Question 3-3.3-12

EE24BTECH11015 - Dhawal

1) Construct a $\triangle ABC$ in which AB = 6cm, BC = 8cm and $\angle ABC = 60^{\circ}$.

Variable	Description	Values
AB	Length	6 cm
BC	Length	8 cm
∠ABC	Angle	60°
A	Point	(6,0)
В	Origin	(0,0)
$R(\theta)$	Rotational Matrix	
С	To find	?

TABLE 1: Variables given

Solution:

As AB = 6cm put:

$$\mathbf{A} = \begin{pmatrix} 6 \\ 0 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \tag{1.1}$$

Let $R(\theta)$ be rotational matrix; Then

$$BC = R(60^{\circ}) \begin{pmatrix} 8 \\ 0 \end{pmatrix} = \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \begin{pmatrix} 8 \\ 0 \end{pmatrix} = \begin{pmatrix} 4 \\ 4\sqrt{3} \end{pmatrix}$$
 (1.2)

Hence

$$\mathbf{C} = \begin{pmatrix} 4\\4\sqrt{3} \end{pmatrix} \tag{1.3}$$

Plot:

Triangle ABC with Points on Line Segments AB, BC, and CA

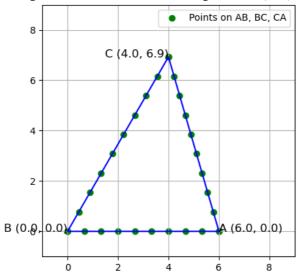


Fig. 1.1: Δ*ABC*