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## Assignment 7

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## CBSE Probability Grade 12

Exercise 13.3.3: Of the students in a college, it is known that 60% reside in hostel and 40% are day scholars (not residing in hostel). Previous year results report that 30% of all students who reside in hostel attain A grade and 20% of day scholars attain A grade in their annual examination. At the end of the year, one student is chosen at random from the college and he has an A grade, what is the probability that the student is a hostler?

**Solution:** Let random variables  $X, Y \in \{0, 1\}$  denote the following events in Table (I)

Event	Description
X = 0	Student is a hostler
X = 1	Student is a day scholar
Y = 0	Student gets an A grade
Y=1	Student doesn't get an A grade

TABLE I

$$\Pr(X=0) = 60\%$$
 (1)

$$=0.6 (2)$$

$$\Pr(X=1) = 40\%$$
 (3)

$$=0.4\tag{4}$$

$$\Pr(Y = 0|X = 0) = 30\% \tag{5}$$

$$=0.3$$
 (6)

$$\Pr(Y = 0|X = 1) = 20\% \tag{7}$$

$$=0.2 \tag{8}$$

$$\begin{array}{c|ccc} \textbf{Probability} & \textbf{Value} \\ Pr \, (X=0) & 0.6 \\ Pr \, (X=1) & 0.4 \\ Pr \, (Y=0|X=0) & 0.3 \\ Pr \, (Y=0|X=1) & 0.2 \\ Pr \, (X=0|Y=0) & ? \\ \end{array}$$

TABLE II

Probability that the student selected is a hostler, if he has an A grade is

$$\Pr\left(X=0|Y=0\right) \tag{9}$$

$$= \frac{\Pr(X=0, Y=0)}{\Pr(Y=0)}$$
 (10)

$$= \frac{\Pr(Y=0|X=0)\Pr(X=0)}{\sum_{i=0}^{1} \Pr(Y=0,X=i)}$$
(11)

$$= \frac{\Pr(X = 0, Y = 0)}{\Pr(Y = 0)}$$

$$= \frac{\Pr(Y = 0|X = 0) \Pr(X = 0)}{\sum_{i=0}^{1} \Pr(Y = 0, X = i)}$$

$$= \frac{\Pr(Y = 0|X = 0) \Pr(X = 0)}{\sum_{i=0}^{1} \Pr(Y = 0|X = i) \Pr(X = i)}$$
(12)

On substituting the values from Table (II) we get:

$$\Pr(X = 0|Y = 0) = \frac{0.3 \times 0.6}{0.3 \times 0.6 + 0.2 \times 0.4}$$
 (13)

$$=\frac{0.18}{0.26}\tag{14}$$

$$= \frac{9}{13} \approx 0.69 \tag{15}$$

Probability that the student selected is a hostler, if he has an A grade is 0.69.