solution :

0	0	0	0
0	10	10	10
0	10	10	20
0	10	15	25

Date : _____

Tracing:

Item	weight	profit
1	2	12
2	1	10
3	3	20
4	2	15

$$v[i,j] = \begin{cases} 0 & (i=j=0) \\ v[i-1,j] & (w[i] > j) \\ \max(v[i-1,j], v[i-1,j-w[i]] + p[i]) & (w[i] \leq j) \end{cases}$$

calc

$M=5$

	0	1	2	3	4	5
0	0	0	0	0	0	0
1	0	0	12	12	12	12
2	0	10	12	22	22	22
3	0	10	12	22	30	32
4	0	10	15	25	30	37

df

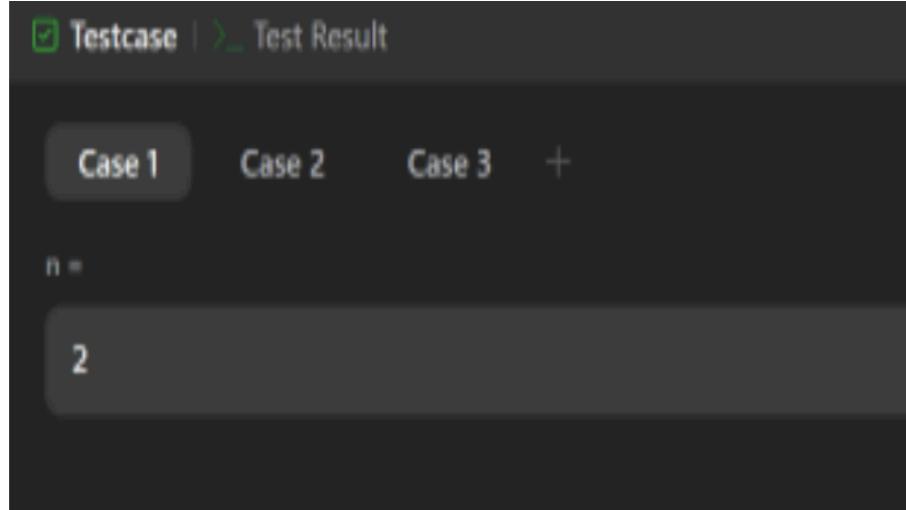
$3 + p[3]$
the optimal solution is 37 which is achieved by selected item 2 & 3 with weights (1+3) and profit 10+20.

LEETCODE: Fibonacci Number

Code:

```
int fib(int n) {  
    if (n == 0) return 0;  
    if (n == 1) return 1;  
  
    int a = 0, b = 1, c;  
  
    // Calculate Fibonacci iteratively  
    for (int i = 2; i <= n; i++) {  
        c = a + b; // Fibonacci relation  
        a = b; // Update a to previous b  
        b = c; // Update b to current Fibonacci number  
    }  
    return b; // Return the nth Fibonacci number  
}
```

Result:



Lab program 7 :

Implement All Pair Shortest paths problem using Floyd's algorithm. Code:

```
#include <stdio.h>  
  
int a[10][10],D[10][10],n;
```

```
void floyd(int [][]a,int n);
int min(int,int);
int main()
{
printf("Enter the no. of vertices:");
scanf("%d",&n);
printf("Enter the cost adjacency matrix:\n");
int i,j;
for(i=0;i<n;i++){
    for(j=0;j<n;j++){
        scanf("%d",&a[i][j]);
    }
}
floyd(a,n);
printf("Distance Matrix:\n");
for(i=0;i<n;i++){
    for(j=0;j<n;j++){
        printf("%d ",D[i][j]);
    }
    printf("\n");
}
return 0;
}

void floyd(int a[][] ,int n){
int i,j,k;
for(i=0;i<n;i++){
    for(j=0;j<n;j++){
        D[i][j]=a[i][j];
    }
}
```

```
}

for(k=0;k<n;k++){

for(i=0;i<n;i++){

for(j=0;j<n;j++){

D[i][j]=min(D[i][j],(D[i][k]+D[k][j]));

} } } }
```

```
int min(int a,int b){

if(a<b){

return a;

}else{

return b;

}}
```

Result:

```
Enter the no. of vertices:4
Enter the cost adjacency matrix:
0 99 3 99
2 0 99 99
99 7 0 1
6 99 99 0
Distance Matrix:
0 10 3 4
2 0 5 6
7 7 0 1
6 16 9 0
```

Algorithm and Tracing :

16/5/2025

Floyd's Algorithm.

Input : The weight matrix W of a graph with no negative-length cycle.

Output : The distance matrix of the shortest path's length.

```
D ← W
for i → 1 to n do
    for j → 1 to n do
        for k → 1 to n do
            D[i][j] → min[D[i][j], D[i][k] + D[k][j]]
```

return D.

Output:

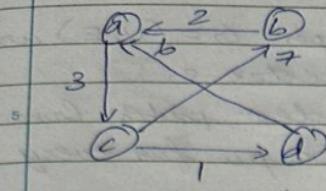
Enter the no. of vertices: 4

Enter the cost of adjacency matrix:

0	99	3	99
2	0	99	99
99	6	0	1
7	99	99	0

Distance Matrix

0	9	3	9
2	0	5	6
8	6	0	1
7	16	10	0

Tracing:

$$D(0) = \begin{bmatrix} a & b & c & d \\ a & 0 & \infty & 3 & \infty \\ b & 2 & 0 & \infty & \infty \\ c & \infty & 4 & 0 & 1 \\ d & 6 & \infty & \infty & 0 \end{bmatrix}$$

$$D(1) = \begin{bmatrix} 0 & \infty & 3 & \infty \\ 2 & 0 & 5 & \infty \\ \infty & 7 & 0 & 1 \\ 6 & \infty & 9 & 0 \end{bmatrix}$$

$$D(2) = \begin{bmatrix} 0 & \infty & 3 & \infty \\ 2 & 0 & 5 & \infty \\ 9 & 7 & 0 & 1 \\ 6 & \infty & 9 & 0 \end{bmatrix}$$

$$D(3) = \begin{bmatrix} 0 & 10 & 3 & 4 \\ 2 & 0 & 5 & 6 \\ 9 & 7 & 0 & 1 \\ 6 & 16 & 9 & 0 \end{bmatrix}$$

~~$$D(4) = \begin{bmatrix} 0 & 10 & 3 & 4 \\ 2 & 0 & 5 & 6 \\ 7 & 7 & 0 & 1 \\ 6 & 16 & 9 & 0 \end{bmatrix}$$~~

LEETCODE: Shortest Path Visiting All Nodes

Code:

```
#include <stdio.h>
```

```
#include <stdlib.h>
```

```
#include <string.h>
```

```
#include <stdbool.h>
```

```
#define MAXN 12
```

```
#define MAXQ (1 << MAXN) * MAXN
```

```
typedef struct {
```

```

int node;
int mask;
int dist;
} State;

int shortestPathLength(int** graph, int graphSize, int* graphColSize)
{ int allVisited = (1 << graphSize) - 1;

bool visited[MAXN][1 << MAXN] = { false };
State queue[MAXQ];
int front = 0, rear = 0;

// Initialize queue with each node as starting point
for (int i = 0; i < graphSize; i++) {
    int mask = 1 << i;
    queue[rear++] = (State){i, mask, 0};
    visited[i][mask] = true;
}

while (front < rear) {
    State curr = queue[front++];
    if (curr.mask == allVisited) {
        return curr.dist;
    }

    for (int i = 0; i < graphColSize[curr.node]; i++) {
        int neighbor = graph[curr.node][i];
        int nextMask = curr.mask | (1 << neighbor);

        if (!visited[neighbor][nextMask]) {
            visited[neighbor][nextMask] = true;
            queue[rear++] = (State){neighbor, nextMask, curr.dist +
1}; }
    }
}

```

```
    return -1; // Should never reach here  
}
```

Result

The screenshot shows a test result interface with the following details:

- Accepted** Runtime: 0 ms
- Case 1** (selected):
 - Input**: graph = [[1, 2, 3], [0], [0], [0]]
 - Output**: 4
 - Expected**: 4
- Case 2**:
 - Input**: graph = [[1, 2, 3], [0], [0], [0]]
 - Output**: 4
 - Expected**: 4

Lab program 8 :

Find Minimum Cost Spanning Tree of a given undirected graph using Prim's algorithm. Code:

```
#include <stdio.h>  
  
#define INF 999  
  
int main() {  
    int n, i, j, min, u, v;  
  
    int cost[10][10], visited[10], parent[10], dist[10];  
  
    int totalCost = 0;  
  
    printf("Enter number of vertices: ");  
  
    scanf("%d", &n);  
  
    printf("Enter cost adjacency matrix (use 999 for no edge):\n");  
    for (i = 0; i < n; i++)  
        for (j = 0; j < n; j++)
```

```

scanf("%d", &cost[i][j]);

// Initialize

for (i = 0; i < n; i++) {

    dist[i] = cost[0][i];

    parent[i] = 0;

    visited[i] = 0;

}

visited[0] = 1; // Start from vertex 0

for (i = 1; i < n; i++) {

    min = INF;

    u = -1;

    // Find the unvisited vertex with the smallest edge weight

    for (j = 0; j < n; j++) {

        if (!visited[j] && dist[j] < min) {

            min = dist[j];

            u = j;

        }

    }

    if (u == -1) break; // Graph is disconnected

    visited[u] = 1;

    totalCost += dist[u];

    printf("Edge selected: (%d, %d) cost = %d\n", parent[u], u, dist[u]); //

    Update distance of adjacent vertices

    for (v = 0; v < n; v++) {

        if (!visited[v] && cost[u][v] < dist[v]) {

            dist[v] = cost[u][v];

            parent[v] = u;

        }

    }

}

```

```
}

printf("Total cost of Minimum Spanning Tree: %d\n", totalCost);

return 0;

}
```

Result:

```
Enter number of vertices: 4
Enter cost adjacency matrix (use 999 for no edge):
0 2 999 6
2 0 3 8
999 3 0 1
6 8 1 0
Edge selected: (0, 1) cost = 2
Edge selected: (1, 2) cost = 3
Edge selected: (2, 3) cost = 1
Total cost of Minimum Spanning Tree: 6
```

Algorithm and Tracing :

41A125:

Prim's Algorithm:

$V_T \leftarrow \{v_0\}$

$E_T \leftarrow \emptyset$

for $i \rightarrow 1$ to $|V| - 1$ do

 find a minimum-weight edge $e^* = (v^*, u^*)$
 among all the edges (v, u) such that v is in
 V_T and u is in $V - V_T$

$V_T \leftarrow V_T \cup v^*$

$E_T \leftarrow E_T \cup \{e^*\}$

return E_T .

Output:

Enter the number of vertices : 4

Enter the cost adjacency matrix

0 1 5 2

1 0 99 99

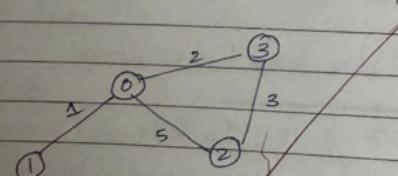
5 99 0 3

2 99 3 0

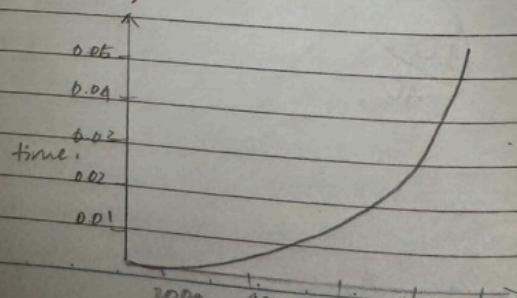
Edges of the minimal spanning

(1,0) (3,0) (2,3)

sum of minimal spanning tree : 6



Graph:



B. Find Minimum Cost Spanning Tree of a given undirected graph using Kruskal's algorithm.

Code:

```
#include <stdio.h>
```

```
#define INF 999
```

```
int cost[10][10], parent[10];
```

```
int n; // Number of vertices
```

```
// Function to find the root of a vertex (used in union-find)
```

```
int find(int i) {
```

```

while (parent[i] != i)
    i = parent[i];
    return i;
}

// Function to join two sets (union)

void unionSets(int i, int j) {
    int root_i = find(i);
    int root_j = find(j);
    parent[root_i] = root_j;
}

void kruskal() {
    int edges = 0, totalCost = 0;

    // Initialize each vertex's parent to itself
    for (int i = 0; i < n; i++)
        parent[i] = i;

    printf("Edges in the Minimum Spanning Tree:\n");

    while (edges < n - 1) {
        int min = INF, u = -1, v = -1;

        // Find the edge with the minimum cost
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                if (i != j && cost[i][j] < min && find(i) != find(j)) {
                    min = cost[i][j];
                    u = i;
                    v = j;
                }
            }
        }

        if (u != -1 && v != -1) {
            unionSets(u, v);
            printf("(%.d, %.d) -> cost = %.d\n", u, v, min);
            totalCost += min;
            edges++;
        }
    }
}

```

```

// Mark edge as used
cost[u][v] = cost[v][u] = INF;

} else {

break; // No valid edge found

}

printf("Total cost of the Minimum Spanning Tree: %d\n", totalCost);

}

int main() {

printf("Enter the number of vertices: ");

scanf("%d", &n);

printf("Enter the cost adjacency matrix (999 for no edge):\n");

for (int i = 0; i < n; i++)

for (int j = 0; j < n; j++)

scanf("%d", &cost[i][j]);

kruskal();

return 0;
}

```

Result:

Date : _____

Kruskall's Algorithm:

Algorithm:

Input : A weighted connected graph
 Output : E_T , the set of edges composing a minimum spanning tree of G .

```

    5       $E_T \leftarrow \emptyset$ 
    6       $k \leftarrow 0$ 
    7       $\text{encounters} \leftarrow 0$ 
    8      while  $\text{counters} < |V| - 1$  do
    9           $k \rightarrow k + 1$ 
    10         if  $E_T \cup \{e_k\}$  is acyclic
    11              $E_T \leftarrow E_T \cup \{e_k\}$ 
    12              $\text{encounters}++$ 
    13     return  $E_T$ .
  
```

Output:

Enter no. of vertices & edges : 4 5
 Enter edges (u, v, weight)

20	0	1	10
	0	2	6
	0	3	5
	1	3	15
	2	3	9

edges in MST

$$2 - 3 = 4$$

$$0 - 3 = 5$$

$$0 - 1 = 10$$

$MST = 19$

Graph:

A graph with 4 vertices labeled 0, 1, 2, 3. Vertex 0 is at the top left, 1 is at the top right, 2 is at the bottom right, and 3 is at the bottom left. There are edges between (0,1) with weight 10, (0,2) with weight 6, (0,3) with weight 5, (1,3) with weight 15, (2,3) with weight 9, and (1,2) which is explicitly drawn as a curved edge.

A graph showing time vs. iterations. The x-axis ranges from 0 to 10,000 with major ticks at 2000, 4000, 6000, and 8000. The y-axis ranges from 0.01 to 0.06 with major ticks at 0.01, 0.02, 0.03, 0.04, 0.05, and 0.06. The curve starts near (0, 0.01) and increases rapidly, showing an exponential growth pattern.

Lab program 9 :

Implement Fractional Knapsack using Greedy

technique. Code:

```
#include <stdio.h>

void knapsack(int n, int p[], int w[], int W) {
    int used[n];
    for (int i = 0; i < n; ++i)
        used[i] = 0;
    float total_weight = 0;
    float total_value = 0;
    for (int i = 0; i < n; ++i) {
        if (used[i] == 1)
            continue;
        if (total_weight + w[i] >= W) {
            used[i] = 1;
            total_weight += w[i];
            total_value += p[i];
            break;
        }
        float fraction = (W - total_weight) / (float)w[i];
        used[i] = 1;
        total_weight += fraction * w[i];
        total_value += fraction * p[i];
    }
    printf("Total Value: %f\n", total_value);
}
```

```

used[i] = 0;

int cur_w = W;

float tot_v = 0.0;

int i, maxi;

while (cur_w > 0) {

maxi = -1;

for (i = 0; i < n; ++i) {

if ((used[i] == 0) &&

((maxi == -1) || ((float)p[i] / w[i] > (float)p[maxi] / w[maxi])))

maxi = i;

}

used[maxi] = 1;

if (w[maxi] <= cur_w) {

cur_w -= w[maxi];

tot_v += p[maxi];

printf("Added object %d (%d, %d) completely in the bag. Space left: %d.\n",
maxi + 1, w[maxi], p[maxi], cur_w);

} else {

int taken = cur_w;

cur_w = 0;

tot_v += ((float)taken / w[maxi]) * p[maxi];

printf("Added %d%% (%d, %d) of object %d in the bag.\n",
(int)((float)taken / w[maxi] * 100), w[maxi], p[maxi], maxi + 1); }

}

printf("Filled the bag with objects worth %.2f.\n", tot_v);

}

int main() {
int n, W;

printf("Enter the number of objects: ");

```

```
scanf("%d", &n);

int p[n], w[n];

printf("Enter the profits of the objects: ");

for (int i = 0; i < n; i++) {

scanf("%d", &p[i]);

}

printf("Enter the weights of the objects: ");

for (int i = 0; i < n; i++) {

scanf("%d", &w[i]);

}

printf("Enter the maximum weight of the bag: ");

scanf("%d", &W);

knapsack(n, p, w, W);

return 0;

}
```

Result:

Date : _____

Fractional Knapsack using Greedy Technique

17 23/5/2025

Algorithm:

- * consider all the items with their weights and profits mentioned.
- * calculate P_i/w_i of all the items & sort the items in descending order based on their P_i/w_i values.
- * without exceeding the limit, add the items into the knapsack.
- * If the knapsack can still store some weight, but the weights of other items exceed the limit, the fractional part of the next item can be added.

15 Output:

Enter the no. of objects : 7

Enter the profit of the objects :

5 10 15 7 8 9 4

20 Enter the weight of the objects :

1 3 5 4 1 3 2

Enter the maximum weight of the bag : 15

25 Added 6(4,7) in bag. space left : 11

Added 7(2,4) in bag. space left : 9

Added 3(5,15) in bag. space left : 9

Added 6(3,9) in bag. space left : 4

Added 3(3,7) (3,10) of object 2.

30 Filled the bag with object worth 36.00

Date : _____

Tracing

Item	1	2	3	4	5
weight	3	3	2	5	1
profit	10	15	10	20	8
P_i/w_i	3.3	5	5	4	8

5 weight = $(1 * 1) + (1 * 3) + (1 * 2) + (4/5 * 5) \}$
 $= 10$

10 Max. profit = $[(1 * 8) + (1 * 15) + (1 * 10) + (4/5 * 20) \} = 37$.

Ans

LEETCODE: Largest Odd Number in String

Code:

```
char* largestOddNumber(char* num) {  
    int len = strlen(num);  
  
    // Traverse from the end to find the rightmost odd digit  
    for (int i = len - 1; i >= 0; i--) {  
        if ((num[i] - '0') % 2 == 1) {  
            // Temporarily terminate the string at the right place  
            num[i + 1] = '\0';  
            return num;  
        }  
    }  
    return ""; // No odd digit found  
}
```

Lab program 10 :

From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm.

Code:

```
#include <stdio.h>  
  
#define MAX 10  
  
#define INF 999  
  
int cost[MAX][MAX], n, result[MAX][2], weight[MAX];  
  
void dijkstras(int cost[][MAX], int s);  
  
int main() {  
    int i, j, s;  
  
    printf("Enter the number of vertices: ");  
    scanf("%d", &n);  
  
    if (n > MAX) {  
        printf("Maximum supported vertices is %d.\n", MAX);  
        return 1;  
    }
```

```

}

printf("Enter the cost adjacency matrix (use 999 for no edge):\n");
for (i = 0; i < n; i++)
for (j = 0; j < n; j++)
scanf("%d", &cost[i][j]);
printf("Enter the source vertex: ");
scanf("%d", &s);
dijkstras(cost, s);

printf("\nShortest paths from source vertex %d:\n", s);
for (i = 0; i < n; i++) {
if (i != s)
printf("(%d -> %d) with weight %d\n", result[i][0], result[i][1], weight[i]);
}
return 0;
}

void dijkstras(int cost[][MAX], int s) {
int d[MAX], visited[MAX], p[MAX];
int i, j, u, v, min;
for (i = 0; i < n; i++) {
d[i] = INF;
visited[i] = 0;
p[i] = s;
}
d[s] = 0;
for (i = 0; i < n - 1; i++) {
min = INF;
u = -1;
// Find unvisited vertex with smallest distance for
(j = 0; j < n; j++) {

```

```

if (!visited[j] && d[j] < min) { min
= d[j];
u = j;
}

}

if (u == -1)
break;

visited[u] = 1;

// Update distances

for (v = 0; v < n; v++)
if (!visited[v] && cost[u][v] != INF && d[u] + cost[u][v] < d[v]) { d[v] = d[u] + cost[u][v];
p[v] = u;

}

}

}

}

// Store the result

for (i = 0; i < n; i++) {
result[i][0] = p[i];
result[i][1] = i;
weight[i] = d[i];

}

```

Result:

Output

```
Enter the number of vertices: 4
Enter the cost adjacency matrix:
0 1 5 2
1 0 99 99
5 99 0 3
2 99 3 0
Enter the source vertex: 0
Path:
(0, 1) with weight 1 (0, 2) with weight 5 (0, 3) with weight 2
==== Code Execution Successful ====
```

Algorithm and Tracing :

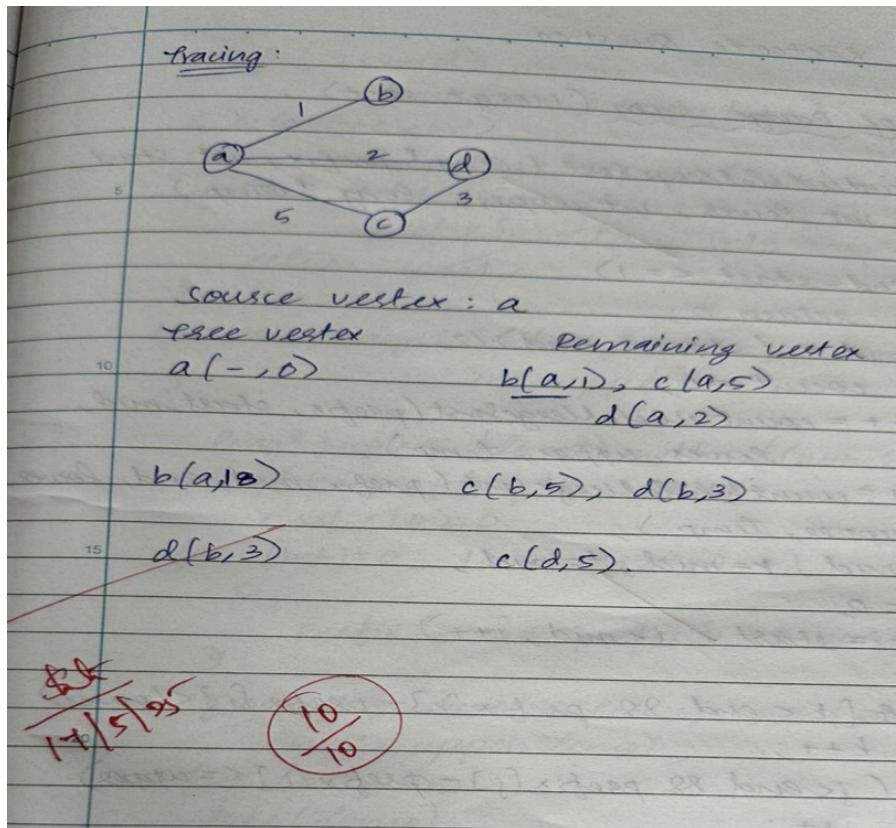
17/5/2025
Dijkstra's Algorithm:

Input : A weighted connected graph $G = (V, E)$ with non-negative weights and its vertex s .
Output : The length d_v of a shortest path from s to v and its predecessor vertex p_v for every vertex $v \in V$.

for every vertex $v \in V$
 $d_v \leftarrow \infty$; $p_v \leftarrow \text{null}$
 insert (Q, v, d_v)
 $d_s \leftarrow 0$; Decrease (Q, s, d_s)
 $V^* \leftarrow \emptyset$
 for $i \leftarrow 0$ to $|V| - 1$ do
 $u^* \leftarrow \text{DeleteMin}(Q)$
 $V^* \leftarrow V^* \cup u^*$
 for every vertex $v \in V - V^*$ that is adjacent to u^* do
 if $d_{u^*} + w(u^*, v) < d_v$
 $d_v \leftarrow d_{u^*} + w(u^*, v)$
 $p_v \leftarrow u^*$
 Decrease (Q, v, d_v)

Output:

Enter the no. of vertices: 4
Enter the cost adjacency matrix:
0 1 5 2
1 0 99 99
5 99 0 3
2 99 0 3
Enter the source vertex: 0
Path:
(0, 1) with weight 1, (0, 2) with weight 5, (0, 3) with weight 2



Lab program 11 :

Implement “N-Queens Problem” using

Backtracking. Code:

```
#include <stdio.h>
#include <stdlib.h>
#include <stdbool.h>

bool isSafe(int** board, int row, int col, int N)
{
    int i, j;

    // Check left side of the current row
    for (i = 0; i < col; i++)
        if (board[row][i])
            return false;

    // Check upper diagonal on left side
    for (i = row, j = col; i >= 0 && j >= 0; i--, j--)
        if (board[i][j])
            return false;

    // Check lower diagonal on left side
    for (i = row, j = col; j >= 0 && i < N; i++, j--)
        if (board[i][j])
            return false;

    return true;
}
```

```

return false;
return true;
}

void printBoard(int** board, int N) {
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++)
            printf("%s ", board[i][j] ? "Q" : ".");
        printf("\n");
    }
    printf("\n");
}

void solveNQueensAll(int** board, int col, int N, int* solutionCount)
{
    if (col == N) {
        (*solutionCount)++;
        printf("Solution %d:\n", *solutionCount);
        printBoard(board, N);
        return;
    }

    for (int i = 0; i < N; i++) {
        if (isSafe(board, i, col, N)) {
            board[i][col] = 1;
            solveNQueensAll(board, col + 1, N, solutionCount);
            board[i][col] = 0; // Backtrack
        }
    }
}

int main() {
    int N;
    printf("Enter the number of queens: ");
    scanf("%d", &N);
    // Dynamically allocate NxN board
    int** board = (int**)malloc(N *

```

```

sizeof(int*)); for (int i = 0; i < N; i++) {
    board[i] = (int*)calloc(N, sizeof(int));
}

int solutionCount = 0;
solveNQueensAll(board, 0, N,
&solutionCount); if (solutionCount == 0)
printf("No solutions found for %d-Queens.\n", N);
else
printf("Total solutions found: %d\n", solutionCount);
// Free allocated memory

for (int i = 0; i < N; i++)
free(board[i]);
free(board);

return 0;
}

```

Result:

Output
<pre> Enter the number of queens: 4 2 4 1 3 Solution found 3 1 4 2 Solution found Total solutions: 2 ==== Code Execution Successful ==== </pre>

Algorithm and Tracing :

22/8/25

N-Queen ProblemAlgorithm:

1. Start with the first row ($k=1$).
2. Try placing a queen in the current row.
 - * Move through each column from left to right.
 - * For each column, check if placing a queen there is safe.
3. If a safe position is found:
 - * Place the queen.
 - * If this is the last row ($k=n$), print solution.
 - * Otherwise, move to the next row ($k=k+1$) and repeat step 2.
4. If no safe column in the current row:
 - * Backtrack to the previous row ($k=k-1$) and try the next column there.
5. Repeat steps 2-4 until all solutions are found.
6. Print the total no. of solutions found.

Output:

Enter the number of queen : 4

2 4 1 3

Solution found

3 1 4 2

Solution found

Total solution : 2

Tracing: