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Assignment 7

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Download all python codes from

https://github.com/Dhatri-nanda/AS7/blob/main/ Assignment7/code.py

and latex-tikz codes from

https://github.com/Dhatri-nanda/AS7/blob/main/ Assignment7/Assignment7.tex

1 Problem

An urn has 3 red and 6 black balls. Balls are drawn at random one by one without replacement. The probability that second red appears at fifth draw.

A)
$$\frac{1}{9!}$$

C)
$$4\left(\frac{6!4!}{9!}\right)$$

B)
$$\frac{4!}{9!}$$

D)
$$\frac{6!4!}{9!}$$

2 Solution

For the first four draws, 1 red ball out of the 3 and 3 black balls out of the 6 must appear; the probability this happens is:

$$\frac{{}^{3}C_{1}{}^{6}C_{3}}{{}^{9}C_{4}} \tag{2.0.1}$$

The probability that second red appears at fifth draw is:

$${}^{2}C_{1} \atop {}^{5}C_{1}$$
 (2.0.2)

Therefore the total probability is (from (2.0.1) and (2.0.2)):

$$=\frac{{}^{3}C_{1}{}^{6}C_{3}{}^{2}C_{1}}{{}^{5}C_{1}{}^{9}C_{4}}$$
 (2.0.3)

$$= \frac{3! \times 6! \times 2! \times 4! \times 4! \times 5!}{2! \times 3! \times 3! \times 5! \times 9!}$$
 (2.0.4)

$$=4\left(\frac{4!6!}{9!}\right) \tag{2.0.5}$$

So, the correct option is (C)

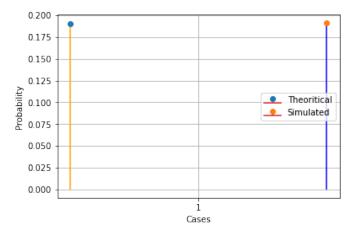


Fig. 4: Simulation and Theoretical Comparison